

Maple 2018.2 Integration Test Results  
on the problems in "6 Hyperbolic functions/6.1 Hyperbolic sine"

Test results for the 136 problems in "6.1.1 (c+d x)^m (a+b sinh)^n.txt"

Problem 1: Result more than twice size of optimal antiderivative.

$$\int (dx + c)^4 \sinh(bx + a) dx$$

Optimal(type 3, 91 leaves, 5 steps):

$$\frac{24 d^4 \cosh(bx + a)}{b^5} + \frac{12 d^2 (dx + c)^2 \cosh(bx + a)}{b^3} + \frac{(dx + c)^4 \cosh(bx + a)}{b} - \frac{24 d^3 (dx + c) \sinh(bx + a)}{b^4} - \frac{4 d (dx + c)^3 \sinh(bx + a)}{b^2}$$

Result(type 3, 546 leaves):

$$\begin{aligned} & \frac{1}{b} \left( c^4 \cosh(bx + a) - \frac{12 d^3 a c ((bx + a)^2 \cosh(bx + a) - 2 (bx + a) \sinh(bx + a) + 2 \cosh(bx + a))}{b^3} \right. \\ & + \frac{12 d^3 a^2 c ((bx + a) \cosh(bx + a) - \sinh(bx + a))}{b^3} - \frac{12 d^2 a c^2 ((bx + a) \cosh(bx + a) - \sinh(bx + a))}{b^2} \\ & + \frac{d^4 ((bx + a)^4 \cosh(bx + a) - 4 (bx + a)^3 \sinh(bx + a) + 12 (bx + a)^2 \cosh(bx + a) - 24 (bx + a) \sinh(bx + a) + 24 \cosh(bx + a))}{b^4} \\ & + \frac{d^4 a^4 \cosh(bx + a)}{b^4} - \frac{4 d^4 a^3 ((bx + a) \cosh(bx + a) - \sinh(bx + a))}{b^4} + \frac{4 d c^3 ((bx + a) \cosh(bx + a) - \sinh(bx + a))}{b} \\ & - \frac{4 d^3 a^3 c \cosh(bx + a)}{b^3} + \frac{6 d^2 a^2 c^2 \cosh(bx + a)}{b^2} - \frac{4 d a c^3 \cosh(bx + a)}{b} \\ & - \frac{4 d^4 a ((bx + a)^3 \cosh(bx + a) - 3 (bx + a)^2 \sinh(bx + a) + 6 (bx + a) \cosh(bx + a) - 6 \sinh(bx + a))}{b^4} \\ & + \frac{4 d^3 c ((bx + a)^3 \cosh(bx + a) - 3 (bx + a)^2 \sinh(bx + a) + 6 (bx + a) \cosh(bx + a) - 6 \sinh(bx + a))}{b^3} \\ & + \frac{6 d^4 a^2 ((bx + a)^2 \cosh(bx + a) - 2 (bx + a) \sinh(bx + a) + 2 \cosh(bx + a))}{b^4} \\ & \left. + \frac{6 d^2 c^2 ((bx + a)^2 \cosh(bx + a) - 2 (bx + a) \sinh(bx + a) + 2 \cosh(bx + a))}{b^2} \right) \end{aligned}$$

Problem 2: Result more than twice size of optimal antiderivative.

$$\int (dx + c)^2 \sinh(bx + a) dx$$

Optimal(type 3, 49 leaves, 3 steps):

$$\frac{2 d^2 \cosh(bx + a)}{b^3} + \frac{(dx + c)^2 \cosh(bx + a)}{b} - \frac{2 d (dx + c) \sinh(bx + a)}{b^2}$$

Result(type 3, 146 leaves):

$$\frac{1}{b} \left( \frac{d^2 \left( (bx+a)^2 \cosh(bx+a) - 2(bx+a) \sinh(bx+a) + 2 \cosh(bx+a) \right)}{b^2} - \frac{2d^2 a \left( (bx+a) \cosh(bx+a) - \sinh(bx+a) \right)}{b^2} \right. \\ \left. + \frac{2dc \left( (bx+a) \cosh(bx+a) - \sinh(bx+a) \right)}{b} + \frac{d^2 a^2 \cosh(bx+a)}{b^2} - \frac{2dac \cosh(bx+a)}{b} + c^2 \cosh(bx+a) \right)$$

Problem 3: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(bx+a)}{(dx+c)^3} dx$$

Optimal(type 4, 96 leaves, 5 steps):

$$-\frac{b \cosh(bx+a)}{2d^2(dx+c)} + \frac{b^2 \cosh\left(a - \frac{bc}{d}\right) \text{Shi}\left(\frac{bc}{d} + bx\right)}{2d^3} + \frac{b^2 \text{Chi}\left(\frac{bc}{d} + bx\right) \sinh\left(a - \frac{bc}{d}\right)}{2d^3} - \frac{\sinh(bx+a)}{2d(dx+c)^2}$$

Result(type 4, 276 leaves):

$$-\frac{b^3 e^{-bx-a} x}{4d(b^2 d^2 x^2 + 2b^2 c dx + c^2 b^2)} - \frac{b^3 e^{-bx-a} c}{4d^2(b^2 d^2 x^2 + 2b^2 c dx + c^2 b^2)} + \frac{b^2 e^{-bx-a}}{4d(b^2 d^2 x^2 + 2b^2 c dx + c^2 b^2)} + \frac{b^2 e^{-\frac{ad-cb}{d}} \text{Ei}_1\left(bx+a - \frac{ad-cb}{d}\right)}{4d^3} \\ - \frac{b^2 e^{bx+a}}{4d^3 \left(\frac{bc}{d} + bx\right)^2} - \frac{b^2 e^{bx+a}}{4d^3 \left(\frac{bc}{d} + bx\right)} - \frac{b^2 e^{\frac{ad-cb}{d}} \text{Ei}_1\left(-bx-a - \frac{-ad+cb}{d}\right)}{4d^3}$$

Problem 4: Result more than twice size of optimal antiderivative.

$$\int (dx+c)^2 \sinh(bx+a)^2 dx$$

Optimal(type 3, 85 leaves, 4 steps):

$$-\frac{d^2 x}{4b^2} - \frac{(dx+c)^3}{6d} + \frac{d^2 \cosh(bx+a) \sinh(bx+a)}{4b^3} + \frac{(dx+c)^2 \cosh(bx+a) \sinh(bx+a)}{2b} - \frac{d(dx+c) \sinh(bx+a)^2}{2b^2}$$

Result(type 3, 261 leaves):

$$\frac{1}{b} \left( \frac{d^2 \left( \frac{(bx+a)^2 \cosh(bx+a) \sinh(bx+a)}{2} - \frac{(bx+a)^3}{6} - \frac{(bx+a) \cosh(bx+a)^2}{2} + \frac{\cosh(bx+a) \sinh(bx+a)}{4} + \frac{bx}{4} + \frac{a}{4} \right)}{b^2} \right. \\ \left. - \frac{2d^2 a \left( \frac{(bx+a) \cosh(bx+a) \sinh(bx+a)}{2} - \frac{(bx+a)^2}{4} - \frac{\cosh(bx+a)^2}{4} \right)}{b^2} \right)$$

$$\begin{aligned}
& + \frac{2dc \left( \frac{(bx+a) \cosh(bx+a) \sinh(bx+a)}{2} - \frac{(bx+a)^2}{4} - \frac{\cosh(bx+a)^2}{4} \right)}{b} + \frac{d^2 a^2 \left( \frac{\cosh(bx+a) \sinh(bx+a)}{2} - \frac{bx}{2} - \frac{a}{2} \right)}{b^2} \\
& - \frac{2dac \left( \frac{\cosh(bx+a) \sinh(bx+a)}{2} - \frac{bx}{2} - \frac{a}{2} \right)}{b} + c^2 \left( \frac{\cosh(bx+a) \sinh(bx+a)}{2} - \frac{bx}{2} - \frac{a}{2} \right)
\end{aligned}$$

Problem 5: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(bx+a)^2}{(dx+c)^4} dx$$

Optimal (type 4, 150 leaves, 7 steps):

$$\begin{aligned}
& - \frac{b^2}{3d^3(dx+c)} + \frac{2b^3 \cosh\left(2a - \frac{2bc}{d}\right) \text{Shi}\left(\frac{2bc}{d} + 2bx\right)}{3d^4} + \frac{2b^3 \text{Chi}\left(\frac{2bc}{d} + 2bx\right) \sinh\left(2a - \frac{2bc}{d}\right)}{3d^4} - \frac{b \cosh(bx+a) \sinh(bx+a)}{3d^2(dx+c)^2} \\
& - \frac{\sinh(bx+a)^2}{3d(dx+c)^3} - \frac{2b^2 \sinh(bx+a)^2}{3d^3(dx+c)}
\end{aligned}$$

Result (type 4, 554 leaves):

$$\begin{aligned}
& \frac{1}{6d(dx+c)^3} - \frac{b^5 e^{-2bx-2a} x^2}{6d(b^3 d^3 x^3 + 3b^3 c d^2 x^2 + 3b^3 c^2 dx + b^3 c^3)} - \frac{b^5 e^{-2bx-2a} cx}{3d^2(b^3 d^3 x^3 + 3b^3 c d^2 x^2 + 3b^3 c^2 dx + b^3 c^3)} \\
& - \frac{b^5 e^{-2bx-2a} c^2}{6d^3(b^3 d^3 x^3 + 3b^3 c d^2 x^2 + 3b^3 c^2 dx + b^3 c^3)} + \frac{b^4 e^{-2bx-2a} x}{12d(b^3 d^3 x^3 + 3b^3 c d^2 x^2 + 3b^3 c^2 dx + b^3 c^3)} \\
& + \frac{b^4 e^{-2bx-2a} c}{12d^2(b^3 d^3 x^3 + 3b^3 c d^2 x^2 + 3b^3 c^2 dx + b^3 c^3)} - \frac{b^3 e^{-2bx-2a}}{12d(b^3 d^3 x^3 + 3b^3 c d^2 x^2 + 3b^3 c^2 dx + b^3 c^3)} \\
& + \frac{b^3 e^{-\frac{2(ad-cb)}{d}} \text{Ei}_1\left(2bx + 2a - \frac{2(ad-cb)}{d}\right)}{3d^4} - \frac{b^3 e^{2bx+2a}}{12d^4\left(\frac{bc}{d} + bx\right)^3} - \frac{b^3 e^{2bx+2a}}{12d^4\left(\frac{bc}{d} + bx\right)^2} - \frac{b^3 e^{2bx+2a}}{6d^4\left(\frac{bc}{d} + bx\right)} \\
& - \frac{b^3 e^{\frac{2(ad-cb)}{d}} \text{Ei}_1\left(-2bx - 2a - \frac{2(-ad+cb)}{d}\right)}{3d^4}
\end{aligned}$$

Problem 6: Result more than twice size of optimal antiderivative.

$$\int (dx+c)^4 \sinh(bx+a)^3 dx$$

Optimal (type 3, 205 leaves, 12 steps):

$$\begin{aligned}
& - \frac{488 d^4 \cosh(bx+a)}{27 b^5} - \frac{80 d^2 (dx+c)^2 \cosh(bx+a)}{9 b^3} - \frac{2 (dx+c)^4 \cosh(bx+a)}{3 b} + \frac{8 d^4 \cosh(bx+a)^3}{81 b^5} + \frac{160 d^3 (dx+c) \sinh(bx+a)}{9 b^4} \\
& + \frac{8 d (dx+c)^3 \sinh(bx+a)}{3 b^2} + \frac{4 d^2 (dx+c)^2 \cosh(bx+a) \sinh(bx+a)^2}{9 b^3} + \frac{(dx+c)^4 \cosh(bx+a) \sinh(bx+a)^2}{3 b} \\
& - \frac{8 d^3 (dx+c) \sinh(bx+a)^3}{27 b^4} - \frac{4 d (dx+c)^3 \sinh(bx+a)^3}{9 b^2}
\end{aligned}$$

Result(type 3, 1216 leaves):

$$\begin{aligned}
& \frac{1}{b} \left( \frac{1}{b^4} \left( d^4 \left( -\frac{2 (bx+a)^4 \cosh(bx+a)}{3} + \frac{(bx+a)^4 \cosh(bx+a) \sinh(bx+a)^2}{3} + \frac{28 (bx+a)^3 \sinh(bx+a)}{9} - \frac{80 (bx+a)^2 \cosh(bx+a)}{9} \right. \right. \right. \\
& + \frac{488 (bx+a) \sinh(bx+a)}{27} - \frac{1456 \cosh(bx+a)}{81} - \frac{4 (bx+a)^3 \sinh(bx+a) \cosh(bx+a)^2}{9} + \frac{4 (bx+a)^2 \sinh(bx+a)^2 \cosh(bx+a)}{9} \\
& - \left. \left. \left. \frac{8 (bx+a) \sinh(bx+a) \cosh(bx+a)^2}{27} + \frac{8 \sinh(bx+a)^2 \cosh(bx+a)}{81} \right) \right) - \frac{1}{b^4} \left( 4 d^4 a \left( -\frac{2 (bx+a)^3 \cosh(bx+a)}{3} \right. \right. \\
& + \frac{(bx+a)^3 \cosh(bx+a) \sinh(bx+a)^2}{3} + \frac{7 (bx+a)^2 \sinh(bx+a)}{3} - \frac{40 (bx+a) \cosh(bx+a)}{9} + \frac{122 \sinh(bx+a)}{27} \\
& - \left. \left. \left. \frac{(bx+a)^2 \sinh(bx+a) \cosh(bx+a)^2}{3} + \frac{2 (bx+a) \sinh(bx+a)^2 \cosh(bx+a)}{9} - \frac{2 \sinh(bx+a) \cosh(bx+a)^2}{27} \right) \right) \right) \\
& + \frac{1}{b^4} \left( 6 d^4 a^2 \left( \frac{(bx+a)^2 \sinh(bx+a)^2 \cosh(bx+a)}{3} - \frac{2 (bx+a)^2 \cosh(bx+a)}{3} - \frac{2 (bx+a) \sinh(bx+a) \cosh(bx+a)^2}{9} \right. \right. \\
& + \left. \left. \left. \frac{14 (bx+a) \sinh(bx+a)}{9} + \frac{2 \sinh(bx+a)^2 \cosh(bx+a)}{27} - \frac{40 \cosh(bx+a)}{27} \right) \right) \right) \\
& - \frac{4 d^4 a^3 \left( -\frac{2 (bx+a) \cosh(bx+a)}{3} + \frac{(bx+a) \sinh(bx+a)^2 \cosh(bx+a)}{3} + \frac{7 \sinh(bx+a)}{9} - \frac{\sinh(bx+a) \cosh(bx+a)^2}{9} \right)}{b^4} \\
& + \frac{d^4 a^4 \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a)}{b^4} + \frac{1}{b^3} \left( 4 c d^3 \left( -\frac{2 (bx+a)^3 \cosh(bx+a)}{3} + \frac{(bx+a)^3 \cosh(bx+a) \sinh(bx+a)^2}{3} \right. \right. \\
& + \left. \left. \left. \frac{7 (bx+a)^2 \sinh(bx+a)}{3} - \frac{40 (bx+a) \cosh(bx+a)}{9} + \frac{122 \sinh(bx+a)}{27} - \frac{(bx+a)^2 \sinh(bx+a) \cosh(bx+a)^2}{3} \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& + \frac{2 (bx+a) \sinh(bx+a)^2 \cosh(bx+a)}{9} - \frac{2 \sinh(bx+a) \cosh(bx+a)^2}{27} \Big) - \frac{1}{b^3} \left( 12 c d^3 a \left( \frac{(bx+a)^2 \sinh(bx+a)^2 \cosh(bx+a)}{3} \right. \right. \\
& - \frac{2 (bx+a)^2 \cosh(bx+a)}{3} - \frac{2 (bx+a) \sinh(bx+a) \cosh(bx+a)^2}{9} + \frac{14 (bx+a) \sinh(bx+a)}{9} + \frac{2 \sinh(bx+a)^2 \cosh(bx+a)}{27} \\
& \left. \left. - \frac{40 \cosh(bx+a)}{27} \right) \right) \\
& + \frac{12 c d^3 a^2 \left( -\frac{2 (bx+a) \cosh(bx+a)}{3} + \frac{(bx+a) \sinh(bx+a)^2 \cosh(bx+a)}{3} + \frac{7 \sinh(bx+a)}{9} - \frac{\sinh(bx+a) \cosh(bx+a)^2}{9} \right)}{b^3} \\
& - \frac{4 c d^3 a^3 \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a)}{b^3} + \frac{1}{b^2} \left( 6 c^2 d^2 \left( \frac{(bx+a)^2 \sinh(bx+a)^2 \cosh(bx+a)}{3} - \frac{2 (bx+a)^2 \cosh(bx+a)}{3} \right. \right. \\
& \left. \left. - \frac{2 (bx+a) \sinh(bx+a) \cosh(bx+a)^2}{9} + \frac{14 (bx+a) \sinh(bx+a)}{9} + \frac{2 \sinh(bx+a)^2 \cosh(bx+a)}{27} - \frac{40 \cosh(bx+a)}{27} \right) \right) \\
& - \frac{12 c^2 d^2 a \left( -\frac{2 (bx+a) \cosh(bx+a)}{3} + \frac{(bx+a) \sinh(bx+a)^2 \cosh(bx+a)}{3} + \frac{7 \sinh(bx+a)}{9} - \frac{\sinh(bx+a) \cosh(bx+a)^2}{9} \right)}{b^2} \\
& + \frac{6 c^2 d^2 a^2 \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a)}{b^2} \\
& + \frac{4 c^3 d \left( -\frac{2 (bx+a) \cosh(bx+a)}{3} + \frac{(bx+a) \sinh(bx+a)^2 \cosh(bx+a)}{3} + \frac{7 \sinh(bx+a)}{9} - \frac{\sinh(bx+a) \cosh(bx+a)^2}{9} \right)}{b} \\
& - \frac{4 c^3 d a \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a)}{b} + c^4 \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a) \Big)
\end{aligned}$$

Problem 7: Result more than twice size of optimal antiderivative.

$$\int (dx+c)^3 \sinh(bx+a)^3 dx$$

Optimal (type 3, 161 leaves, 8 steps):

$$-\frac{40 d^2 (dx+c) \cosh(bx+a)}{9 b^3} - \frac{2 (dx+c)^3 \cosh(bx+a)}{3 b} + \frac{40 d^3 \sinh(bx+a)}{9 b^4} + \frac{2 d (dx+c)^2 \sinh(bx+a)}{b^2}$$

$$+ \frac{2d^2(dx+c)\cosh(bx+a)\sinh(bx+a)^2}{9b^3} + \frac{(dx+c)^3\cosh(bx+a)\sinh(bx+a)^2}{3b} - \frac{2d^3\sinh(bx+a)^3}{27b^4} - \frac{d(dx+c)^2\sinh(bx+a)^3}{3b^2}$$

Result (type 3, 675 leaves):

$$\begin{aligned} & \frac{1}{b} \left( \frac{1}{b^3} \left( d^3 \left( -\frac{2(bx+a)^3\cosh(bx+a)}{3} + \frac{(bx+a)^3\cosh(bx+a)\sinh(bx+a)^2}{3} + \frac{7(bx+a)^2\sinh(bx+a)}{3} - \frac{40(bx+a)\cosh(bx+a)}{9} \right. \right. \right. \\ & + \left. \left. \frac{122\sinh(bx+a)}{27} - \frac{(bx+a)^2\sinh(bx+a)\cosh(bx+a)^2}{3} + \frac{2(bx+a)\sinh(bx+a)^2\cosh(bx+a)}{9} - \frac{2\sinh(bx+a)\cosh(bx+a)^2}{27} \right) \right) \\ & - \frac{1}{b^3} \left( 3d^3a \left( \frac{(bx+a)^2\sinh(bx+a)^2\cosh(bx+a)}{3} - \frac{2(bx+a)^2\cosh(bx+a)}{3} - \frac{2(bx+a)\sinh(bx+a)\cosh(bx+a)^2}{9} \right. \right. \\ & + \left. \left. \frac{14(bx+a)\sinh(bx+a)}{9} + \frac{2\sinh(bx+a)^2\cosh(bx+a)}{27} - \frac{40\cosh(bx+a)}{27} \right) \right) + \frac{1}{b^2} \left( 3d^2c \left( \frac{(bx+a)^2\sinh(bx+a)^2\cosh(bx+a)}{3} \right. \right. \\ & - \frac{2(bx+a)^2\cosh(bx+a)}{3} - \frac{2(bx+a)\sinh(bx+a)\cosh(bx+a)^2}{9} + \frac{14(bx+a)\sinh(bx+a)}{9} + \frac{2\sinh(bx+a)^2\cosh(bx+a)}{27} \\ & - \left. \left. \frac{40\cosh(bx+a)}{27} \right) \right) \\ & + \frac{3d^3a^2 \left( -\frac{2(bx+a)\cosh(bx+a)}{3} + \frac{(bx+a)\sinh(bx+a)^2\cosh(bx+a)}{3} + \frac{7\sinh(bx+a)}{9} - \frac{\sinh(bx+a)\cosh(bx+a)^2}{9} \right)}{b^3} \\ & - \frac{6d^2ac \left( -\frac{2(bx+a)\cosh(bx+a)}{3} + \frac{(bx+a)\sinh(bx+a)^2\cosh(bx+a)}{3} + \frac{7\sinh(bx+a)}{9} - \frac{\sinh(bx+a)\cosh(bx+a)^2}{9} \right)}{b^2} \\ & + \frac{3c^2d \left( -\frac{2(bx+a)\cosh(bx+a)}{3} + \frac{(bx+a)\sinh(bx+a)^2\cosh(bx+a)}{3} + \frac{7\sinh(bx+a)}{9} - \frac{\sinh(bx+a)\cosh(bx+a)^2}{9} \right)}{b} \\ & - \frac{d^3a^3 \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a)}{b^3} + \frac{3d^2a^2c \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a)}{b^2} \\ & - \frac{3da^2c^2 \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a)}{b} + c^3 \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a) \end{aligned}$$

Problem 8: Result more than twice size of optimal antiderivative.

$$\int (dx+c)^2 \sinh(bx+a)^3 dx$$

Optimal(type 3, 111 leaves, 6 steps):

$$\begin{aligned} & -\frac{14 d^2 \cosh(bx+a)}{9 b^3} - \frac{2 (dx+c)^2 \cosh(bx+a)}{3 b} + \frac{2 d^2 \cosh(bx+a)^3}{27 b^3} + \frac{4 d (dx+c) \sinh(bx+a)}{3 b^2} + \frac{(dx+c)^2 \cosh(bx+a) \sinh(bx+a)^2}{3 b} \\ & - \frac{2 d (dx+c) \sinh(bx+a)^3}{9 b^2} \end{aligned}$$

Result(type 3, 319 leaves):

$$\begin{aligned} & \frac{1}{b} \left( \frac{1}{b^2} \left( d^2 \left( \frac{(bx+a)^2 \sinh(bx+a)^2 \cosh(bx+a)}{3} - \frac{2 (bx+a)^2 \cosh(bx+a)}{3} - \frac{2 (bx+a) \sinh(bx+a) \cosh(bx+a)^2}{9} \right. \right. \right. \\ & \left. \left. \left. + \frac{14 (bx+a) \sinh(bx+a)}{9} + \frac{2 \sinh(bx+a)^2 \cosh(bx+a)}{27} - \frac{40 \cosh(bx+a)}{27} \right) \right) \\ & - \frac{2 d^2 a \left( -\frac{2 (bx+a) \cosh(bx+a)}{3} + \frac{(bx+a) \sinh(bx+a)^2 \cosh(bx+a)}{3} + \frac{7 \sinh(bx+a)}{9} - \frac{\sinh(bx+a) \cosh(bx+a)^2}{9} \right)}{b^2} \\ & + \frac{2 d c \left( -\frac{2 (bx+a) \cosh(bx+a)}{3} + \frac{(bx+a) \sinh(bx+a)^2 \cosh(bx+a)}{3} + \frac{7 \sinh(bx+a)}{9} - \frac{\sinh(bx+a) \cosh(bx+a)^2}{9} \right)}{b} \\ & + \frac{d^2 a^2 \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a)}{b^2} - \frac{2 d a c \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a)}{b} + c^2 \left( -\frac{2}{3} + \frac{\sinh(bx+a)^2}{3} \right) \cosh(bx+a) \end{aligned}$$

Problem 10: Result more than twice size of optimal antiderivative.

$$\int (dx+c)^3 \operatorname{csch}(bx+a) dx$$

Optimal(type 4, 142 leaves, 9 steps):

$$\begin{aligned} & -\frac{2 (dx+c)^3 \operatorname{arctanh}(e^{bx+a})}{b} - \frac{3 d (dx+c)^2 \operatorname{polylog}(2, -e^{bx+a})}{b^2} + \frac{3 d (dx+c)^2 \operatorname{polylog}(2, e^{bx+a})}{b^2} + \frac{6 d^2 (dx+c) \operatorname{polylog}(3, -e^{bx+a})}{b^3} \\ & - \frac{6 d^2 (dx+c) \operatorname{polylog}(3, e^{bx+a})}{b^3} - \frac{6 d^3 \operatorname{polylog}(4, -e^{bx+a})}{b^4} + \frac{6 d^3 \operatorname{polylog}(4, e^{bx+a})}{b^4} \end{aligned}$$

Result(type 4, 540 leaves):

$$\frac{3 c^2 d \ln(1 - e^{bx+a}) a}{b^2} - \frac{3 c^2 d \ln(1 + e^{bx+a}) x}{b} - \frac{3 c^2 d \ln(1 + e^{bx+a}) a}{b^2} + \frac{3 d^2 c \ln(1 - e^{bx+a}) x^2}{b} - \frac{3 d^2 c \ln(1 - e^{bx+a}) a^2}{b^3}$$

$$\begin{aligned}
& + \frac{6 d^2 c \operatorname{polylog}(2, e^{bx+a}) x}{b^2} - \frac{3 d^2 c \ln(1 + e^{bx+a}) x^2}{b} + \frac{3 d^2 c \ln(1 + e^{bx+a}) a^2}{b^3} - \frac{6 d^2 c \operatorname{polylog}(2, -e^{bx+a}) x}{b^2} + \frac{6 d a c^2 \operatorname{arctanh}(e^{bx+a})}{b^2} \\
& - \frac{6 d^2 a^2 c \operatorname{arctanh}(e^{bx+a})}{b^3} + \frac{3 c^2 d \ln(1 - e^{bx+a}) x}{b} - \frac{2 c^3 \operatorname{arctanh}(e^{bx+a})}{b} - \frac{6 d^3 \operatorname{polylog}(4, -e^{bx+a})}{b^4} + \frac{6 d^3 \operatorname{polylog}(4, e^{bx+a})}{b^4} \\
& + \frac{6 d^3 \operatorname{polylog}(3, -e^{bx+a}) x}{b^3} - \frac{6 d^2 c \operatorname{polylog}(3, e^{bx+a})}{b^3} + \frac{6 d^2 c \operatorname{polylog}(3, -e^{bx+a})}{b^3} + \frac{3 c^2 d \operatorname{polylog}(2, e^{bx+a})}{b^2} - \frac{3 c^2 d \operatorname{polylog}(2, -e^{bx+a})}{b^2} \\
& + \frac{2 d^3 a^3 \operatorname{arctanh}(e^{bx+a})}{b^4} + \frac{d^3 a^3 \ln(1 - e^{bx+a})}{b^4} - \frac{d^3 a^3 \ln(1 + e^{bx+a})}{b^4} + \frac{d^3 \ln(1 - e^{bx+a}) x^3}{b} + \frac{3 d^3 \operatorname{polylog}(2, e^{bx+a}) x^2}{b^2} \\
& - \frac{6 d^3 \operatorname{polylog}(3, e^{bx+a}) x}{b^3} - \frac{d^3 \ln(1 + e^{bx+a}) x^3}{b} - \frac{3 d^3 \operatorname{polylog}(2, -e^{bx+a}) x^2}{b^2}
\end{aligned}$$

Problem 11: Result more than twice size of optimal antiderivative.

$$\int (dx + c)^2 \operatorname{csch}(bx + a)^2 dx$$

Optimal (type 4, 74 leaves, 5 steps):

$$-\frac{(dx + c)^2}{b} - \frac{(dx + c)^2 \operatorname{coth}(bx + a)}{b} + \frac{2d(dx + c) \ln(1 - e^{2bx+2a})}{b^2} + \frac{d^2 \operatorname{polylog}(2, e^{2bx+2a})}{b^3}$$

Result (type 4, 239 leaves):

$$\begin{aligned}
& - \frac{2(d^2 x^2 + 2cdx + c^2)}{b(e^{2bx+2a} - 1)} + \frac{2dc \ln(e^{bx+a} - 1)}{b^2} - \frac{4dc \ln(e^{bx+a})}{b^2} + \frac{2dc \ln(1 + e^{bx+a})}{b^2} - \frac{2d^2 x^2}{b} - \frac{4d^2 ax}{b^2} - \frac{2d^2 a^2}{b^3} + \frac{2d^2 \ln(1 - e^{bx+a}) x}{b^2} \\
& + \frac{2d^2 \ln(1 - e^{bx+a}) a}{b^3} + \frac{2d^2 \operatorname{polylog}(2, e^{bx+a})}{b^3} + \frac{2d^2 \ln(1 + e^{bx+a}) x}{b^2} + \frac{2d^2 \operatorname{polylog}(2, -e^{bx+a})}{b^3} - \frac{2d^2 a \ln(e^{bx+a} - 1)}{b^3} + \frac{4d^2 a \ln(e^{bx+a})}{b^3}
\end{aligned}$$

Problem 12: Result more than twice size of optimal antiderivative.

$$\int (dx + c) \operatorname{csch}(bx + a)^3 dx$$

Optimal (type 4, 81 leaves, 6 steps):

$$\frac{(dx + c) \operatorname{arctanh}(e^{bx+a})}{b} - \frac{d \operatorname{csch}(bx + a)}{2b^2} - \frac{(dx + c) \operatorname{coth}(bx + a) \operatorname{csch}(bx + a)}{2b} + \frac{d \operatorname{polylog}(2, -e^{bx+a})}{2b^2} - \frac{d \operatorname{polylog}(2, e^{bx+a})}{2b^2}$$

Result (type 4, 196 leaves):

$$\begin{aligned}
& - \frac{e^{bx+a} (bdxe^{2bx+2a} + bce^{2bx+2a} + bdx + de^{2bx+2a} + cb - d)}{b^2 (e^{2bx+2a} - 1)^2} + \frac{c \operatorname{arctanh}(e^{bx+a})}{b} - \frac{d \ln(1 - e^{bx+a}) x}{2b} - \frac{d \ln(1 - e^{bx+a}) a}{2b^2} \\
& - \frac{d \operatorname{polylog}(2, e^{bx+a})}{2b^2} + \frac{d \ln(1 + e^{bx+a}) x}{2b} + \frac{da \ln(1 + e^{bx+a})}{2b^2} + \frac{d \operatorname{polylog}(2, -e^{bx+a})}{2b^2} - \frac{da \operatorname{arctanh}(e^{bx+a})}{b^2}
\end{aligned}$$



Problem 13: Unable to integrate problem.

$$\int (dx+c)^{3/2} \sinh(bx+a) dx$$

Optimal(type 4, 110 leaves, 7 steps):

$$\frac{(dx+c)^{3/2} \cosh(bx+a)}{b} - \frac{3d^{3/2} e^{-a+\frac{bc}{d}} \operatorname{erf}\left(\frac{\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{\pi}}{8b^5/2} + \frac{3d^{3/2} e^{a-\frac{bc}{d}} \operatorname{erfi}\left(\frac{\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{\pi}}{8b^5/2} - \frac{3d \sinh(bx+a) \sqrt{dx+c}}{2b^2}$$

Result(type 8, 16 leaves):

$$\int (dx+c)^{3/2} \sinh(bx+a) dx$$

Problem 14: Unable to integrate problem.

$$\int \frac{\sinh(bx+a)}{\sqrt{dx+c}} dx$$

Optimal(type 4, 74 leaves, 5 steps):

$$-\frac{e^{-a+\frac{bc}{d}} \operatorname{erf}\left(\frac{\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{\pi}}{2\sqrt{b}\sqrt{d}} + \frac{e^{a-\frac{bc}{d}} \operatorname{erfi}\left(\frac{\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{\pi}}{2\sqrt{b}\sqrt{d}}$$

Result(type 8, 16 leaves):

$$\int \frac{\sinh(bx+a)}{\sqrt{dx+c}} dx$$

Problem 15: Unable to integrate problem.

$$\int (dx+c)^{5/2} \sinh(bx+a)^2 dx$$

Optimal(type 4, 183 leaves, 10 steps):

$$-\frac{5d(dx+c)^{3/2}}{16b^2} - \frac{(dx+c)^{7/2}}{7d} + \frac{(dx+c)^{5/2} \cosh(bx+a) \sinh(bx+a)}{2b} - \frac{5d(dx+c)^{3/2} \sinh(bx+a)^2}{8b^2} + \frac{15d^{5/2} e^{-2a+\frac{2bc}{d}} \operatorname{erf}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{2}\sqrt{\pi}}{512b^7/2} - \frac{15d^{5/2} e^{2a-\frac{2bc}{d}} \operatorname{erfi}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{2}\sqrt{\pi}}{512b^7/2} + \frac{15d^2 \sinh(2bx+2a) \sqrt{dx+c}}{64b^3}$$

Result(type 8, 18 leaves):

$$\int (dx+c)^{5/2} \sinh(bx+a)^2 dx$$

Problem 16: Unable to integrate problem.

$$\int \sinh(bx + a)^2 \sqrt{dx + c} \, dx$$

Optimal(type 4, 122 leaves, 8 steps):

$$-\frac{(dx+c)^{3/2}}{3d} + \frac{e^{-2a+\frac{2bc}{d}} \operatorname{erf}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{d}\sqrt{2}\sqrt{\pi}}{32b^{3/2}} - \frac{e^{2a-\frac{2bc}{d}} \operatorname{erfi}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{d}\sqrt{2}\sqrt{\pi}}{32b^{3/2}} + \frac{\sinh(2bx+2a)\sqrt{dx+c}}{4b}$$

Result(type 8, 18 leaves):

$$\int \sinh(bx + a)^2 \sqrt{dx + c} \, dx$$

Problem 17: Unable to integrate problem.

$$\int \frac{\sinh(bx + a)^2}{(dx + c)^{3/2}} \, dx$$

Optimal(type 4, 109 leaves, 7 steps):

$$-\frac{e^{-2a+\frac{2bc}{d}} \operatorname{erf}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{b}\sqrt{2}\sqrt{\pi}}{2d^{3/2}} + \frac{e^{2a-\frac{2bc}{d}} \operatorname{erfi}\left(\frac{\sqrt{2}\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{b}\sqrt{2}\sqrt{\pi}}{2d^{3/2}} - \frac{2\sinh(bx+a)^2}{d\sqrt{dx+c}}$$

Result(type 8, 18 leaves):

$$\int \frac{\sinh(bx + a)^2}{(dx + c)^{3/2}} \, dx$$

Problem 18: Unable to integrate problem.

$$\int \frac{\sinh(bx + a)^3}{\sqrt{dx + c}} \, dx$$

Optimal(type 4, 162 leaves, 12 steps):

$$-\frac{e^{-3a+\frac{3bc}{d}} \operatorname{erf}\left(\frac{\sqrt{3}\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{3}\sqrt{\pi}}{24\sqrt{b}\sqrt{d}} + \frac{e^{3a-\frac{3bc}{d}} \operatorname{erfi}\left(\frac{\sqrt{3}\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{3}\sqrt{\pi}}{24\sqrt{b}\sqrt{d}} + \frac{3e^{-a+\frac{bc}{d}} \operatorname{erf}\left(\frac{\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{\pi}}{8\sqrt{b}\sqrt{d}} - \frac{3e^{a-\frac{bc}{d}} \operatorname{erfi}\left(\frac{\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{\pi}}{8\sqrt{b}\sqrt{d}}$$

Result(type 8, 18 leaves):

$$\int \frac{\sinh(bx+a)^3}{\sqrt{dx+c}} dx$$

Problem 19: Unable to integrate problem.

$$\int \frac{\sinh(bx+a)^3}{(dx+c)^{7/2}} dx$$

Optimal(type 4, 253 leaves, 19 steps):

$$\begin{aligned} & -\frac{4b \cosh(bx+a) \sinh(bx+a)^2}{5d^2(dx+c)^{3/2}} - \frac{2 \sinh(bx+a)^3}{5d(dx+c)^{5/2}} - \frac{b^5/2 e^{-a+\frac{bc}{d}} \operatorname{erf}\left(\frac{\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{\pi}}{5d^{7/2}} - \frac{b^5/2 e^{a-\frac{bc}{d}} \operatorname{erfi}\left(\frac{\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{\pi}}{5d^{7/2}} \\ & + \frac{3b^5/2 e^{-3a+\frac{3bc}{d}} \operatorname{erf}\left(\frac{\sqrt{3}\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{3}\sqrt{\pi}}{5d^{7/2}} + \frac{3b^5/2 e^{3a-\frac{3bc}{d}} \operatorname{erfi}\left(\frac{\sqrt{3}\sqrt{b}\sqrt{dx+c}}{\sqrt{d}}\right) \sqrt{3}\sqrt{\pi}}{5d^{7/2}} - \frac{16b^2 \sinh(bx+a)}{5d^3 \sqrt{dx+c}} \\ & - \frac{24b^2 \sinh(bx+a)^3}{5d^3 \sqrt{dx+c}} \end{aligned}$$

Result(type 8, 18 leaves):

$$\int \frac{\sinh(bx+a)^3}{(dx+c)^{7/2}} dx$$

Problem 23: Unable to integrate problem.

$$\int \left( \frac{x}{\sinh(x)^{7/2}} + \frac{3x\sqrt{\sinh(x)}}{5} \right) dx$$

Optimal(type 3, 31 leaves, 3 steps):

$$-\frac{2x \cosh(x)}{5 \sinh(x)^{5/2}} - \frac{4}{15 \sinh(x)^{3/2}} + \frac{6x \cosh(x)}{5 \sqrt{\sinh(x)}} - \frac{12 \sqrt{\sinh(x)}}{5}$$

Result(type 8, 16 leaves):

$$\int \left( \frac{x}{\sinh(x)^{7/2}} + \frac{3x\sqrt{\sinh(x)}}{5} \right) dx$$

Problem 24: Result unnecessarily involves higher level functions.

$$\int x^{1+m} \sinh(bx+a) dx$$

Optimal(type 4, 53 leaves, 3 steps):

$$-\frac{e^a x^m \Gamma(2+m, -bx)}{2 b^2 (-bx)^m} + \frac{x^m \Gamma(2+m, bx)}{2 b^2 e^a (bx)^m}$$

Result(type 5, 72 leaves):

$$\frac{x^{2+m} \text{hypergeom}\left(\left[1 + \frac{m}{2}\right], \left[\frac{1}{2}, 2 + \frac{m}{2}\right], \frac{b^2 x^2}{4}\right) \sinh(a)}{2+m} + \frac{b x^{3+m} \text{hypergeom}\left(\left[\frac{3}{2} + \frac{m}{2}\right], \left[\frac{3}{2}, \frac{5}{2} + \frac{m}{2}\right], \frac{b^2 x^2}{4}\right) \cosh(a)}{3+m}$$

Problem 25: Result unnecessarily involves higher level functions.

$$\int x^m \sinh(bx + a) dx$$

Optimal(type 4, 53 leaves, 3 steps):

$$\frac{e^a x^m \Gamma(1+m, -bx)}{2 b (-bx)^m} + \frac{x^m \Gamma(1+m, bx)}{2 b e^a (bx)^m}$$

Result(type 5, 72 leaves):

$$\frac{x^{1+m} \text{hypergeom}\left(\left[\frac{1}{2} + \frac{m}{2}\right], \left[\frac{1}{2}, \frac{3}{2} + \frac{m}{2}\right], \frac{b^2 x^2}{4}\right) \sinh(a)}{1+m} + \frac{b x^{2+m} \text{hypergeom}\left(\left[1 + \frac{m}{2}\right], \left[\frac{3}{2}, 2 + \frac{m}{2}\right], \frac{b^2 x^2}{4}\right) \cosh(a)}{2+m}$$

Problem 26: Unable to integrate problem.

$$\int x^{-3+m} \sinh(bx + a)^2 dx$$

Optimal(type 4, 82 leaves, 5 steps):

$$\frac{x^{-2+m}}{2(2-m)} - \frac{b^2 e^{2a} x^m \Gamma(-2+m, -2bx)}{2^m (-bx)^m} - \frac{b^2 x^m \Gamma(-2+m, 2bx)}{2^m e^{2a} (bx)^m}$$

Result(type 8, 16 leaves):

$$\int x^{-3+m} \sinh(bx + a)^2 dx$$

Problem 27: Unable to integrate problem.

$$\int \left( \frac{x}{\text{csch}(x)^3 / 2} + \frac{x \sqrt{\text{csch}(x)}}{3} \right) dx$$

Optimal(type 3, 16 leaves, 4 steps):

$$-\frac{4}{9 \text{csch}(x)^3 / 2} + \frac{2x \cosh(x)}{3 \sqrt{\text{csch}(x)}}$$

Result(type 8, 16 leaves):

$$\int \left( \frac{x}{\operatorname{csch}(x)^3} + \frac{x\sqrt{\operatorname{csch}(x)}}{3} \right) dx$$

Problem 29: Result more than twice size of optimal antiderivative.

$$\int \frac{a + I a \sinh(fx + e)}{(dx + c)^3} dx$$

Optimal (type 4, 119 leaves, 7 steps):

$$-\frac{a}{2d(dx+c)^2} - \frac{Iaf \cosh(fx+e)}{2d^2(dx+c)} + \frac{Iaf^2 \cosh\left(-e + \frac{cf}{d}\right) \operatorname{Shi}\left(\frac{cf}{d} + fx\right)}{2d^3} - \frac{Iaf^2 \operatorname{Chi}\left(\frac{cf}{d} + fx\right) \sinh\left(-e + \frac{cf}{d}\right)}{2d^3} - \frac{Ia \sinh(fx+e)}{2d(dx+c)^2}$$

Result (type 4, 302 leaves):

$$-\frac{a}{2d(dx+c)^2} - \frac{Iaf^3 e^{-fx-e} x}{4d(d^2 f^2 x^2 + 2cdf^2 x + c^2 f^2)} - \frac{Iaf^3 e^{-fx-e} c}{4d^2(d^2 f^2 x^2 + 2cdf^2 x + c^2 f^2)} + \frac{Iaf^2 e^{-fx-e}}{4d(d^2 f^2 x^2 + 2cdf^2 x + c^2 f^2)} + \frac{Iaf^2 e^{\frac{cf-de}{d}} \operatorname{Ei}_1\left(fx+e + \frac{cf-de}{d}\right)}{4d^3} - \frac{Iaf^2 e^{fx+e}}{4d^3 \left(\frac{cf}{d} + fx\right)^2} - \frac{Iaf^2 e^{fx+e}}{4d^3 \left(\frac{cf}{d} + fx\right)} - \frac{Iaf^2 e^{-\frac{cf-de}{d}} \operatorname{Ei}_1\left(-fx-e - \frac{cf-de}{d}\right)}{4d^3}$$

Problem 30: Result more than twice size of optimal antiderivative.

$$\int (dx + c)^3 (a + I a \sinh(fx + e))^2 dx$$

Optimal (type 3, 227 leaves, 10 steps):

$$\frac{3a^2 c d^2 x}{4f^2} + \frac{3a^2 d^3 x^2}{8f^2} + \frac{3a^2 (dx+c)^4}{8d} + \frac{12Ia^2 d^2 (dx+c) \cosh(fx+e)}{f^3} + \frac{2Ia^2 (dx+c)^3 \cosh(fx+e)}{f} - \frac{12Ia^2 d^3 \sinh(fx+e)}{f^4} - \frac{6Ia^2 d (dx+c)^2 \sinh(fx+e)}{f^2} - \frac{3a^2 d^2 (dx+c) \cosh(fx+e) \sinh(fx+e)}{4f^3} - \frac{a^2 (dx+c)^3 \cosh(fx+e) \sinh(fx+e)}{2f} + \frac{3a^2 d^3 \sinh(fx+e)^2}{8f^4} + \frac{3a^2 d (dx+c)^2 \sinh(fx+e)^2}{4f^2}$$

Result (type 3, 1081 leaves):

$$\frac{1}{f} \left( \frac{6Ic d^2 e^2 a^2 \cosh(fx+e)}{f^2} - \frac{6Ic^2 d e a^2 \cosh(fx+e)}{f} - \frac{12Ic d^2 e a^2 ((fx+e) \cosh(fx+e) - \sinh(fx+e))}{f^2} + \frac{c d^2 a^2 (fx+e)^3}{f^2} - \frac{d^3 e^3 a^2 (fx+e)}{f^3} - \frac{3d^3 e^2 a^2 \left( \frac{(fx+e) \cosh(fx+e) \sinh(fx+e)}{2} - \frac{(fx+e)^2}{4} - \frac{\cosh(fx+e)^2}{4} \right)}{f^3} \right)$$

$$\begin{aligned}
& - \frac{3 c d^2 a^2 \left( \frac{(f x + e)^2 \cosh(f x + e) \sinh(f x + e)}{2} - \frac{(f x + e)^3}{6} - \frac{(f x + e) \cosh(f x + e)^2}{2} + \frac{\cosh(f x + e) \sinh(f x + e)}{4} + \frac{f x}{4} + \frac{e}{4} \right)}{f^2} \\
& - \frac{3 c^2 d a^2 \left( \frac{(f x + e) \cosh(f x + e) \sinh(f x + e)}{2} - \frac{(f x + e)^2}{4} - \frac{\cosh(f x + e)^2}{4} \right)}{f} + \frac{d^3 e^3 a^2 \left( \frac{\cosh(f x + e) \sinh(f x + e)}{2} - \frac{f x}{2} - \frac{e}{2} \right)}{f^3} \\
& + \frac{2 I d^3 a^2 \left( (f x + e)^3 \cosh(f x + e) - 3 (f x + e)^2 \sinh(f x + e) + 6 (f x + e) \cosh(f x + e) - 6 \sinh(f x + e) \right)}{f^3} \\
& + \frac{3 d^3 e a^2 \left( \frac{(f x + e)^2 \cosh(f x + e) \sinh(f x + e)}{2} - \frac{(f x + e)^3}{6} - \frac{(f x + e) \cosh(f x + e)^2}{2} + \frac{\cosh(f x + e) \sinh(f x + e)}{4} + \frac{f x}{4} + \frac{e}{4} \right)}{f^3} \\
& + \frac{3 c^2 d a^2 (f x + e)^2}{2 f} - \frac{d^3 e a^2 (f x + e)^3}{f^3} + \frac{3 d^3 e^2 a^2 (f x + e)^2}{2 f^3} + \frac{6 c d^2 e a^2 \left( \frac{(f x + e) \cosh(f x + e) \sinh(f x + e)}{2} - \frac{(f x + e)^2}{4} - \frac{\cosh(f x + e)^2}{4} \right)}{f^2} \\
& - \frac{6 I d^3 e a^2 \left( (f x + e)^2 \cosh(f x + e) - 2 (f x + e) \sinh(f x + e) + 2 \cosh(f x + e) \right)}{f^3} + \frac{6 I d^3 e^2 a^2 \left( (f x + e) \cosh(f x + e) - \sinh(f x + e) \right)}{f^3} \\
& + \frac{6 I c d^2 a^2 \left( (f x + e)^2 \cosh(f x + e) - 2 (f x + e) \sinh(f x + e) + 2 \cosh(f x + e) \right)}{f^2} + \frac{6 I c^2 d a^2 \left( (f x + e) \cosh(f x + e) - \sinh(f x + e) \right)}{f} \\
& + \frac{3 c d^2 e^2 a^2 (f x + e)}{f^2} - \frac{3 c^2 d e a^2 (f x + e)}{f} - \frac{3 c d^2 e a^2 (f x + e)^2}{f^2} - \frac{3 c d^2 e^2 a^2 \left( \frac{\cosh(f x + e) \sinh(f x + e)}{2} - \frac{f x}{2} - \frac{e}{2} \right)}{f^2} \\
& + \frac{3 c^2 d e a^2 \left( \frac{\cosh(f x + e) \sinh(f x + e)}{2} - \frac{f x}{2} - \frac{e}{2} \right)}{f} - \frac{2 I d^3 e^3 a^2 \cosh(f x + e)}{f^3} - c^3 a^2 \left( \frac{\cosh(f x + e) \sinh(f x + e)}{2} - \frac{f x}{2} - \frac{e}{2} \right) + c^3 a^2 (f x + e) \\
& - \frac{1}{f^3} \left( d^3 a^2 \left( \frac{(f x + e)^3 \cosh(f x + e) \sinh(f x + e)}{2} - \frac{(f x + e)^4}{8} - \frac{3 (f x + e)^2 \cosh(f x + e)^2}{4} + \frac{3 (f x + e) \cosh(f x + e) \sinh(f x + e)}{4} \right. \right. \\
& \left. \left. + \frac{3 (f x + e)^2}{8} - \frac{3 \cosh(f x + e)^2}{8} \right) \right) + \frac{d^3 a^2 (f x + e)^4}{4 f^3} + 2 I c^3 a^2 \cosh(f x + e)
\end{aligned}$$

Problem 31: Result more than twice size of optimal antiderivative.

$$\int \frac{(d x + c)^3}{(a + I a \sinh(f x + e))^2} dx$$

Optimal(type 4, 249 leaves, 10 steps):

$$\begin{aligned} & \frac{(dx+c)^3}{3a^2f} - \frac{2d(dx+c)^2 \ln(1+Ie^{fx+e})}{a^2f^2} + \frac{4d^3 \ln\left(\cosh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)\right)}{a^2f^4} - \frac{4d^2(dx+c) \operatorname{polylog}(2, -Ie^{fx+e})}{a^2f^3} + \frac{4d^3 \operatorname{polylog}(3, -Ie^{fx+e})}{a^2f^4} \\ & + \frac{d(dx+c)^2 \operatorname{sech}\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)^2}{2a^2f^2} - \frac{2d^2(dx+c) \tanh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)}{a^2f^3} + \frac{(dx+c)^3 \tanh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)}{3a^2f} \\ & + \frac{(dx+c)^3 \operatorname{sech}\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)^2 \tanh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)}{6a^2f} \end{aligned}$$

Result(type 4, 722 leaves):

$$\begin{aligned} & \frac{1}{3(e^{fx+e}-1)^3 f^3 a^2} (2(-I f^2 d^3 x^3 - 6I c d^2 e^{2fx+2e} - 3f d^3 x^2 e^{fx+e} - 3f c^2 d e^{fx+e} + 3f^2 d^3 x^3 e^{fx+e} - 6I f c d^2 x e^{2fx+2e} + 6I d^3 x - 6I d^3 x e^{2fx+2e} \\ & - 12d^3 x e^{fx+e} - 12c d^2 e^{fx+e} + 3f^2 c^3 e^{fx+e} - 3I f d^3 x^2 e^{2fx+2e} + 9f^2 c d^2 x^2 e^{fx+e} + 9f^2 c^2 d x e^{fx+e} - 3I f^2 c d^2 x^2 - 3I f c^2 d e^{2fx+2e} - I f^2 c^3 \\ & - 3I f^2 c^2 d x - 6f c d^2 x e^{fx+e} + 6I c d^2)) - \frac{2d^3 e^2 x}{f^3 a^2} + \frac{2d^2 c x^2}{f a^2} + \frac{2d^2 c e^2}{f^3 a^2} - \frac{2d^3 \ln(1+Ie^{fx+e}) x^2}{f^2 a^2} - \frac{4d^3 \operatorname{polylog}(2, -Ie^{fx+e}) x}{f^3 a^2} \\ & - \frac{4d^2 c \operatorname{polylog}(2, -Ie^{fx+e})}{f^3 a^2} + \frac{4d^2 c e x}{f^2 a^2} - \frac{4d^2 \ln(1+Ie^{fx+e}) c x}{f^2 a^2} - \frac{4d^2 \ln(1+Ie^{fx+e}) c e}{f^3 a^2} - \frac{4d^2 \ln(e^{fx+e}) c e}{f^3 a^2} + \frac{4d^2 \ln(e^{fx+e}-1) c e}{f^3 a^2} \\ & + \frac{2d^3 \ln(1+Ie^{fx+e}) e^2}{f^4 a^2} + \frac{2d^3 x^3}{3f a^2} + \frac{2d \ln(e^{fx+e}) c^2}{f^2 a^2} - \frac{2d^3 \ln(e^{fx+e}-1) e^2}{f^4 a^2} - \frac{2d \ln(e^{fx+e}-1) c^2}{f^2 a^2} + \frac{2d^3 \ln(e^{fx+e}) e^2}{f^4 a^2} - \frac{4d^3 e^3}{3f^4 a^2} \\ & + \frac{4d^3 \operatorname{polylog}(3, -Ie^{fx+e})}{a^2 f^4} + \frac{4d^3 \ln(e^{fx+e}-1)}{f^4 a^2} - \frac{4d^3 \ln(e^{fx+e})}{f^4 a^2} \end{aligned}$$

Problem 36: Unable to integrate problem.

$$\int \frac{\sqrt{a + I a \sinh(fx + e)}}{x} dx$$

Optimal(type 4, 85 leaves, 4 steps):

$$\sinh\left(\frac{e}{2} + \frac{I\pi}{4}\right) \operatorname{sech}\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right) \operatorname{Shi}\left(\frac{fx}{2}\right) \sqrt{a + I a \sinh(fx + e)} + \operatorname{Chi}\left(\frac{fx}{2}\right) \operatorname{sech}\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right) \cosh\left(\frac{e}{2} + \frac{I\pi}{4}\right) \sqrt{a + I a \sinh(fx + e)}$$

Result(type 8, 20 leaves):

$$\int \frac{\sqrt{a + I a \sinh(fx + e)}}{x} dx$$

Problem 37: Unable to integrate problem.

$$\int \frac{\sqrt{a + I a \sinh(fx + e)}}{x^3} dx$$

Optimal(type 4, 145 leaves, 6 steps):

$$\begin{aligned} & -\frac{\sqrt{a + I a \sinh(fx + e)}}{2x^2} + \frac{f^2 \sinh\left(\frac{e}{2} + \frac{I\pi}{4}\right) \operatorname{sech}\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right) \operatorname{Shi}\left(\frac{fx}{2}\right) \sqrt{a + I a \sinh(fx + e)}}{8} \\ & + \frac{f^2 \operatorname{Chi}\left(\frac{fx}{2}\right) \operatorname{sech}\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right) \cosh\left(\frac{e}{2} + \frac{I\pi}{4}\right) \sqrt{a + I a \sinh(fx + e)}}{8} - \frac{f \sqrt{a + I a \sinh(fx + e)} \tanh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)}{4x} \end{aligned}$$

Result(type 8, 20 leaves):

$$\int \frac{\sqrt{a + I a \sinh(fx + e)}}{x^3} dx$$

Problem 38: Unable to integrate problem.

$$\int x^2 (a + I a \sinh(fx + e))^{3/2} dx$$

Optimal(type 3, 224 leaves, 7 steps):

$$\begin{aligned} & -\frac{32ax\sqrt{a + I a \sinh(fx + e)}}{3f^2} - \frac{16ax \cosh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)^2 \sqrt{a + I a \sinh(fx + e)}}{9f^2} \\ & + \frac{4ax^2 \cosh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right) \sinh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right) \sqrt{a + I a \sinh(fx + e)}}{3f} + \frac{224a\sqrt{a + I a \sinh(fx + e)} \tanh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)}{9f^3} \\ & + \frac{8ax^2 \sqrt{a + I a \sinh(fx + e)} \tanh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)}{3f} + \frac{32a \sinh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)^2 \sqrt{a + I a \sinh(fx + e)} \tanh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)}{27f^3} \end{aligned}$$

Result(type 8, 20 leaves):

$$\int x^2 (a + I a \sinh(fx + e))^{3/2} dx$$

Problem 39: Unable to integrate problem.

$$\int x^2 (a + I a \sinh(dx + c))^{5/2} dx$$

Optimal(type 3, 377 leaves, 10 steps):

$$\begin{aligned} & -\frac{256a^2x\sqrt{a + I a \sinh(dx + c)}}{15d^2} - \frac{128a^2x \cosh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)^2 \sqrt{a + I a \sinh(dx + c)}}{45d^2} - \frac{32a^2x \cosh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)^4 \sqrt{a + I a \sinh(dx + c)}}{25d^2} \end{aligned}$$



$$\begin{aligned}
& + \frac{32 a^2 x^2 \cosh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \sinh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \sqrt{a + I a \sinh(dx + c)}}{15 d} \\
& + \frac{8 a^2 x^2 \cosh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)^3 \sinh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \sqrt{a + I a \sinh(dx + c)}}{5 d} + \frac{9536 a^2 \sqrt{a + I a \sinh(dx + c)} \tanh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)}{225 d^3} \\
& + \frac{64 a^2 x^2 \sqrt{a + I a \sinh(dx + c)} \tanh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)}{15 d} + \frac{2432 a^2 \sinh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)^2 \sqrt{a + I a \sinh(dx + c)} \tanh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)}{675 d^3} \\
& + \frac{64 a^2 \sinh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)^4 \sqrt{a + I a \sinh(dx + c)} \tanh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)}{125 d^3}
\end{aligned}$$

Result(type 8, 20 leaves):

$$\int x^2 (a + I a \sinh(dx + c))^{5/2} dx$$

Problem 40: Unable to integrate problem.

$$\int \frac{(a + I a \sinh(dx + c))^{5/2}}{x} dx$$

Optimal(type 4, 279 leaves, 12 steps):

$$\begin{aligned}
& \frac{5 a^2 \sinh\left(\frac{c}{2} + \frac{I\pi}{4}\right) \operatorname{sech}\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \operatorname{Shi}\left(\frac{dx}{2}\right) \sqrt{a + I a \sinh(dx + c)}}{2} \\
& + \frac{5 I a^2 \cosh\left(\frac{3c}{2} + \frac{I\pi}{4}\right) \operatorname{sech}\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \operatorname{Shi}\left(\frac{3dx}{2}\right) \sqrt{a + I a \sinh(dx + c)}}{4} \\
& - \frac{a^2 \sinh\left(\frac{5c}{2} + \frac{I\pi}{4}\right) \operatorname{sech}\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \operatorname{Shi}\left(\frac{5dx}{2}\right) \sqrt{a + I a \sinh(dx + c)}}{4} \\
& - \frac{a^2 \operatorname{Chi}\left(\frac{5dx}{2}\right) \operatorname{sech}\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \cosh\left(\frac{5c}{2} + \frac{I\pi}{4}\right) \sqrt{a + I a \sinh(dx + c)}}{4} \\
& + \frac{5 a^2 \operatorname{Chi}\left(\frac{dx}{2}\right) \operatorname{sech}\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \cosh\left(\frac{c}{2} + \frac{I\pi}{4}\right) \sqrt{a + I a \sinh(dx + c)}}{2} \\
& + \frac{5 I a^2 \operatorname{Chi}\left(\frac{3dx}{2}\right) \operatorname{sech}\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \sinh\left(\frac{3c}{2} + \frac{I\pi}{4}\right) \sqrt{a + I a \sinh(dx + c)}}{4}
\end{aligned}$$

Result(type 8, 20 leaves):

$$\int \frac{(a + I a \sinh(dx + c))^5 / 2}{x} dx$$

Problem 41: Unable to integrate problem.

$$\int \frac{x^2}{(a + I a \sinh(fx + e))^3 / 2} dx$$

Optimal(type 4, 374 leaves, 10 steps):

$$\begin{aligned} & \frac{2x}{a^2 \sqrt{a + I a \sinh(fx + e)}} - \frac{4 \arctan\left(\sinh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)\right) \cosh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)}{a^3 \sqrt{a + I a \sinh(fx + e)}} - \frac{I x^2 \operatorname{arctanh}\left(e^{\frac{e}{2} + \frac{3I\pi}{4} + \frac{fx}{2}}\right) \cosh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)}{a f \sqrt{a + I a \sinh(fx + e)}} \\ & + \frac{2 I x \cosh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right) \operatorname{polylog}\left(2, e^{\frac{e}{2} + \frac{3I\pi}{4} + \frac{fx}{2}}\right)}{a^2 \sqrt{a + I a \sinh(fx + e)}} - \frac{2 I x \cosh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right) \operatorname{polylog}\left(2, -e^{\frac{e}{2} + \frac{3I\pi}{4} + \frac{fx}{2}}\right)}{a^2 \sqrt{a + I a \sinh(fx + e)}} \\ & - \frac{4 I \cosh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right) \operatorname{polylog}\left(3, e^{\frac{e}{2} + \frac{3I\pi}{4} + \frac{fx}{2}}\right)}{a^3 \sqrt{a + I a \sinh(fx + e)}} + \frac{4 I \cosh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right) \operatorname{polylog}\left(3, -e^{\frac{e}{2} + \frac{3I\pi}{4} + \frac{fx}{2}}\right)}{a^3 \sqrt{a + I a \sinh(fx + e)}} + \frac{x^2 \tanh\left(\frac{e}{2} + \frac{I\pi}{4} + \frac{fx}{2}\right)}{2 a f \sqrt{a + I a \sinh(fx + e)}} \end{aligned}$$

Result(type 8, 20 leaves):

$$\int \frac{x^2}{(a + I a \sinh(fx + e))^3 / 2} dx$$

Problem 42: Unable to integrate problem.

$$\int \frac{x^2}{(a + I a \sinh(dx + c))^5 / 2} dx$$

Optimal(type 4, 500 leaves, 13 steps):

$$\begin{aligned} & \frac{3x}{4 a^2 d^2 \sqrt{a + I a \sinh(dx + c)}} - \frac{5 \arctan\left(\sinh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)\right) \cosh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)}{3 a^2 d^3 \sqrt{a + I a \sinh(dx + c)}} - \frac{3 I x^2 \operatorname{arctanh}\left(e^{\frac{c}{2} + \frac{3I\pi}{4} + \frac{dx}{2}}\right) \cosh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)}{8 a^2 d \sqrt{a + I a \sinh(dx + c)}} \\ & + \frac{3 I x \cosh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \operatorname{polylog}\left(2, e^{\frac{c}{2} + \frac{3I\pi}{4} + \frac{dx}{2}}\right)}{4 a^2 d^2 \sqrt{a + I a \sinh(dx + c)}} - \frac{3 I x \cosh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right) \operatorname{polylog}\left(2, -e^{\frac{c}{2} + \frac{3I\pi}{4} + \frac{dx}{2}}\right)}{4 a^2 d^2 \sqrt{a + I a \sinh(dx + c)}} \end{aligned}$$

$$\begin{aligned}
& - \frac{3 \operatorname{Icosh}\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right) \operatorname{polylog}\left(3, e^{\frac{c}{2} + \frac{3\operatorname{I}\pi}{4} + \frac{dx}{2}}\right)}{2 a^2 d^3 \sqrt{a + \operatorname{I}a \sinh(dx + c)}} + \frac{3 \operatorname{Icosh}\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right) \operatorname{polylog}\left(3, -e^{\frac{c}{2} + \frac{3\operatorname{I}\pi}{4} + \frac{dx}{2}}\right)}{2 a^2 d^3 \sqrt{a + \operatorname{I}a \sinh(dx + c)}} + \frac{x \operatorname{sech}\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right)^2}{6 a^2 d^2 \sqrt{a + \operatorname{I}a \sinh(dx + c)}} \\
& - \frac{\tanh\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right)}{6 a^2 d^3 \sqrt{a + \operatorname{I}a \sinh(dx + c)}} + \frac{3 x^2 \tanh\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right)}{16 a^2 d \sqrt{a + \operatorname{I}a \sinh(dx + c)}} + \frac{x^2 \operatorname{sech}\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right)^2 \tanh\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right)}{8 a^2 d \sqrt{a + \operatorname{I}a \sinh(dx + c)}}
\end{aligned}$$

Result(type 8, 20 leaves):

$$\int \frac{x^2}{(a + \operatorname{I}a \sinh(dx + c))^5 / 2} dx$$

Problem 43: Unable to integrate problem.

$$\int \frac{x}{(a + \operatorname{I}a \sinh(dx + c))^5 / 2} dx$$

Optimal(type 4, 302 leaves, 8 steps):

$$\begin{aligned}
& \frac{3}{8 a^2 d^2 \sqrt{a + \operatorname{I}a \sinh(dx + c)}} - \frac{3 \operatorname{I}x \operatorname{arctanh}\left(e^{\frac{c}{2} + \frac{3\operatorname{I}\pi}{4} + \frac{dx}{2}}\right) \cosh\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right)}{8 a^2 d \sqrt{a + \operatorname{I}a \sinh(dx + c)}} + \frac{3 \operatorname{Icosh}\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right) \operatorname{polylog}\left(2, e^{\frac{c}{2} + \frac{3\operatorname{I}\pi}{4} + \frac{dx}{2}}\right)}{8 a^2 d^2 \sqrt{a + \operatorname{I}a \sinh(dx + c)}} \\
& - \frac{3 \operatorname{Icosh}\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right) \operatorname{polylog}\left(2, -e^{\frac{c}{2} + \frac{3\operatorname{I}\pi}{4} + \frac{dx}{2}}\right)}{8 a^2 d^2 \sqrt{a + \operatorname{I}a \sinh(dx + c)}} + \frac{\operatorname{sech}\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right)^2}{12 a^2 d^2 \sqrt{a + \operatorname{I}a \sinh(dx + c)}} + \frac{3 x \tanh\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right)}{16 a^2 d \sqrt{a + \operatorname{I}a \sinh(dx + c)}} \\
& + \frac{x \operatorname{sech}\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right)^2 \tanh\left(\frac{c}{2} + \frac{\operatorname{I}\pi}{4} + \frac{dx}{2}\right)}{8 a^2 d \sqrt{a + \operatorname{I}a \sinh(dx + c)}}
\end{aligned}$$

Result(type 8, 18 leaves):

$$\int \frac{x}{(a + \operatorname{I}a \sinh(dx + c))^5 / 2} dx$$

Problem 44: Unable to integrate problem.

$$\int (dx + c)^m (a + \operatorname{I}a \sinh(dx + c))^3 dx$$

Optimal(type 4, 390 leaves, 12 steps):

$$\begin{aligned}
& \frac{5a^3(dx+c)^{1+m}}{2d(1+m)} - \frac{13^{-1-m}a^3e^{3e-\frac{3cf}{d}}(dx+c)^m\Gamma\left(1+m, -\frac{3f(dx+c)}{d}\right)}{8f\left(-\frac{f(dx+c)}{d}\right)^m} - \frac{32^{-3-m}a^3e^{2e-\frac{2cf}{d}}(dx+c)^m\Gamma\left(1+m, -\frac{2f(dx+c)}{d}\right)}{f\left(-\frac{f(dx+c)}{d}\right)^m} \\
& + \frac{151a^3e^{-\frac{cf}{d}}(dx+c)^m\Gamma\left(1+m, -\frac{f(dx+c)}{d}\right)}{8f\left(-\frac{f(dx+c)}{d}\right)^m} + \frac{151a^3e^{-e+\frac{cf}{d}}(dx+c)^m\Gamma\left(1+m, \frac{f(dx+c)}{d}\right)}{8f\left(\frac{f(dx+c)}{d}\right)^m} \\
& + \frac{32^{-3-m}a^3e^{-2e+\frac{2cf}{d}}(dx+c)^m\Gamma\left(1+m, \frac{2f(dx+c)}{d}\right)}{f\left(\frac{f(dx+c)}{d}\right)^m} - \frac{13^{-1-m}a^3e^{-3e+\frac{3cf}{d}}(dx+c)^m\Gamma\left(1+m, \frac{3f(dx+c)}{d}\right)}{8f\left(\frac{f(dx+c)}{d}\right)^m}
\end{aligned}$$

Result(type 8, 24 leaves):

$$\int (dx+c)^m (a+Ia \sinh(fx+e))^3 dx$$

Problem 49: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx+e)^2 \sinh(dx+c)}{a+Ia \sinh(dx+c)} dx$$

Optimal(type 4, 112 leaves, 8 steps):

$$\frac{I(fx+e)^2}{ad} - \frac{I(fx+e)^3}{3af} - \frac{4If(fx+e) \ln(1+Ie^{dx+c})}{ad^2} - \frac{4If^2 \operatorname{polylog}(2, -Ie^{dx+c})}{ad^3} + \frac{I(fx+e)^2 \tanh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)}{ad}$$

Result(type 4, 268 leaves):

$$\begin{aligned}
& -\frac{Ix^3f^2}{3a} - \frac{Iefx^2}{a} - \frac{Ie^2x}{a} - \frac{2(x^2f^2+2efx+e^2)}{da(e^{dx+c}-1)} + \frac{4I \ln(e^{dx+c})ef}{ad^2} - \frac{4I \ln(e^{dx+c}-1)ef}{ad^2} + \frac{2If^2x^2}{ad} + \frac{4If^2cx}{ad^2} + \frac{2If^2c^2}{ad^3} - \frac{4If^2 \ln(1+Ie^{dx+c})x}{ad^2} \\
& - \frac{4If^2 \ln(1+Ie^{dx+c})c}{ad^3} - \frac{4If^2 \operatorname{polylog}(2, -Ie^{dx+c})}{ad^3} - \frac{4If^2c \ln(e^{dx+c})}{ad^3} + \frac{4If^2c \ln(e^{dx+c}-1)}{ad^3}
\end{aligned}$$

Problem 53: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx+e)^3 \operatorname{csch}(dx+c)}{a+Ia \sinh(dx+c)} dx$$

Optimal(type 4, 288 leaves, 17 steps):

$$-\frac{I(fx+e)^3}{ad} - \frac{2(fx+e)^3 \operatorname{arctanh}(e^{dx+c})}{ad} + \frac{6If(fx+e)^2 \ln(1+Ie^{dx+c})}{ad^2} - \frac{3f(fx+e)^2 \operatorname{polylog}(2, -e^{dx+c})}{ad^2} + \frac{12If^2(fx+e) \operatorname{polylog}(2, -Ie^{dx+c})}{ad^3}$$

$$\begin{aligned}
& + \frac{3f(fx+e)^2 \operatorname{polylog}(2, e^{dx+c})}{a^2} + \frac{6f^2(fx+e) \operatorname{polylog}(3, -e^{dx+c})}{a^3} - \frac{12If^3 \operatorname{polylog}(3, -Ie^{dx+c})}{a^4} - \frac{6f^2(fx+e) \operatorname{polylog}(3, e^{dx+c})}{a^3} \\
& - \frac{6f^3 \operatorname{polylog}(4, -e^{dx+c})}{a^4} + \frac{6f^3 \operatorname{polylog}(4, e^{dx+c})}{a^4} - \frac{I(fx+e)^3 \tanh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)}{ad}
\end{aligned}$$

Result(type 4, 1033 leaves):

$$\begin{aligned}
& - \frac{e^3 \ln(1+e^{dx+c})}{ad} + \frac{e^3 \ln(e^{dx+c}-1)}{ad} + \frac{6ef^2 \operatorname{polylog}(3, -e^{dx+c})}{a^3} - \frac{f^3 c^3 \ln(e^{dx+c}-1)}{a^4} - \frac{3e^2 f \operatorname{polylog}(2, -e^{dx+c})}{a^2} + \frac{3e^2 f \operatorname{polylog}(2, e^{dx+c})}{a^2} \\
& + \frac{4If^3 c^3}{a^4} - \frac{2If^3 x^3}{ad} - \frac{6ef^2 \operatorname{polylog}(3, e^{dx+c})}{a^3} + \frac{f^3 c^3 \ln(1-e^{dx+c})}{a^4} - \frac{f^3 \ln(1+e^{dx+c}) x^3}{ad} - \frac{3f^3 \operatorname{polylog}(2, -e^{dx+c}) x^2}{a^2} \\
& + \frac{6f^3 \operatorname{polylog}(3, -e^{dx+c}) x}{a^3} + \frac{f^3 \ln(1-e^{dx+c}) x^3}{ad} + \frac{3f^3 \operatorname{polylog}(2, e^{dx+c}) x^2}{a^2} - \frac{6f^3 \operatorname{polylog}(3, e^{dx+c}) x}{a^3} + \frac{12Ief^2 \ln(1+Ie^{dx+c}) x}{a^2} \\
& + \frac{12Ief^2 \ln(1+Ie^{dx+c}) c}{a^3} - \frac{12Ief^2 cx}{a^2} - \frac{12Ief^2 c \ln(e^{dx+c}-1)}{a^3} + \frac{12Ief^2 c \ln(e^{dx+c})}{a^3} - \frac{12If^3 \operatorname{polylog}(3, -Ie^{dx+c})}{a^4} - \frac{6f^3 \operatorname{polylog}(4, -e^{dx+c})}{a^4} \\
& + \frac{6f^3 \operatorname{polylog}(4, e^{dx+c})}{a^4} + \frac{3ef^2 c^2 \ln(e^{dx+c}-1)}{a^3} - \frac{3cf^2 \ln(e^{dx+c}-1)}{a^2} + \frac{6If^3 \ln(1+Ie^{dx+c}) x^2}{a^2} - \frac{6If^3 \ln(1+Ie^{dx+c}) c^2}{a^4} \\
& + \frac{12If^3 \operatorname{polylog}(2, -Ie^{dx+c}) x}{a^3} + \frac{6If^3 c^2 x}{a^3} - \frac{6Ief^2 x^2}{ad} - \frac{6Ief^2 c^2}{a^3} + \frac{12Ief^2 \operatorname{polylog}(2, -Ie^{dx+c})}{a^3} - \frac{6If^3 c^2 \ln(e^{dx+c})}{a^4} + \frac{6If^3 c^2 \ln(e^{dx+c}-1)}{a^4} \\
& - \frac{6Ie^2 f \ln(e^{dx+c})}{a^2} + \frac{6Ie^2 f \ln(e^{dx+c}-1)}{a^2} + \frac{3 \ln(1-e^{dx+c}) c^2 f}{a^2} + \frac{3 \ln(1-e^{dx+c}) e^2 fx}{ad} - \frac{3 \ln(1+e^{dx+c}) e^2 fx}{ad} + \frac{6ef^2 \operatorname{polylog}(2, e^{dx+c}) x}{a^2} \\
& - \frac{3ef^2 \ln(1+e^{dx+c}) x^2}{ad} - \frac{6ef^2 \operatorname{polylog}(2, -e^{dx+c}) x}{a^2} + \frac{3ef^2 \ln(1-e^{dx+c}) x^2}{ad} - \frac{3ef^2 \ln(1-e^{dx+c}) c^2}{a^3} + \frac{2(x^3 f^3 + 3ef^2 x^2 + 3e^2 fx + e^3)}{da(e^{dx+c}-1)}
\end{aligned}$$

Problem 56: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx+e)^3 \operatorname{csch}(dx+c)^3}{a+Ia \sinh(dx+c)} dx$$

Optimal(type 4, 504 leaves, 40 steps):

$$\begin{aligned}
& \frac{I(fx+e)^3 \tanh\left(\frac{c}{2} + \frac{I\pi}{4} + \frac{dx}{2}\right)}{ad} - \frac{6f^2(fx+e) \operatorname{arctanh}(e^{dx+c})}{a^3} + \frac{3(fx+e)^3 \operatorname{arctanh}(e^{dx+c})}{ad} + \frac{I(fx+e)^3 \operatorname{coth}(dx+c)}{ad} \\
& - \frac{3f(fx+e)^2 \operatorname{csch}(dx+c)}{2a^2} - \frac{(fx+e)^3 \operatorname{coth}(dx+c) \operatorname{csch}(dx+c)}{2ad} - \frac{6If(fx+e)^2 \ln(1+Ie^{dx+c})}{a^2} + \frac{12If^3 \operatorname{polylog}(3, -Ie^{dx+c})}{a^4} \\
& - \frac{3f^3 \operatorname{polylog}(2, -e^{dx+c})}{a^4} + \frac{9f(fx+e)^2 \operatorname{polylog}(2, -e^{dx+c})}{2a^2} + \frac{2I(fx+e)^3}{ad} + \frac{3f^3 \operatorname{polylog}(2, e^{dx+c})}{a^4} - \frac{9f(fx+e)^2 \operatorname{polylog}(2, e^{dx+c})}{2a^2} \\
& - \frac{3If(fx+e)^2 \ln(1-e^{2dx+2c})}{a^2} - \frac{9f^2(fx+e) \operatorname{polylog}(3, -e^{dx+c})}{a^3} - \frac{12If^2(fx+e) \operatorname{polylog}(2, -Ie^{dx+c})}{a^3} + \frac{9f^2(fx+e) \operatorname{polylog}(3, e^{dx+c})}{a^3}
\end{aligned}$$

$$-\frac{3If^2(fx+e)\operatorname{polylog}(2, e^{2dx+2c})}{ad^3} + \frac{9f^3\operatorname{polylog}(4, -e^{dx+c})}{ad^4} - \frac{9f^3\operatorname{polylog}(4, e^{dx+c})}{ad^4} + \frac{3If^3\operatorname{polylog}(3, e^{2dx+2c})}{2ad^4}$$

Result(type ?, 2057 leaves): Display of huge result suppressed!

Problem 59: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx+e)\sinh(dx+c)}{a+b\sinh(dx+c)} dx$$

Optimal(type 4, 198 leaves, 10 steps):

$$\begin{aligned} & \frac{ex}{b} + \frac{fx^2}{2b} - \frac{a(fx+e)\ln\left(1 + \frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{bd\sqrt{a^2+b^2}} + \frac{a(fx+e)\ln\left(1 + \frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{bd\sqrt{a^2+b^2}} - \frac{af\operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{bd^2\sqrt{a^2+b^2}} \\ & + \frac{af\operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{bd^2\sqrt{a^2+b^2}} \end{aligned}$$

Result(type 4, 439 leaves):

$$\begin{aligned} & \frac{fx^2}{2b} + \frac{ex}{b} + \frac{2ae\operatorname{arctanh}\left(\frac{2e^{dx+c}b+2a}{2\sqrt{a^2+b^2}}\right)}{bd\sqrt{a^2+b^2}} - \frac{af\ln\left(\frac{-e^{dx+c}b+\sqrt{a^2+b^2}-a}{-a+\sqrt{a^2+b^2}}\right)x}{bd\sqrt{a^2+b^2}} - \frac{af\ln\left(\frac{-e^{dx+c}b+\sqrt{a^2+b^2}-a}{-a+\sqrt{a^2+b^2}}\right)c}{bd^2\sqrt{a^2+b^2}} \\ & + \frac{af\ln\left(\frac{e^{dx+c}b+\sqrt{a^2+b^2}+a}{a+\sqrt{a^2+b^2}}\right)x}{bd\sqrt{a^2+b^2}} + \frac{af\ln\left(\frac{e^{dx+c}b+\sqrt{a^2+b^2}+a}{a+\sqrt{a^2+b^2}}\right)c}{bd^2\sqrt{a^2+b^2}} - \frac{afdilog\left(\frac{-e^{dx+c}b+\sqrt{a^2+b^2}-a}{-a+\sqrt{a^2+b^2}}\right)}{bd^2\sqrt{a^2+b^2}} \\ & + \frac{afdilog\left(\frac{e^{dx+c}b+\sqrt{a^2+b^2}+a}{a+\sqrt{a^2+b^2}}\right)}{bd^2\sqrt{a^2+b^2}} - \frac{2ac\operatorname{farctanh}\left(\frac{2e^{dx+c}b+2a}{2\sqrt{a^2+b^2}}\right)}{bd^2\sqrt{a^2+b^2}} \end{aligned}$$

Problem 60: Unable to integrate problem.

$$\int \frac{(fx+e)^3\sinh(dx+c)^2}{a+b\sinh(dx+c)} dx$$

Optimal(type 4, 509 leaves, 19 steps):

$$-\frac{a(fx+e)^4}{4b^2f} + \frac{6f^2(fx+e)\cosh(dx+c)}{bd^3} + \frac{(fx+e)^3\cosh(dx+c)}{bd} - \frac{6f^3\sinh(dx+c)}{bd^4} - \frac{3f(fx+e)^2\sinh(dx+c)}{bd^2}$$

$$\begin{aligned}
& + \frac{a^2 (fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^2 d \sqrt{a^2 + b^2}} - \frac{a^2 (fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^2 d \sqrt{a^2 + b^2}} + \frac{3 a^2 f (fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^2 d^2 \sqrt{a^2 + b^2}} \\
& - \frac{3 a^2 f (fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^2 d^2 \sqrt{a^2 + b^2}} - \frac{6 a^2 f^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^2 d^3 \sqrt{a^2 + b^2}} + \frac{6 a^2 f^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^2 d^3 \sqrt{a^2 + b^2}} \\
& + \frac{6 a^2 f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^2 d^4 \sqrt{a^2 + b^2}} - \frac{6 a^2 f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^2 d^4 \sqrt{a^2 + b^2}}
\end{aligned}$$

Result (type 8, 314 leaves):

$$\begin{aligned}
& - \frac{a \left( \frac{1}{4} x^4 f^3 + e f^2 x^3 + \frac{3}{2} e^2 f x^2 + e^3 x \right)}{b^2} + \frac{(d^3 f^3 x^3 + 3 d^3 e f^2 x^2 + 3 d^3 e^2 f x - 3 d^2 f^3 x^2 + d^3 e^3 - 6 d^2 e f^2 x - 3 d^2 e^2 f + 6 d f^3 x + 6 d e f^2 - 6 f^3) e^{dx+c}}{2 b d^4} \\
& + \frac{d^3 f^3 x^3 + 3 d^3 e f^2 x^2 + 3 d^3 e^2 f x + 3 d^2 f^3 x^2 + d^3 e^3 + 6 d^2 e f^2 x + 3 d^2 e^2 f + 6 d f^3 x + 6 d e f^2 + 6 f^3}{2 b d^4 e^{dx+c}} + \int \frac{2 a^2 (x^3 f^3 + 3 e f^2 x^2 + 3 e^2 f x + e^3) e^{dx+c}}{b^2 (b (e^{dx+c})^2 + 2 a e^{dx+c} - b)} dx
\end{aligned}$$

Problem 61: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \sinh(dx + c)^2}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 242 leaves, 13 steps):

$$\begin{aligned}
& - \frac{a e x}{b^2} - \frac{a f x^2}{2 b^2} + \frac{(fx + e) \cosh(dx + c)}{b d} - \frac{f \sinh(dx + c)}{b d^2} + \frac{a^2 (fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^2 d \sqrt{a^2 + b^2}} - \frac{a^2 (fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^2 d \sqrt{a^2 + b^2}} \\
& + \frac{a^2 f \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^2 d^2 \sqrt{a^2 + b^2}} - \frac{a^2 f \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^2 d^2 \sqrt{a^2 + b^2}}
\end{aligned}$$

Result (type 4, 509 leaves):

$$\begin{aligned}
& - \frac{a f x^2}{2 b^2} - \frac{a e x}{b^2} + \frac{(d f x + d e - f) e^{dx+c}}{2 b d^2} + \frac{(d f x + d e + f) e^{-dx-c}}{2 b d^2} - \frac{2 a^2 e \operatorname{arctanh}\left(\frac{2 e^{dx+c} b + 2 a}{2 \sqrt{a^2 + b^2}}\right)}{b^2 d \sqrt{a^2 + b^2}} + \frac{a^2 f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right)}{b^2 d \sqrt{a^2 + b^2}} x
\end{aligned}$$

$$\begin{aligned}
& + \frac{a^2 f \ln \left( \frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}} \right) c}{b^2 d^2 \sqrt{a^2 + b^2}} - \frac{a^2 f \ln \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right) x}{b^2 d \sqrt{a^2 + b^2}} - \frac{a^2 f \ln \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right) c}{b^2 d^2 \sqrt{a^2 + b^2}} \\
& + \frac{a^2 f \operatorname{dilog} \left( \frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}} \right)}{b^2 d^2 \sqrt{a^2 + b^2}} - \frac{a^2 f \operatorname{dilog} \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right)}{b^2 d^2 \sqrt{a^2 + b^2}} + \frac{2 a^2 c f \operatorname{arctanh} \left( \frac{2 e^{dx+c} b + 2 a}{2 \sqrt{a^2 + b^2}} \right)}{b^2 d^2 \sqrt{a^2 + b^2}}
\end{aligned}$$

Problem 63: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \sinh(dx + c)^3}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 656 leaves, 24 steps):

$$\begin{aligned}
& - \frac{3 e f^2 x}{4 b d^2} - \frac{3 f^3 x^2}{8 b d^2} + \frac{a^2 (fx + e)^4}{4 b^3 f} - \frac{(fx + e)^4}{8 b f} - \frac{6 a f^2 (fx + e) \cosh(dx + c)}{b^2 d^3} - \frac{a (fx + e)^3 \cosh(dx + c)}{b^2 d} + \frac{6 a f^3 \sinh(dx + c)}{b^2 d^4} \\
& + \frac{3 a f (fx + e)^2 \sinh(dx + c)}{b^2 d^2} + \frac{3 f^2 (fx + e) \cosh(dx + c) \sinh(dx + c)}{4 b d^3} + \frac{(fx + e)^3 \cosh(dx + c) \sinh(dx + c)}{2 b d} - \frac{3 f^3 \sinh(dx + c)^2}{8 b d^4} \\
& - \frac{3 f (fx + e)^2 \sinh(dx + c)^2}{4 b d^2} - \frac{a^3 (fx + e)^3 \ln \left( 1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^3 d \sqrt{a^2 + b^2}} + \frac{a^3 (fx + e)^3 \ln \left( 1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^3 d \sqrt{a^2 + b^2}} \\
& - \frac{3 a^3 f (fx + e)^2 \operatorname{polylog} \left( 2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^3 d^2 \sqrt{a^2 + b^2}} + \frac{3 a^3 f (fx + e)^2 \operatorname{polylog} \left( 2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^3 d^2 \sqrt{a^2 + b^2}} + \frac{6 a^3 f^2 (fx + e) \operatorname{polylog} \left( 3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^3 d^3 \sqrt{a^2 + b^2}} \\
& - \frac{6 a^3 f^2 (fx + e) \operatorname{polylog} \left( 3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^3 d^3 \sqrt{a^2 + b^2}} - \frac{6 a^3 f^3 \operatorname{polylog} \left( 4, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^3 d^4 \sqrt{a^2 + b^2}} + \frac{6 a^3 f^3 \operatorname{polylog} \left( 4, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^3 d^4 \sqrt{a^2 + b^2}}
\end{aligned}$$

Result (type 8, 587 leaves):

$$\begin{aligned}
& \frac{\frac{1}{2} a^2 f^3 x^4 - \frac{1}{4} b^2 f^3 x^4 + 2 a^2 e f^2 x^3 - b^2 e f^2 x^3 + 3 a^2 e^2 f x^2 - \frac{3}{2} b^2 e^2 f x^2 + 2 a^2 e^3 x - b^2 e^3 x}{2 b^3} \\
& + \frac{(4 d^3 f^3 x^3 + 12 d^3 e f^2 x^2 + 12 d^3 e^2 f x - 6 d^2 f^3 x^2 + 4 d^3 e^3 - 12 d^2 e f^2 x - 6 d^2 e^2 f + 6 d f^3 x + 6 d e f^2 - 3 f^3) (e^{dx+c})^2}{32 b d^4} \\
& - \frac{a (d^3 f^3 x^3 + 3 d^3 e f^2 x^2 + 3 d^3 e^2 f x - 3 d^2 f^3 x^2 + d^3 e^3 - 6 d^2 e f^2 x - 3 d^2 e^2 f + 6 d f^3 x + 6 d e f^2 - 6 f^3) e^{dx+c}}{2 d^4 b^2}
\end{aligned}$$



$$\begin{aligned}
& - \frac{a (d^3 f^3 x^3 + 3 d^3 e f^2 x^2 + 3 d^3 e^2 f x + 3 d^2 f^3 x^2 + d^3 e^3 + 6 d^2 e f^2 x + 3 d^2 e^2 f + 6 d f^3 x + 6 d e f^2 + 6 f^3)}{2 d^4 b^2 e^{d x+c}} \\
& - \frac{4 d^3 f^3 x^3 + 12 d^3 e f^2 x^2 + 12 d^3 e^2 f x + 6 d^2 f^3 x^2 + 4 d^3 e^3 + 12 d^2 e f^2 x + 6 d^2 e^2 f + 6 d f^3 x + 6 d e f^2 + 3 f^3}{32 b d^4 (e^{d x+c})^2} + \int \\
& - \frac{2 a^3 (x^3 f^3 + 3 e f^2 x^2 + 3 e^2 f x + e^3) e^{d x+c}}{(b (e^{d x+c})^2 + 2 a e^{d x+c} - b) b^3} dx
\end{aligned}$$

Problem 64: Unable to integrate problem.

$$\int \frac{(f x + e)^3 \operatorname{csch}(d x + c)}{a + b \sinh(d x + c)} dx$$

Optimal(type 4, 558 leaves, 22 steps):

$$\begin{aligned}
& - \frac{2 (f x + e)^3 \operatorname{arctanh}(e^{d x+c})}{a d} - \frac{3 f (f x + e)^2 \operatorname{polylog}(2, -e^{d x+c})}{a d^2} + \frac{3 f (f x + e)^2 \operatorname{polylog}(2, e^{d x+c})}{a d^2} + \frac{6 f^2 (f x + e) \operatorname{polylog}(3, -e^{d x+c})}{a d^3} \\
& - \frac{6 f^2 (f x + e) \operatorname{polylog}(3, e^{d x+c})}{a d^3} - \frac{6 f^3 \operatorname{polylog}(4, -e^{d x+c})}{a d^4} + \frac{6 f^3 \operatorname{polylog}(4, e^{d x+c})}{a d^4} - \frac{b (f x + e)^3 \ln\left(1 + \frac{b e^{d x+c}}{a - \sqrt{a^2 + b^2}}\right)}{a d \sqrt{a^2 + b^2}} \\
& + \frac{b (f x + e)^3 \ln\left(1 + \frac{b e^{d x+c}}{a + \sqrt{a^2 + b^2}}\right)}{a d \sqrt{a^2 + b^2}} - \frac{3 b f (f x + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{d x+c}}{a - \sqrt{a^2 + b^2}}\right)}{a d^2 \sqrt{a^2 + b^2}} + \frac{3 b f (f x + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{d x+c}}{a + \sqrt{a^2 + b^2}}\right)}{a d^2 \sqrt{a^2 + b^2}} \\
& + \frac{6 b f^2 (f x + e) \operatorname{polylog}\left(3, -\frac{b e^{d x+c}}{a - \sqrt{a^2 + b^2}}\right)}{a d^3 \sqrt{a^2 + b^2}} - \frac{6 b f^2 (f x + e) \operatorname{polylog}\left(3, -\frac{b e^{d x+c}}{a + \sqrt{a^2 + b^2}}\right)}{a d^3 \sqrt{a^2 + b^2}} - \frac{6 b f^3 \operatorname{polylog}\left(4, -\frac{b e^{d x+c}}{a - \sqrt{a^2 + b^2}}\right)}{a d^4 \sqrt{a^2 + b^2}} \\
& + \frac{6 b f^3 \operatorname{polylog}\left(4, -\frac{b e^{d x+c}}{a + \sqrt{a^2 + b^2}}\right)}{a d^4 \sqrt{a^2 + b^2}}
\end{aligned}$$

Result(type 8, 28 leaves):

$$\int \frac{(f x + e)^3 \operatorname{csch}(d x + c)}{a + b \sinh(d x + c)} dx$$

Problem 65: Unable to integrate problem.

$$\int \frac{(f x + e)^2 \operatorname{csch}(d x + c)}{a + b \sinh(d x + c)} dx$$

Optimal(type 4, 398 leaves, 18 steps):

$$\begin{aligned}
& -\frac{2(fx+e)^2 \operatorname{arctanh}(e^{dx+c})}{ad} - \frac{2f(fx+e) \operatorname{polylog}(2, -e^{dx+c})}{ad^2} + \frac{2f(fx+e) \operatorname{polylog}(2, e^{dx+c})}{ad^2} + \frac{2f^2 \operatorname{polylog}(3, -e^{dx+c})}{ad^3} - \frac{2f^2 \operatorname{polylog}(3, e^{dx+c})}{ad^3} \\
& - \frac{b(fx+e)^2 \ln\left(1 + \frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{ad\sqrt{a^2+b^2}} + \frac{b(fx+e)^2 \ln\left(1 + \frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{ad\sqrt{a^2+b^2}} - \frac{2bf(fx+e) \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{ad^2\sqrt{a^2+b^2}} \\
& + \frac{2bf(fx+e) \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{ad^2\sqrt{a^2+b^2}} + \frac{2bf^2 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{ad^3\sqrt{a^2+b^2}} - \frac{2bf^2 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{ad^3\sqrt{a^2+b^2}}
\end{aligned}$$

Result(type 8, 28 leaves):

$$\int \frac{(fx+e)^2 \operatorname{csch}(dx+c)}{a+b \sinh(dx+c)} dx$$

Problem 67: Unable to integrate problem.

$$\int \frac{(fx+e)^3 \operatorname{csch}(dx+c)^2}{a+b \sinh(dx+c)} dx$$

Optimal(type 4, 696 leaves, 29 steps):

$$\begin{aligned}
& -\frac{(fx+e)^3}{ad} + \frac{2b(fx+e)^3 \operatorname{arctanh}(e^{dx+c})}{a^2d} - \frac{(fx+e)^3 \operatorname{coth}(dx+c)}{ad} + \frac{3f(fx+e)^2 \ln(1 - e^{2dx+2c})}{ad^2} + \frac{3bf(fx+e)^2 \operatorname{polylog}(2, -e^{dx+c})}{a^2d^2} \\
& - \frac{3bf(fx+e)^2 \operatorname{polylog}(2, e^{dx+c})}{a^2d^2} + \frac{3f^2(fx+e) \operatorname{polylog}(2, e^{2dx+2c})}{ad^3} - \frac{6bf^2(fx+e) \operatorname{polylog}(3, -e^{dx+c})}{a^2d^3} + \frac{6bf^2(fx+e) \operatorname{polylog}(3, e^{dx+c})}{a^2d^3} \\
& - \frac{3f^3 \operatorname{polylog}(3, e^{2dx+2c})}{2ad^4} + \frac{6bf^3 \operatorname{polylog}(4, -e^{dx+c})}{a^2d^4} - \frac{6bf^3 \operatorname{polylog}(4, e^{dx+c})}{a^2d^4} + \frac{b^2(fx+e)^3 \ln\left(1 + \frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{a^2d\sqrt{a^2+b^2}} \\
& - \frac{b^2(fx+e)^3 \ln\left(1 + \frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{a^2d\sqrt{a^2+b^2}} + \frac{3b^2f(fx+e)^2 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{a^2d^2\sqrt{a^2+b^2}} - \frac{3b^2f(fx+e)^2 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{a^2d^2\sqrt{a^2+b^2}} \\
& - \frac{6b^2f^2(fx+e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{a^2d^3\sqrt{a^2+b^2}} + \frac{6b^2f^2(fx+e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{a^2d^3\sqrt{a^2+b^2}} + \frac{6b^2f^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{a^2d^4\sqrt{a^2+b^2}} \\
& - \frac{6b^2f^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{a^2d^4\sqrt{a^2+b^2}}
\end{aligned}$$

Result(type 8, 281 leaves):

$$\begin{aligned} & -\frac{2(x^3 f^3 + 3ef^2 x^2 + 3e^2 f x + e^3)}{da((e^{dx+c})^2 - 1)} + 4 \left( \int \frac{1}{2ad((e^{dx+c})^2 - 1)(b(e^{dx+c})^2 + 2ae^{dx+c} - b)} \right. \\ & \quad \left. (-2bd f^3 x^3 (e^{dx+c})^2 - 6bde f^2 x^2 (e^{dx+c})^2 - 6bd e^2 f x (e^{dx+c})^2 + 3bf^3 x^2 (e^{dx+c})^2 + 6af^3 x^2 e^{dx+c} - 2bd e^3 (e^{dx+c})^2 + 6be f^2 x (e^{dx+c})^2 + 12ae f^2 x e^{dx+c} + 3be^2 f (e^{dx+c})^2 - 3bf^3 x^2 \right. \\ & \quad \left. + 6ae^2 f e^{dx+c} - 6be f^2 x - 3be^2 f) dx \right) \end{aligned}$$

Problem 69: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \operatorname{csch}(dx + c)^3}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 386 leaves, 24 steps):

$$\begin{aligned} & \frac{(fx + e) \operatorname{arctanh}(e^{dx+c})}{ad} - \frac{2b^2 (fx + e) \operatorname{arctanh}(e^{dx+c})}{a^3 d} + \frac{b (fx + e) \operatorname{coth}(dx + c)}{a^2 d} - \frac{f \operatorname{csch}(dx + c)}{2ad^2} - \frac{(fx + e) \operatorname{coth}(dx + c) \operatorname{csch}(dx + c)}{2ad} \\ & - \frac{bf \ln(\sinh(dx + c))}{a^2 d^2} + \frac{f \operatorname{polylog}(2, -e^{dx+c})}{2ad^2} - \frac{b^2 f \operatorname{polylog}(2, -e^{dx+c})}{a^3 d^2} - \frac{f \operatorname{polylog}(2, e^{dx+c})}{2ad^2} + \frac{b^2 f \operatorname{polylog}(2, e^{dx+c})}{a^3 d^2} \\ & - \frac{b^3 (fx + e) \ln\left(1 + \frac{be^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 d \sqrt{a^2 + b^2}} + \frac{b^3 (fx + e) \ln\left(1 + \frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 d \sqrt{a^2 + b^2}} - \frac{b^3 f \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 d^2 \sqrt{a^2 + b^2}} \\ & + \frac{b^3 f \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 d^2 \sqrt{a^2 + b^2}} \end{aligned}$$

Result(type 4, 860 leaves):

$$\begin{aligned} & \frac{adfx e^{3dx+3c} + ade e^{3dx+3c} - 2bdfx e^{2dx+2c} + adfx e^{dx+c} + e^{3dx+3c} af - 2bde e^{2dx+2c} + ade e^{dx+c} + 2bdfx - afe^{dx+c} + 2bde}{(e^{2dx+2c} - 1)^2 a^2 d^2} \\ & - \frac{b^2 e \ln(1 + e^{dx+c})}{a^3 d} - \frac{b^2 c f \ln(e^{dx+c} - 1)}{a^3 d^2} - \frac{b^3 f \operatorname{dilog}\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right)}{a^3 d^2 \sqrt{a^2 + b^2}} + \frac{b^3 f \operatorname{dilog}\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right)}{a^3 d^2 \sqrt{a^2 + b^2}} \\ & + \frac{b^2 e \ln(e^{dx+c} - 1)}{a^3 d} + \frac{\ln(1 + e^{dx+c}) fx}{2ad} - \frac{e \ln(e^{dx+c} - 1)}{2ad} + \frac{e \ln(1 + e^{dx+c})}{2ad} + \frac{c f \ln(e^{dx+c} - 1)}{2ad^2} - \frac{b^2 f \operatorname{dilog}(e^{dx+c})}{a^3 d^2} - \frac{b^2 f \operatorname{dilog}(1 + e^{dx+c})}{a^3 d^2} \\ & + \frac{2b^3 e \operatorname{arctanh}\left(\frac{2e^{dx+c} b + 2a}{2\sqrt{a^2 + b^2}}\right)}{a^3 d \sqrt{a^2 + b^2}} - \frac{2b^3 c f \operatorname{arctanh}\left(\frac{2e^{dx+c} b + 2a}{2\sqrt{a^2 + b^2}}\right)}{a^3 d^2 \sqrt{a^2 + b^2}} - \frac{b^3 f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) c}{a^3 d^2 \sqrt{a^2 + b^2}} \end{aligned}$$

$$\begin{aligned}
& + \frac{b^3 f \ln \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right) c}{a^3 d^2 \sqrt{a^2 + b^2}} - \frac{b^2 f \ln(1 + e^{dx+c}) x}{a^3 d} - \frac{b^3 f \ln \left( \frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}} \right) x}{a^3 d \sqrt{a^2 + b^2}} + \frac{b^3 f \ln \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right) x}{a^3 d \sqrt{a^2 + b^2}} \\
& + \frac{f \operatorname{dilog}(e^{dx+c})}{2 a d^2} + \frac{f \operatorname{dilog}(1 + e^{dx+c})}{2 a d^2} - \frac{b f \ln(e^{dx+c} - 1)}{a^2 d^2} - \frac{b f \ln(1 + e^{dx+c})}{a^2 d^2} + \frac{2 b f \ln(e^{dx+c})}{a^2 d^2}
\end{aligned}$$

Problem 71: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e)^3 \cosh(dx + c)^2}{a + I a \sinh(dx + c)} dx$$

Optimal (type 3, 102 leaves, 6 steps):

$$\frac{(fx + e)^4}{4 a f} - \frac{6 I f^2 (fx + e) \cosh(dx + c)}{a d^3} - \frac{I (fx + e)^3 \cosh(dx + c)}{a d} + \frac{6 I f^3 \sinh(dx + c)}{a d^4} + \frac{3 I f (fx + e)^2 \sinh(dx + c)}{a d^2}$$

Result (type 3, 447 leaves):

$$\begin{aligned}
& - \frac{1}{d^4 a} \left( -6 I e d c f^2 ((dx + c) \cosh(dx + c) - \sinh(dx + c)) + I f^3 ((dx + c)^3 \cosh(dx + c) - 3 (dx + c)^2 \sinh(dx + c) + 6 (dx + c) \cosh(dx + c) \right. \\
& \quad \left. - 6 \sinh(dx + c)) - 3 I c f^3 ((dx + c)^2 \cosh(dx + c) - 2 (dx + c) \sinh(dx + c) + 2 \cosh(dx + c)) - 3 I e^2 d^2 c f \cosh(dx + c) + I d^3 e^3 \cosh(dx + c) \right. \\
& \quad \left. + 3 I e d c^2 f^2 \cosh(dx + c) + 3 I e d f^2 ((dx + c)^2 \cosh(dx + c) - 2 (dx + c) \sinh(dx + c) + 2 \cosh(dx + c)) + 3 I e^2 d^2 f ((dx + c) \cosh(dx + c) \right. \\
& \quad \left. - \sinh(dx + c)) + 3 I c^2 f^3 ((dx + c) \cosh(dx + c) - \sinh(dx + c)) - I c^3 f^3 \cosh(dx + c) - \frac{f^3 (dx + c)^4}{4} + c f^3 (dx + c)^3 - d e f^2 (dx + c)^3 \right. \\
& \quad \left. - \frac{3 c^2 f^3 (dx + c)^2}{2} + 3 c d e f^2 (dx + c)^2 - \frac{3 d^2 e^2 f (dx + c)^2}{2} + c^3 f^3 (dx + c) - 3 e d c^2 f^2 (dx + c) + 3 e^2 d^2 c f (dx + c) - e^3 d^3 (dx + c) \right)
\end{aligned}$$

Problem 77: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e)^2 \operatorname{sech}(dx + c)^3}{a + I a \sinh(dx + c)} dx$$

Optimal (type 4, 373 leaves, 17 steps):

$$\begin{aligned}
& \frac{3 (fx + e)^2 \arctan(e^{dx+c})}{4 a d} - \frac{5 f^2 \arctan(\sinh(dx + c))}{6 a d^3} - \frac{I f^2 \operatorname{sech}(dx + c)^2}{12 a d^3} + \frac{I f^2 \ln(\cosh(dx + c))}{3 a d^3} - \frac{3 I f^2 \operatorname{polylog}(3, I e^{dx+c})}{4 a d^3} \\
& - \frac{I f (fx + e) \tanh(dx + c)}{3 a d^2} + \frac{I (fx + e)^2 \operatorname{sech}(dx + c)^4}{4 a d} + \frac{3 f (fx + e) \operatorname{sech}(dx + c)}{4 a d^2} + \frac{3 I f (fx + e) \operatorname{polylog}(2, I e^{dx+c})}{4 a d^2} + \frac{f (fx + e) \operatorname{sech}(dx + c)^3}{6 a d^2} \\
& - \frac{I f (fx + e) \operatorname{sech}(dx + c)^2 \tanh(dx + c)}{6 a d^2} - \frac{3 I f (fx + e) \operatorname{polylog}(2, -I e^{dx+c})}{4 a d^2} - \frac{f^2 \operatorname{sech}(dx + c) \tanh(dx + c)}{12 a d^3}
\end{aligned}$$

$$+ \frac{3 (fx + e)^2 \operatorname{sech}(dx + c) \tanh(dx + c)}{8ad} + \frac{3 I f^2 \operatorname{polylog}(3, -I e^{dx+c})}{4ad^3} + \frac{(fx + e)^2 \operatorname{sech}(dx + c)^3 \tanh(dx + c)}{4ad}$$

Result(type 4, 1043 leaves):

$$\begin{aligned} & \frac{1}{12 (e^{dx+c} + I)^2 (e^{dx+c} - I)^4 d^3 a} (18 d^2 e f x e^{dx+c} - 4 f^2 e^3 dx+3c - 2 f^2 e^{dx+c} + 6 d^2 e^2 e^3 dx+3c + 9 d^2 e^2 e^5 dx+5c + 9 d^2 f^2 x^2 e^{dx+c} - 2 d f^2 x e^{dx+c} \\ & + 16 d f^2 x e^3 dx+3c + 16 d e f e^3 dx+3c - 8 I d e f - 8 I d f^2 x - 44 I d e f e^2 dx+2c - 36 I d f^2 x e^4 dx+4c - 36 I d e f e^4 dx+4c + 18 I d^2 f^2 x^2 e^2 dx+2c \\ & - 44 I d f^2 x e^2 dx+2c + 12 d^2 e f x e^3 dx+3c + 18 d^2 e f x e^5 dx+5c - 18 I d^2 f^2 x^2 e^4 dx+4c + 9 d^2 e^2 e^{dx+c} - 18 I d^2 e^2 e^4 dx+4c + 18 I d^2 e^2 e^2 dx+2c \\ & + 9 d^2 f^2 x^2 e^5 dx+5c + 6 d^2 f^2 x^2 e^3 dx+3c + 18 d f^2 x e^5 dx+5c + 18 d e f e^5 dx+5c - 2 f^2 e^5 dx+5c + 36 I d^2 e f x e^2 dx+2c - 36 I d^2 e f x e^4 dx+4c - 2 d e f e^{dx+c}) \\ & - \frac{2 I f^2 \ln(e^{dx+c})}{3ad^3} - \frac{3 I f^2 \operatorname{polylog}(3, I e^{dx+c})}{4ad^3} - \frac{3 I e f \operatorname{polylog}(2, -I e^{dx+c})}{4ad^2} + \frac{3 I \operatorname{polylog}(2, I e^{dx+c}) f^2 x}{4ad^2} - \frac{I f^2 \ln(e^{dx+c} + I)}{2ad^3} \\ & + \frac{3 I \ln(1 - I e^{dx+c}) e f x}{4ad} + \frac{7 I f^2 \ln(e^{dx+c} - I)}{6ad^3} + \frac{3 I e f \operatorname{polylog}(2, I e^{dx+c})}{4ad^2} + \frac{3 I f^2 \operatorname{polylog}(3, -I e^{dx+c})}{4ad^3} + \frac{3 I \ln(1 - I e^{dx+c}) c e f}{4ad^2} \\ & + \frac{3 I \ln(1 - I e^{dx+c}) f^2 x^2}{8ad} - \frac{3 I \ln(1 - I e^{dx+c}) c^2 f^2}{8ad^3} + \frac{3 I e^2 \ln(e^{dx+c} + I)}{8ad} - \frac{3 I \ln(1 + I e^{dx+c}) e f x}{4ad} - \frac{3 I c f e \ln(e^{dx+c} + I)}{4ad^2} \\ & - \frac{3 I \operatorname{polylog}(2, -I e^{dx+c}) f^2 x}{4ad^2} - \frac{3 I \ln(1 + I e^{dx+c}) c e f}{4ad^2} + \frac{3 I \ln(1 + I e^{dx+c}) c^2 f^2}{8ad^3} - \frac{3 I \ln(1 + I e^{dx+c}) f^2 x^2}{8ad} + \frac{3 I c f e \ln(e^{dx+c} - I)}{4ad^2} \\ & + \frac{3 I c^2 f^2 \ln(e^{dx+c} + I)}{8ad^3} - \frac{3 I e^2 \ln(e^{dx+c} - I)}{8ad} - \frac{3 I c^2 f^2 \ln(e^{dx+c} - I)}{8ad^3} \end{aligned}$$

Problem 78: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \cosh(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 330 leaves, 11 steps):

$$\begin{aligned} & - \frac{(fx + e)^4}{4bf} + \frac{(fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{bd} + \frac{(fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{bd} + \frac{3f(fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{bd^2} \\ & + \frac{3f(fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{bd^2} - \frac{6f^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{bd^3} - \frac{6f^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{bd^3} \\ & + \frac{6f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{bd^4} + \frac{6f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{bd^4} \end{aligned}$$

Result(type 8, 157 leaves):

$$\frac{\frac{1}{4} x^4 f^3 + e f^2 x^3 + \frac{3}{2} e^2 f x^2 + e^3 x}{b} + \int -\frac{2(a f^3 x^3 e^{dx+c} + 3 a e f^2 x^2 e^{dx+c} - b f^3 x^3 + 3 a e^2 f x e^{dx+c} - 3 b e f^2 x^2 + a e^3 e^{dx+c} - 3 b e^2 f x - b e^3)}{b(b(e^{dx+c})^2 + 2 a e^{dx+c} - b)} dx$$

Problem 79: Unable to integrate problem.

$$\int \frac{(fx + e)^2 \cosh(dx + c)^2}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 357 leaves, 15 steps):

$$\begin{aligned} & -\frac{a(fx + e)^3}{3b^2 f} + \frac{2f^2 \cosh(dx + c)}{bd^3} + \frac{(fx + e)^2 \cosh(dx + c)}{bd} - \frac{2f(fx + e) \sinh(dx + c)}{bd^2} + \frac{(fx + e)^2 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^2 d} \\ & - \frac{(fx + e)^2 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^2 d} + \frac{2f(fx + e) \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^2 d^2} \\ & - \frac{2f(fx + e) \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^2 d^2} - \frac{2f^2 \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^2 d^3} + \frac{2f^2 \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^2 d^3} \end{aligned}$$

Result(type 8, 232 leaves):

$$\begin{aligned} & -\frac{a\left(\frac{1}{3} x^3 f^2 + e f x^2 + e^2 x\right)}{b^2} + \frac{(d^2 f^2 x^2 + 2 d^2 e f x + d^2 e^2 - 2 d f^2 x - 2 e f d + 2 f^2) e^{dx+c}}{2 d^3 b} + \frac{d^2 f^2 x^2 + 2 d^2 e f x + d^2 e^2 + 2 d f^2 x + 2 e f d + 2 f^2}{2 d^3 b e^{dx+c}} + \\ & \int \frac{2(a^2 f^2 x^2 + b^2 f^2 x^2 + 2 a^2 e f x + 2 b^2 e f x + a^2 e^2 + b^2 e^2) e^{dx+c}}{(b(e^{dx+c})^2 + 2 a e^{dx+c} - b) b^2} dx \end{aligned}$$

Problem 80: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \cosh(dx + c)^3}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 604 leaves, 21 steps):

$$\begin{aligned} & \frac{3f^3 x}{8bd^3} + \frac{(fx + e)^3}{4bd} - \frac{(a^2 + b^2)(fx + e)^4}{4b^3 f} + \frac{6af^3 \cosh(dx + c)}{b^2 d^4} + \frac{3af(fx + e)^2 \cosh(dx + c)}{b^2 d^2} + \frac{(a^2 + b^2)(fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^3 d} \\ & + \frac{(a^2 + b^2)(fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^3 d} + \frac{3(a^2 + b^2)f(fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^3 d^2} \end{aligned}$$

$$\begin{aligned}
& + \frac{3(a^2 + b^2)f(fx + e)^2 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^3 d^2} - \frac{6(a^2 + b^2)f^2(fx + e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^3 d^3} \\
& - \frac{6(a^2 + b^2)f^2(fx + e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^3 d^3} + \frac{6(a^2 + b^2)f^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^3 d^4} + \frac{6(a^2 + b^2)f^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^3 d^4} \\
& - \frac{6af^2(fx + e) \sinh(dx + c)}{b^2 d^3} - \frac{a(fx + e)^3 \sinh(dx + c)}{b^2 d} - \frac{3f^3 \cosh(dx + c) \sinh(dx + c)}{8bd^4} - \frac{3f(fx + e)^2 \cosh(dx + c) \sinh(dx + c)}{4bd^2} \\
& + \frac{3f^2(fx + e) \sinh(dx + c)^2}{4bd^3} + \frac{(fx + e)^3 \sinh(dx + c)^2}{2bd}
\end{aligned}$$

Result(type 8, 763 leaves):

$$\begin{aligned}
& \frac{\frac{1}{4}a^2 f^3 x^4 + \frac{1}{4}b^2 f^3 x^4 + a^2 e f^2 x^3 + b^2 e f^2 x^3 + \frac{3}{2}a^2 e^2 f x^2 + \frac{3}{2}b^2 e^2 f x^2 + a^2 e^3 x + b^2 e^3 x}{b^3} \\
& + \frac{(4d^3 f^3 x^3 + 12d^3 e f^2 x^2 + 12d^3 e^2 f x - 6d^2 f^3 x^2 + 4e^3 d^3 - 12d^2 e f^2 x - 6d^2 e^2 f + 6d f^3 x + 6d e f^2 - 3f^3) (e^{dx+c})^2}{32bd^4} \\
& - \frac{a(d^3 f^3 x^3 + 3d^3 e f^2 x^2 + 3d^3 e^2 f x - 3d^2 f^3 x^2 + e^3 d^3 - 6d^2 e f^2 x - 3d^2 e^2 f + 6d f^3 x + 6d e f^2 - 6f^3) e^{dx+c}}{2d^4 b^2} \\
& + \frac{a(d^3 f^3 x^3 + 3d^3 e f^2 x^2 + 3d^3 e^2 f x + 3d^2 f^3 x^2 + e^3 d^3 + 6d^2 e f^2 x + 3d^2 e^2 f + 6d f^3 x + 6d e f^2 + 6f^3)}{2d^4 b^2 e^{dx+c}} \\
& + \frac{4d^3 f^3 x^3 + 12d^3 e f^2 x^2 + 12d^3 e^2 f x + 6d^2 f^3 x^2 + 4e^3 d^3 + 12d^2 e f^2 x + 6d^2 e^2 f + 6d f^3 x + 6d e f^2 + 3f^3}{32bd^4 (e^{dx+c})^2} + \int \\
& - \frac{1}{b^3 (b (e^{dx+c})^2 + 2a e^{dx+c} - b)} (2(a^3 f^3 x^3 e^{dx+c} + a b^2 f^3 x^3 e^{dx+c} + 3a^3 e f^2 x^2 e^{dx+c} - a^2 b f^3 x^3 + 3a b^2 e f^2 x^2 e^{dx+c} - b^3 f^3 x^3 + 3a^3 e^2 f x e^{dx+c} \\
& - 3a^2 b e f^2 x^2 + 3a b^2 e^2 f x e^{dx+c} - 3b^3 e f^2 x^2 + a^3 e^3 e^{dx+c} - 3a^2 b e^2 f x + a b^2 e^3 e^{dx+c} - 3b^3 e^2 f x - a^2 b e^3 - b^3 e^3) dx
\end{aligned}$$

Problem 81: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(dx + c)^3}{a + b \sinh(dx + c)} dx$$

Optimal(type 3, 57 leaves, 3 steps):

$$\frac{(a^2 + b^2) \ln(a + b \sinh(dx + c))}{b^3 d} - \frac{a \sinh(dx + c)}{b^2 d} + \frac{\sinh(dx + c)^2}{2bd}$$

Result(type 3, 290 leaves):

$$\begin{aligned}
& \frac{1}{2db \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^2} + \frac{1}{2db \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} + \frac{a}{db^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right) a^2}{db^3} \\
& - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)}{db} + \frac{1}{2db \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2} - \frac{1}{2db \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)} + \frac{a}{db^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)} \\
& - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right) a^2}{db^3} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)}{db} + \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)^2 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b - a}{db^3} a^2 \\
& + \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)^2 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b - a}{db}
\end{aligned}$$

Problem 82: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \operatorname{sech}(dx + c)^2}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 725 leaves, 29 steps):

$$\begin{aligned}
& \frac{a (fx + e)^3}{(a^2 + b^2) d} - \frac{6bf (fx + e)^2 \arctan(e^{dx+c})}{(a^2 + b^2) d^2} - \frac{3af (fx + e)^2 \ln(1 + e^{2dx+2c})}{(a^2 + b^2) d^2} + \frac{b^2 (fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d} \\
& - \frac{b^2 (fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d} - \frac{61bf^2 (fx + e) \operatorname{polylog}(2, I e^{dx+c})}{(a^2 + b^2) d^3} + \frac{61bf^3 \operatorname{polylog}(3, I e^{dx+c})}{(a^2 + b^2) d^4} - \frac{3af^2 (fx + e) \operatorname{polylog}(2, -e^{2dx+2c})}{(a^2 + b^2) d^3} \\
& + \frac{3b^2 f (fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d^2} - \frac{3b^2 f (fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d^2} + \frac{61bf^2 (fx + e) \operatorname{polylog}(2, -I e^{dx+c})}{(a^2 + b^2) d^3} \\
& - \frac{61bf^3 \operatorname{polylog}(3, -I e^{dx+c})}{(a^2 + b^2) d^4} + \frac{3af^3 \operatorname{polylog}(3, -e^{2dx+2c})}{2(a^2 + b^2) d^4} - \frac{6b^2 f^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d^3} \\
& + \frac{6b^2 f^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d^3} + \frac{6b^2 f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d^4} - \frac{6b^2 f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d^4}
\end{aligned}$$



$$+ \frac{b (fx + e)^3 \operatorname{sech}(dx + c)}{(a^2 + b^2) d} + \frac{a (fx + e)^3 \tanh(dx + c)}{(a^2 + b^2) d}$$

Result(type 8, 491 leaves):

$$\begin{aligned} & - \frac{2 (f^3 x^3 + 3 e f^2 x^2 + 3 e^2 f x + e^3) (-e^{dx+c} b + a)}{d (a^2 + b^2) ((e^{dx+c})^2 + 1)} + 4 \left( \int \frac{1}{2 d (a^2 + b^2) ((e^{dx+c})^2 + 1) (b (e^{dx+c})^2 + 2 a e^{dx+c} - b)} (b^2 d f^3 x^3 (e^{dx+c})^3 \right. \\ & + 3 b^2 d e f^2 x^2 (e^{dx+c})^3 + 3 b^2 d e^2 f x (e^{dx+c})^3 + b^2 d f^3 x^3 e^{dx+c} - 3 b^2 f^3 x^2 (e^{dx+c})^3 - 3 a b f^3 x^2 (e^{dx+c})^2 + b^2 d e^3 (e^{dx+c})^3 + 3 b^2 d e f^2 x^2 e^{dx+c} \\ & - 6 b^2 e f^2 x (e^{dx+c})^3 + 6 a^2 f^3 x^2 e^{dx+c} - 6 a b e f^2 x (e^{dx+c})^2 + 3 b^2 d e^2 f x e^{dx+c} - 3 b^2 e^2 f (e^{dx+c})^3 + 3 b^2 f^3 x^2 e^{dx+c} + 12 a^2 e f^2 x e^{dx+c} \\ & \left. - 3 a b e^2 f (e^{dx+c})^2 - 3 a b f^3 x^2 + b^2 d e^3 e^{dx+c} + 6 b^2 e f^2 x e^{dx+c} + 6 a^2 e^2 f e^{dx+c} - 6 a b e f^2 x + 3 b^2 e^2 f e^{dx+c} - 3 a b e^2 f) dx \right) \end{aligned}$$

Problem 84: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(dx + c)^3}{a + b \sinh(dx + c)} dx$$

Optimal(type 3, 115 leaves, 7 steps):

$$\frac{a (a^2 + 3 b^2) \arctan(\sinh(dx + c))}{2 (a^2 + b^2)^2 d} - \frac{b^3 \ln(\cosh(dx + c))}{(a^2 + b^2)^2 d} + \frac{b^3 \ln(a + b \sinh(dx + c))}{(a^2 + b^2)^2 d} + \frac{\operatorname{sech}(dx + c)^2 (b + a \sinh(dx + c))}{2 (a^2 + b^2) d}$$

Result(type 3, 467 leaves):

$$\begin{aligned} & - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 a^3}{d (a^4 + 2 b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 b^2 a}{d (a^4 + 2 b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} - \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a^2 b}{d (a^4 + 2 b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} \\ & - \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 b^3}{d (a^4 + 2 b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a^3}{d (a^4 + 2 b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} \\ & + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^2 a}{d (a^4 + 2 b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} - \frac{b^3 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)}{d (a^4 + 2 b^2 a^2 + b^4)} + \frac{\arctan\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right) a^3}{d (a^4 + 2 b^2 a^2 + b^4)} \\ & + \frac{3 \arctan\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right) b^2 a}{d (a^4 + 2 b^2 a^2 + b^4)} + \frac{b^3 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b - a\right)}{d (a^4 + 2 b^2 a^2 + b^4)} \end{aligned}$$

Problem 85: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \cosh(dx + c)}{(a + b \sinh(dx + c))^3} dx$$

Optimal(type 3, 106 leaves, 6 steps):

$$-\frac{a \operatorname{farctanh}\left(\frac{b - a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{a^2 + b^2}}\right)}{b (a^2 + b^2)^{3/2} d^2} + \frac{-fx - e}{2 b d (a + b \sinh(dx + c))^2} - \frac{f \cosh(dx + c)}{2 (a^2 + b^2) d^2 (a + b \sinh(dx + c))}$$

Result(type 3, 307 leaves):

$$-\frac{2 a^2 d f x e^{2 d x+2 c} + 2 b^2 d f x e^{2 d x+2 c} + 2 a^2 d e e^{2 d x+2 c} - e^{3 d x+3 c} a b f + 2 b^2 d e e^{2 d x+2 c} - 2 e^{2 d x+2 c} a^2 f + b^2 f e^{2 d x+2 c} + 3 a b f e^{d x+c} - b^2 f}{b d^2 (a^2 + b^2) (b e^{2 d x+2 c} + 2 a e^{d x+c} - b)^2} + \frac{f a \ln\left(e^{d x+c} + \frac{a (a^2 + b^2)^{3/2} - a^4 - 2 b^2 a^2 - b^4}{(a^2 + b^2)^{3/2} b}\right)}{2 (a^2 + b^2)^{3/2} d^2 b} - \frac{f a \ln\left(e^{d x+c} + \frac{a (a^2 + b^2)^{3/2} + a^4 + 2 b^2 a^2 + b^4}{(a^2 + b^2)^{3/2} b}\right)}{2 (a^2 + b^2)^{3/2} d^2 b}$$

Problem 86: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \cosh(dx + c)}{(a + b \sinh(dx + c))^3} dx$$

Optimal(type 3, 106 leaves, 6 steps):

$$-\frac{a \operatorname{farctanh}\left(\frac{b - a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{a^2 + b^2}}\right)}{b (a^2 + b^2)^{3/2} d^2} + \frac{-fx - e}{2 b d (a + b \sinh(dx + c))^2} - \frac{f \cosh(dx + c)}{2 (a^2 + b^2) d^2 (a + b \sinh(dx + c))}$$

Result(type 3, 307 leaves):

$$-\frac{2 a^2 d f x e^{2 d x+2 c} + 2 b^2 d f x e^{2 d x+2 c} + 2 a^2 d e e^{2 d x+2 c} - e^{3 d x+3 c} a b f + 2 b^2 d e e^{2 d x+2 c} - 2 e^{2 d x+2 c} a^2 f + b^2 f e^{2 d x+2 c} + 3 a b f e^{d x+c} - b^2 f}{b d^2 (a^2 + b^2) (b e^{2 d x+2 c} + 2 a e^{d x+c} - b)^2} + \frac{f a \ln\left(e^{d x+c} + \frac{a (a^2 + b^2)^{3/2} - a^4 - 2 b^2 a^2 - b^4}{(a^2 + b^2)^{3/2} b}\right)}{2 (a^2 + b^2)^{3/2} d^2 b} - \frac{f a \ln\left(e^{d x+c} + \frac{a (a^2 + b^2)^{3/2} + a^4 + 2 b^2 a^2 + b^4}{(a^2 + b^2)^{3/2} b}\right)}{2 (a^2 + b^2)^{3/2} d^2 b}$$

Problem 87: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \cosh(dx + c)}{(a + b \sinh(dx + c))^3} dx$$

Optimal(type 4, 579 leaves, 19 steps):

$$-\frac{3 f (f x + e)^2}{2 b (a^2 + b^2) d^2} + \frac{3 f^2 (f x + e) \ln\left(1 + \frac{b e^{d x+c}}{a - \sqrt{a^2 + b^2}}\right)}{b (a^2 + b^2) d^3} + \frac{3 a f (f x + e)^2 \ln\left(1 + \frac{b e^{d x+c}}{a - \sqrt{a^2 + b^2}}\right)}{2 b (a^2 + b^2)^{3/2} d^2} + \frac{3 f^2 (f x + e) \ln\left(1 + \frac{b e^{d x+c}}{a + \sqrt{a^2 + b^2}}\right)}{b (a^2 + b^2) d^3}$$

$$\begin{aligned}
& - \frac{3af(fx+e)^2 \ln\left(1 + \frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{2b(a^2+b^2)^{3/2}d^2} + \frac{3f^3 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{b(a^2+b^2)d^4} + \frac{3af^2(fx+e) \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{b(a^2+b^2)^{3/2}d^3} \\
& + \frac{3f^3 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{b(a^2+b^2)d^4} - \frac{3af^2(fx+e) \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{b(a^2+b^2)^{3/2}d^3} - \frac{3af^3 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{b(a^2+b^2)^{3/2}d^4} \\
& + \frac{3af^3 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{b(a^2+b^2)^{3/2}d^4} - \frac{(fx+e)^3}{2bd(a+b\sinh(dx+c))^2} - \frac{3f(fx+e)^2 \cosh(dx+c)}{2(a^2+b^2)d^2(a+b\sinh(dx+c))}
\end{aligned}$$

Result(type 8, 554 leaves):

$$\begin{aligned}
& - \frac{1}{bd^2(b(e^{dx+c})^2 + 2ae^{dx+c} - b)^2(a^2+b^2)} (2a^2df^3x^3(e^{dx+c})^2 + 2b^2df^3x^3(e^{dx+c})^2 + 6a^2def^2x^2(e^{dx+c})^2 - 3abf^3x^2(e^{dx+c})^3 \\
& + 6b^2def^2x^2(e^{dx+c})^2 + 6a^2d^2fx(e^{dx+c})^2 - 6a^2f^3x^2(e^{dx+c})^2 - 6abef^2x(e^{dx+c})^3 + 6b^2d^2fx(e^{dx+c})^2 + 3b^2f^3x^2(e^{dx+c})^2 \\
& + 2a^2d^3(e^{dx+c})^2 - 12a^2ef^2x(e^{dx+c})^2 - 3ab^2ef(e^{dx+c})^3 + 9abf^3x^2e^{dx+c} + 2b^2d^3(e^{dx+c})^2 + 6b^2ef^2x(e^{dx+c})^2 - 6a^2e^2f(e^{dx+c})^2 \\
& + 18abef^2xe^{dx+c} + 3b^2e^2f(e^{dx+c})^2 - 3b^2f^3x^2 + 9ab^2ef^2e^{dx+c} - 6b^2ef^2x - 3b^2e^2f) + \\
& \int \frac{3f(adf^2x^2e^{dx+c} + 2adefxe^{dx+c} + ad^2e^{dx+c} - 2af^2xe^{dx+c} - 2afe^{dx+c} + 2bf^2x + 2bef)}{bd^2(a^2+b^2)(b(e^{dx+c})^2 + 2ae^{dx+c} - b)} dx
\end{aligned}$$

Problem 88: Unable to integrate problem.

$$\int \frac{(fx+e)^3 \cosh(dx+c) \sinh(dx+c)}{a+b\sinh(dx+c)} dx$$

Optimal(type 4, 422 leaves, 16 steps):

$$\begin{aligned}
& \frac{a(fx+e)^4}{4b^2f} - \frac{6f^3 \cosh(dx+c)}{bd^4} - \frac{3f(fx+e)^2 \cosh(dx+c)}{bd^2} - \frac{a(fx+e)^3 \ln\left(1 + \frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{b^2d} - \frac{a(fx+e)^3 \ln\left(1 + \frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{b^2d} \\
& - \frac{3af(fx+e)^2 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{b^2d^2} - \frac{3af(fx+e)^2 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{b^2d^2} + \frac{6af^2(fx+e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{b^2d^3} \\
& + \frac{6af^2(fx+e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{b^2d^3} - \frac{6af^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{b^2d^4} - \frac{6af^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{b^2d^4} \\
& + \frac{6f^2(fx+e) \sinh(dx+c)}{bd^3} + \frac{(fx+e)^3 \sinh(dx+c)}{bd}
\end{aligned}$$

Result(type 8, 368 leaves):

$$\begin{aligned} & - \frac{a \left( \frac{1}{4} x^4 f^3 + e f^2 x^3 + \frac{3}{2} e^2 f x^2 + e^3 x \right)}{b^2} + \frac{(d^3 f^3 x^3 + 3 d^3 e f^2 x^2 + 3 d^3 e^2 f x - 3 d^2 f^3 x^2 + e^3 d^3 - 6 d^2 e f^2 x - 3 d^2 e^2 f + 6 d f^3 x + 6 d e f^2 - 6 f^3) e^{dx+c}}{2 b d^4} \\ & - \frac{d^3 f^3 x^3 + 3 d^3 e f^2 x^2 + 3 d^3 e^2 f x + 3 d^2 f^3 x^2 + e^3 d^3 + 6 d^2 e f^2 x + 3 d^2 e^2 f + 6 d f^3 x + 6 d e f^2 + 6 f^3}{2 b d^4 e^{dx+c}} + \\ & \int \frac{2 a (a f^3 x^3 e^{dx+c} + 3 a e f^2 x^2 e^{dx+c} - b f^3 x^3 + 3 a e^2 f x e^{dx+c} - 3 b e f^2 x^2 + a e^3 e^{dx+c} - 3 b e^2 f x - b e^3)}{(b (e^{dx+c})^2 + 2 a e^{dx+c} - b) b^2} dx \end{aligned}$$

Problem 89: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \cosh(dx + c) \sinh(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 198 leaves, 10 steps):

$$\begin{aligned} & \frac{a (fx + e)^2}{2 b^2 f} - \frac{f \cosh(dx + c)}{b d^2} - \frac{a (fx + e) \ln \left( 1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^2 d} - \frac{a (fx + e) \ln \left( 1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^2 d} - \frac{a f \operatorname{polylog} \left( 2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^2 d^2} \\ & - \frac{a f \operatorname{polylog} \left( 2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^2 d^2} + \frac{(fx + e) \sinh(dx + c)}{b d} \end{aligned}$$

Result(type 4, 482 leaves):

$$\begin{aligned} & \frac{a f x^2}{2 b^2} - \frac{a e x}{b^2} + \frac{(d f x + d e - f) e^{dx+c}}{2 b d^2} - \frac{(d f x + d e + f) e^{-dx-c}}{2 b d^2} - \frac{2 a f c \ln(e^{dx+c})}{b^2 d^2} + \frac{a f c \ln(b e^{2 dx+2 c} + 2 a e^{dx+c} - b)}{b^2 d^2} + \frac{2 a e \ln(e^{dx+c})}{b^2 d} \\ & - \frac{a e \ln(b e^{2 dx+2 c} + 2 a e^{dx+c} - b)}{b^2 d} + \frac{2 a f c x}{b^2 d} + \frac{a f c^2}{b^2 d^2} - \frac{a f \ln \left( \frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}} \right) x}{b^2 d} - \frac{a f \ln \left( \frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}} \right) c}{b^2 d^2} \\ & - \frac{a f \ln \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right) x}{b^2 d} - \frac{a f \ln \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right) c}{b^2 d^2} - \frac{a f \operatorname{dilog} \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right)}{b^2 d^2} \\ & - \frac{a f \operatorname{dilog} \left( \frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}} \right)}{b^2 d^2} \end{aligned}$$

Problem 91: Unable to integrate problem.

$$\int \frac{(fx + e)^2 \cosh(dx + c)^2 \sinh(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 468 leaves, 20 steps):

$$\begin{aligned} & \frac{f^2 x}{4 b d^2} + \frac{a^2 (fx + e)^3}{3 b^3 f} + \frac{(fx + e)^3}{6 b f} - \frac{2 a f^2 \cosh(dx + c)}{b^2 d^3} - \frac{a (fx + e)^2 \cosh(dx + c)}{b^2 d} - \frac{f (fx + e) \cosh(dx + c)^2}{2 b d^2} + \frac{2 a f (fx + e) \sinh(dx + c)}{b^2 d^2} \\ & + \frac{f^2 \cosh(dx + c) \sinh(dx + c)}{4 b d^3} + \frac{(fx + e)^2 \cosh(dx + c) \sinh(dx + c)}{2 b d} - \frac{a (fx + e)^2 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^3 d} \\ & + \frac{a (fx + e)^2 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^3 d} - \frac{2 a f (fx + e) \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^3 d^2} \\ & + \frac{2 a f (fx + e) \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^3 d^2} + \frac{2 a f^2 \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^3 d^3} \\ & - \frac{2 a f^2 \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^3 d^3} \end{aligned}$$

Result (type 8, 391 leaves):

$$\begin{aligned} & \frac{\frac{2}{3} a^2 f^2 x^3 + \frac{1}{3} b^2 f^2 x^3 + 2 a^2 e f x^2 + b^2 e f x^2 + 2 a^2 e^2 x + b^2 e^2 x}{2 b^3} + \frac{(2 d^2 f^2 x^2 + 4 d^2 e f x + 2 d^2 e^2 - 2 d f^2 x - 2 e f d + f^2) (e^{dx+c})^2}{16 b d^3} \\ & - \frac{a (d^2 f^2 x^2 + 2 d^2 e f x + d^2 e^2 - 2 d f^2 x - 2 e f d + 2 f^2) e^{dx+c}}{2 b^2 d^3} - \frac{a (d^2 f^2 x^2 + 2 d^2 e f x + d^2 e^2 + 2 d f^2 x + 2 e f d + 2 f^2)}{2 b^2 d^3 e^{dx+c}} \\ & - \frac{2 d^2 f^2 x^2 + 4 d^2 e f x + 2 d^2 e^2 + 2 d f^2 x + 2 e f d + f^2}{16 b d^3 (e^{dx+c})^2} + \int - \frac{2 a (a^2 f^2 x^2 + b^2 f^2 x^2 + 2 a^2 e f x + 2 b^2 e f x + a^2 e^2 + b^2 e^2) e^{dx+c}}{(b (e^{dx+c})^2 + 2 a e^{dx+c} - b) b^3} dx \end{aligned}$$

Problem 92: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \cosh(dx + c)^3 \sinh(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 812 leaves, 30 steps):

$$-\frac{3 a (a^2 + b^2) f (fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^4 d^2} - \frac{3 a (a^2 + b^2) f (fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^4 d^2}$$

$$\begin{aligned}
& + \frac{6a(a^2+b^2)f^2(fx+e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{b^4 d^3} + \frac{6a(a^2+b^2)f^2(fx+e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{b^4 d^3} \\
& + \frac{3af(fx+e)^2 \cosh(dx+c) \sinh(dx+c)}{4b^2 d^2} + \frac{a^2(fx+e)^3 \sinh(dx+c)}{b^3 d} - \frac{a(a^2+b^2)(fx+e)^3 \ln\left(1 + \frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{b^4 d} \\
& - \frac{a(a^2+b^2)(fx+e)^3 \ln\left(1 + \frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{b^4 d} - \frac{6a(a^2+b^2)f^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{b^4 d^4} - \frac{6a(a^2+b^2)f^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{b^4 d^4} \\
& - \frac{40f^3 \cosh(dx+c)}{9b d^4} - \frac{a(fx+e)^3}{4b^2 d} - \frac{2f^3 \cosh(dx+c)^3}{27b d^4} + \frac{2(fx+e)^3 \sinh(dx+c)}{3b d} + \frac{a(a^2+b^2)(fx+e)^4}{4b^4 f} - \frac{6a^2 f^3 \cosh(dx+c)}{b^3 d^4} \\
& - \frac{f(fx+e)^2 \cosh(dx+c)^3}{3b d^2} + \frac{(fx+e)^3 \cosh(dx+c)^2 \sinh(dx+c)}{3b d} - \frac{a(fx+e)^3 \sinh(dx+c)^2}{2b^2 d} - \frac{2f(fx+e)^2 \cosh(dx+c)}{b d^2} \\
& + \frac{40f^2(fx+e) \sinh(dx+c)}{9b d^3} - \frac{3af^3 x}{8b^2 d^3} - \frac{3a^2 f(fx+e)^2 \cosh(dx+c)}{b^3 d^2} + \frac{6a^2 f^2(fx+e) \sinh(dx+c)}{b^3 d^3} + \frac{3af^3 \cosh(dx+c) \sinh(dx+c)}{8b^2 d^4} \\
& + \frac{2f^2(fx+e) \cosh(dx+c)^2 \sinh(dx+c)}{9b d^3} - \frac{3af^2(fx+e) \sinh(dx+c)^2}{4b^2 d^3}
\end{aligned}$$

Result(type 8, 1143 leaves):

$$\begin{aligned}
& - \frac{a\left(\frac{1}{4}a^2 f^3 x^4 + \frac{1}{4}b^2 f^3 x^4 + a^2 e f^2 x^3 + b^2 e f^2 x^3 + \frac{3}{2}a^2 e^2 f x^2 + \frac{3}{2}b^2 e^2 f x^2 + a^2 e^3 x + b^2 e^3 x\right)}{b^4} \\
& + \frac{(9d^3 f^3 x^3 + 27d^3 e f^2 x^2 + 27d^3 e^2 f x - 9d^2 f^3 x^2 + 9e^3 d^3 - 18d^2 e f^2 x - 9d^2 e^2 f + 6d f^3 x + 6d e f^2 - 2f^3)(e^{dx+c})^3}{216b d^4} \\
& - \frac{a(4d^3 f^3 x^3 + 12d^3 e f^2 x^2 + 12d^3 e^2 f x - 6d^2 f^3 x^2 + 4e^3 d^3 - 12d^2 e f^2 x - 6d^2 e^2 f + 6d f^3 x + 6d e f^2 - 3f^3)(e^{dx+c})^2}{32b^2 d^4} + \frac{1}{8b^3 d^4} \left( (4a^2 d^3 f^3 x^3 \right. \\
& + 3b^2 d^3 f^3 x^3 + 12a^2 d^3 e f^2 x^2 + 9b^2 d^3 e f^2 x^2 + 12a^2 d^3 e^2 f x - 12a^2 d^2 f^3 x^2 + 9b^2 d^3 e^2 f x - 9b^2 d^2 f^3 x^2 + 4a^2 d^3 e^3 - 24a^2 d^2 e f^2 x + 3b^2 d^3 e^3 \\
& \left. - 18b^2 d^2 e f^2 x - 12a^2 d^2 e^2 f + 24a^2 d f^3 x - 9b^2 d^2 e^2 f + 18b^2 d f^3 x + 24a^2 d e f^2 + 18b^2 d e f^2 - 24a^2 f^3 - 18b^2 f^3) e^{dx+c} \right) \\
& - \frac{(4a^2 + 3b^2)(d^3 f^3 x^3 + 3d^3 e f^2 x^2 + 3d^3 e^2 f x + 3d^2 f^3 x^2 + e^3 d^3 + 6d^2 e f^2 x + 3d^2 e^2 f + 6d f^3 x + 6d e f^2 + 6f^3)}{8b^3 d^4 e^{dx+c}} \\
& - \frac{a(4d^3 f^3 x^3 + 12d^3 e f^2 x^2 + 12d^3 e^2 f x + 6d^2 f^3 x^2 + 4e^3 d^3 + 12d^2 e f^2 x + 6d^2 e^2 f + 6d f^3 x + 6d e f^2 + 3f^3)}{32b^2 d^4 (e^{dx+c})^2} \\
& - \frac{9d^3 f^3 x^3 + 27d^3 e f^2 x^2 + 27d^3 e^2 f x + 9d^2 f^3 x^2 + 9e^3 d^3 + 18d^2 e f^2 x + 9d^2 e^2 f + 6d f^3 x + 6d e f^2 + 2f^3}{216b d^4 (e^{dx+c})^3} +
\end{aligned}$$

$$\int \frac{1}{(b(e^{dx+c})^2 + 2ae^{dx+c} - b)b^4} (2a(a^3 f^3 x^3 e^{dx+c} + ab^2 f^3 x^3 e^{dx+c} + 3a^3 e f^2 x^2 e^{dx+c} - a^2 b f^3 x^3 + 3ab^2 e f^2 x^2 e^{dx+c} - b^3 f^3 x^3 + 3a^3 e^2 f x e^{dx+c} - 3a^2 b e f^2 x^2 + 3ab^2 e^2 f x e^{dx+c} - 3b^3 e f^2 x^2 + a^3 e^3 e^{dx+c} - 3a^2 b e^2 f x + ab^2 e^3 e^{dx+c} - 3b^3 e^2 f x - a^2 b e^3 - b^3 e^3)) dx$$

Problem 93: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \cosh(dx + c)^3 \sinh(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 372 leaves, 17 steps):

$$\begin{aligned} & -\frac{afx}{4b^2d} + \frac{a(a^2 + b^2)(fx + e)^2}{2b^4f} - \frac{a^2 f \cosh(dx + c)}{b^3 d^2} - \frac{2f \cosh(dx + c)}{3b d^2} - \frac{f \cosh(dx + c)^3}{9b d^2} - \frac{a(a^2 + b^2)(fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^4 d} \\ & - \frac{a(a^2 + b^2)(fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^4 d} - \frac{a(a^2 + b^2) f \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^4 d^2} - \frac{a(a^2 + b^2) f \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^4 d^2} \\ & + \frac{a^2 (fx + e) \sinh(dx + c)}{b^3 d} + \frac{2(fx + e) \sinh(dx + c)}{3b d} + \frac{a f \cosh(dx + c) \sinh(dx + c)}{4b^2 d^2} + \frac{(fx + e) \cosh(dx + c)^2 \sinh(dx + c)}{3b d} \\ & - \frac{a(fx + e) \sinh(dx + c)^2}{2b^2 d} \end{aligned}$$

Result (type 4, 1101 leaves):

$$\begin{aligned} & -\frac{a^3 e \ln(b e^{2dx+2c} + 2a e^{dx+c} - b)}{b^4 d} - \frac{a^3 f \operatorname{dilog}\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right)}{b^4 d^2} - \frac{a^3 f \operatorname{dilog}\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right)}{b^4 d^2} + \frac{2a^3 e \ln(e^{dx+c})}{b^4 d} + \frac{a^3 f c^2}{b^4 d^2} \\ & - \frac{a(2dfx + 2de - f) e^{2dx+2c}}{16b^2 d^2} - \frac{(4a^2 + 3b^2)(dfx + de + f) e^{-dx-c}}{8b^3 d^2} - \frac{a(2dfx + 2de + f) e^{-2dx-2c}}{16b^2 d^2} - \frac{a e \ln(b e^{2dx+2c} + 2a e^{dx+c} - b)}{b^2 d} \\ & - \frac{a f \operatorname{dilog}\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right)}{b^2 d^2} - \frac{a f \operatorname{dilog}\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right)}{b^2 d^2} + \frac{a f c^2}{b^2 d^2} + \frac{2a e \ln(e^{dx+c})}{b^2 d} + \frac{a^3 f x^2}{2b^4} + \frac{a f x^2}{2b^2} - \frac{a^3 e x}{b^4} - \frac{a e x}{b^2} \\ & + \frac{2a f c x}{b^2 d} - \frac{2a f c \ln(e^{dx+c})}{b^2 d^2} + \frac{a f c \ln(b e^{2dx+2c} + 2a e^{dx+c} - b)}{b^2 d^2} - \frac{a f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) x}{b^2 d} - \frac{a f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) c}{b^2 d^2} \\ & - \frac{a f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) x}{b^2 d} - \frac{a f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) c}{b^2 d^2} + \frac{(3dfx + 3de - f) e^{3dx+3c}}{72d^2 b} - \frac{(3dfx + 3de + f) e^{-3dx-3c}}{72d^2 b} \end{aligned}$$

$$\begin{aligned}
& + \frac{2a^3 f c x}{b^4 d} - \frac{a^3 f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) x}{b^4 d} - \frac{a^3 f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) c}{b^4 d^2} - \frac{a^3 f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) x}{b^4 d} \\
& - \frac{a^3 f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) c}{b^4 d^2} - \frac{2a^3 f c \ln(e^{dx+c})}{b^4 d^2} + \frac{a^3 f c \ln(b e^{2dx+2c} + 2a e^{dx+c} - b)}{b^4 d^2} \\
& + \frac{(4a^2 d f x + 3b^2 d f x + 4a^2 d e + 3b^2 d e - 4a^2 f - 3b^2 f) e^{dx+c}}{8b^3 d^2}
\end{aligned}$$

Problem 95: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \tanh(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 953 leaves, 39 steps):

$$\begin{aligned}
& \frac{3Ia^2 f (fx + e)^2 \operatorname{polylog}(2, -Ie^{dx+c})}{b(a^2 + b^2)d^2} + \frac{6Ia^2 f^2 (fx + e) \operatorname{polylog}(3, Ie^{dx+c})}{b(a^2 + b^2)d^3} - \frac{6Ia^2 f^3 \operatorname{polylog}(4, Ie^{dx+c})}{b(a^2 + b^2)d^4} + \frac{3If(fx + e)^2 \operatorname{polylog}(2, Ie^{dx+c})}{b d^2} \\
& + \frac{6If^2 (fx + e) \operatorname{polylog}(3, -Ie^{dx+c})}{b d^3} + \frac{a (fx + e)^3 \ln(1 + e^{2dx+2c})}{(a^2 + b^2)d} - \frac{a (fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d} \\
& - \frac{a (fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d} - \frac{6af^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d^4} - \frac{6af^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d^4} \\
& - \frac{3af(fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d^2} - \frac{3af(fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d^2} + \frac{6af^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d^3} \\
& + \frac{6af^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d^3} - \frac{2a^2 (fx + e)^3 \arctan(e^{dx+c})}{b(a^2 + b^2)d} + \frac{3af(fx + e)^2 \operatorname{polylog}(2, -e^{2dx+2c})}{2(a^2 + b^2)d^2} \\
& - \frac{3af^2 (fx + e) \operatorname{polylog}(3, -e^{2dx+2c})}{2(a^2 + b^2)d^3} + \frac{6If^3 \operatorname{polylog}(4, Ie^{dx+c})}{b d^4} - \frac{3If(fx + e)^2 \operatorname{polylog}(2, -Ie^{dx+c})}{b d^2} - \frac{6If^2 (fx + e) \operatorname{polylog}(3, Ie^{dx+c})}{b d^3} \\
& + \frac{2(fx + e)^3 \arctan(e^{dx+c})}{b d} + \frac{6Ia^2 f^3 \operatorname{polylog}(4, -Ie^{dx+c})}{b(a^2 + b^2)d^4} - \frac{3Ia^2 f (fx + e)^2 \operatorname{polylog}(2, Ie^{dx+c})}{b(a^2 + b^2)d^2} - \frac{6Ia^2 f^2 (fx + e) \operatorname{polylog}(3, -Ie^{dx+c})}{b(a^2 + b^2)d^3} \\
& + \frac{3af^3 \operatorname{polylog}(4, -e^{2dx+2c})}{4(a^2 + b^2)d^4} - \frac{6If^3 \operatorname{polylog}(4, -Ie^{dx+c})}{b d^4}
\end{aligned}$$



Result(type 8, 28 leaves):

$$\int \frac{(fx + e)^3 \tanh(dx + c)}{a + b \sinh(dx + c)} dx$$

Problem 96: Unable to integrate problem.

$$\int \frac{(fx + e)^2 \tanh(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 670 leaves, 32 steps):

$$\begin{aligned} & \frac{2(fx + e)^2 \arctan(e^{dx+c})}{bd} - \frac{2a^2(fx + e)^2 \arctan(e^{dx+c})}{b(a^2 + b^2)d} + \frac{a(fx + e)^2 \ln(1 + e^{2dx+2c})}{(a^2 + b^2)d} - \frac{a(fx + e)^2 \ln\left(1 + \frac{be^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d} \\ & - \frac{a(fx + e)^2 \ln\left(1 + \frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d} + \frac{2Ia^2f(fx + e) \operatorname{polylog}(2, -Ie^{dx+c})}{b(a^2 + b^2)d^2} + \frac{2Ia^2f^2 \operatorname{polylog}(3, Ie^{dx+c})}{b(a^2 + b^2)d^3} - \frac{2If(fx + e) \operatorname{polylog}(2, -Ie^{dx+c})}{bd^2} \\ & - \frac{2Ia^2f(fx + e) \operatorname{polylog}(2, Ie^{dx+c})}{b(a^2 + b^2)d^2} + \frac{af(fx + e) \operatorname{polylog}(2, -e^{2dx+2c})}{(a^2 + b^2)d^2} - \frac{2af(fx + e) \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d^2} \\ & - \frac{2af(fx + e) \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d^2} + \frac{2If^2 \operatorname{polylog}(3, -Ie^{dx+c})}{bd^3} - \frac{2If^2 \operatorname{polylog}(3, Ie^{dx+c})}{bd^3} - \frac{2Ia^2f^2 \operatorname{polylog}(3, -Ie^{dx+c})}{b(a^2 + b^2)d^3} \\ & + \frac{2If(fx + e) \operatorname{polylog}(2, Ie^{dx+c})}{bd^2} - \frac{af^2 \operatorname{polylog}(3, -e^{2dx+2c})}{2(a^2 + b^2)d^3} + \frac{2af^2 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d^3} + \frac{2af^2 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)d^3} \end{aligned}$$

Result(type 8, 28 leaves):

$$\int \frac{(fx + e)^2 \tanh(dx + c)}{a + b \sinh(dx + c)} dx$$

Problem 97: Unable to integrate problem.

$$\int \frac{(fx + e)^2 \operatorname{sech}(dx + c) \tanh(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 611 leaves, 30 steps):

$$\frac{(fx + e)^2}{bd} - \frac{a^2(fx + e)^2}{b(a^2 + b^2)d} + \frac{4af(fx + e) \arctan(e^{dx+c})}{(a^2 + b^2)d^2} - \frac{2f(fx + e) \ln(1 + e^{2dx+2c})}{bd^2} + \frac{2a^2f(fx + e) \ln(1 + e^{2dx+2c})}{b(a^2 + b^2)d^2}$$

$$\begin{aligned}
& - \frac{ab (fx + e)^2 \ln \left( 1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{(a^2 + b^2)^{3/2} d} + \frac{ab (fx + e)^2 \ln \left( 1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{(a^2 + b^2)^{3/2} d} - \frac{2 I a f^2 \operatorname{polylog}(2, -I e^{dx+c})}{(a^2 + b^2) d^3} + \frac{2 I a f^2 \operatorname{polylog}(2, I e^{dx+c})}{(a^2 + b^2) d^3} \\
& - \frac{f^2 \operatorname{polylog}(2, -e^{2dx+2c})}{b d^3} + \frac{a^2 f^2 \operatorname{polylog}(2, -e^{2dx+2c})}{b (a^2 + b^2) d^3} - \frac{2 a b f (fx + e) \operatorname{polylog} \left( 2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{(a^2 + b^2)^{3/2} d^2} \\
& + \frac{2 a b f (fx + e) \operatorname{polylog} \left( 2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{(a^2 + b^2)^{3/2} d^2} + \frac{2 a b f^2 \operatorname{polylog} \left( 3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{(a^2 + b^2)^{3/2} d^3} - \frac{2 a b f^2 \operatorname{polylog} \left( 3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{(a^2 + b^2)^{3/2} d^3} \\
& - \frac{a (fx + e)^2 \operatorname{sech}(dx + c)}{(a^2 + b^2) d} + \frac{(fx + e)^2 \tanh(dx + c)}{b d} - \frac{a^2 (fx + e)^2 \tanh(dx + c)}{b (a^2 + b^2) d}
\end{aligned}$$

Result(type 8, 340 leaves):

$$\begin{aligned}
& - \frac{2 (x^2 f^2 + 2 e f x + e^2) (a e^{dx+c} + b)}{d (a^2 + b^2) ((e^{dx+c})^2 + 1)} + 2 \left( \int \frac{1}{d (a^2 + b^2) ((e^{dx+c})^2 + 1) (b (e^{dx+c})^2 + 2 a e^{dx+c} - b)} (-a b d f^2 x^2 (e^{dx+c})^3 - 2 a b d e f x (e^{dx+c})^3 \right. \\
& - a b d e^2 (e^{dx+c})^3 - a b d f^2 x^2 e^{dx+c} + 2 a b f^2 x (e^{dx+c})^3 + 4 a^2 f^2 x (e^{dx+c})^2 - 2 a b d e f x e^{dx+c} + 2 a b e f (e^{dx+c})^3 + 2 b^2 f^2 x (e^{dx+c})^2 \\
& \left. + 4 a^2 e f (e^{dx+c})^2 - a b d e^2 e^{dx+c} + 2 a b f^2 x e^{dx+c} + 2 b^2 e f (e^{dx+c})^2 + 2 a b e f e^{dx+c} - 2 b^2 f^2 x - 2 b^2 e f) dx \right)
\end{aligned}$$

Problem 98: Unable to integrate problem.

$$\int \frac{(fx + e)^2 \cosh(dx + c) \sinh(dx + c)^2}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 419 leaves, 17 steps):

$$\begin{aligned}
& \frac{efx}{2 b d} + \frac{f^2 x^2}{4 b d} - \frac{a^2 (fx + e)^3}{3 b^3 f} + \frac{2 a f (fx + e) \cosh(dx + c)}{b^2 d^2} + \frac{a^2 (fx + e)^2 \ln \left( 1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^3 d} + \frac{a^2 (fx + e)^2 \ln \left( 1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^3 d} \\
& + \frac{2 a^2 f (fx + e) \operatorname{polylog} \left( 2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^3 d^2} + \frac{2 a^2 f (fx + e) \operatorname{polylog} \left( 2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^3 d^2} - \frac{2 a^2 f^2 \operatorname{polylog} \left( 3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^3 d^3} \\
& - \frac{2 a^2 f^2 \operatorname{polylog} \left( 3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^3 d^3} - \frac{2 a f^2 \sinh(dx + c)}{b^2 d^3} - \frac{a (fx + e)^2 \sinh(dx + c)}{b^2 d} - \frac{f (fx + e) \cosh(dx + c) \sinh(dx + c)}{2 b d^2} \\
& + \frac{f^2 \sinh(dx + c)^2}{4 b d^3} + \frac{(fx + e)^2 \sinh(dx + c)^2}{2 b d}
\end{aligned}$$

Result(type 8, 358 leaves):

$$\frac{a^2 \left( \frac{1}{3} x^3 f^2 + e f x^2 + e^2 x \right)}{b^3} + \frac{(2 d^2 f^2 x^2 + 4 d^2 e f x + 2 d^2 e^2 - 2 d f^2 x - 2 e f d + f^2) (e^{dx+c})^2}{16 b d^3} - \frac{a (d^2 f^2 x^2 + 2 d^2 e f x + d^2 e^2 - 2 d f^2 x - 2 e f d + 2 f^2) e^{dx+c}}{2 b^2 d^3}$$

$$+ \frac{a (d^2 f^2 x^2 + 2 d^2 e f x + d^2 e^2 + 2 d f^2 x + 2 e f d + 2 f^2)}{2 b^2 d^3 e^{dx+c}} + \frac{2 d^2 f^2 x^2 + 4 d^2 e f x + 2 d^2 e^2 + 2 d f^2 x + 2 e f d + f^2}{16 b d^3 (e^{dx+c})^2} + \int$$

$$- \frac{2 a^2 (a f^2 x^2 e^{dx+c} + 2 a e f x e^{dx+c} - b f^2 x^2 + a e^2 e^{dx+c} - 2 b e f x - b e^2)}{(b (e^{dx+c})^2 + 2 a e^{dx+c} - b) b^3} dx$$

Problem 99: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \cosh(dx + c) \sinh(dx + c)^2}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 258 leaves, 14 steps):

$$\frac{fx}{4 b d} - \frac{a^2 (fx + e)^2}{2 b^3 f} + \frac{a f \cosh(dx + c)}{b^2 d^2} + \frac{a^2 (fx + e) \ln \left( 1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^3 d} + \frac{a^2 (fx + e) \ln \left( 1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^3 d}$$

$$+ \frac{a^2 f \text{polylog} \left( 2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}} \right)}{b^3 d^2} + \frac{a^2 f \text{polylog} \left( 2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}} \right)}{b^3 d^2} - \frac{a (fx + e) \sinh(dx + c)}{b^2 d} - \frac{f \cosh(dx + c) \sinh(dx + c)}{4 b d^2}$$

$$+ \frac{(fx + e) \sinh(dx + c)^2}{2 b d}$$

Result (type 4, 564 leaves):

$$- \frac{a^2 f x^2}{2 b^3} + \frac{a^2 e x}{b^3} + \frac{(2 d f x + 2 d e - f) e^{2 dx+2 c}}{16 b d^2} - \frac{a (d f x + d e - f) e^{dx+c}}{2 b^2 d^2} + \frac{a (d f x + d e + f) e^{-dx-c}}{2 b^2 d^2} + \frac{(2 d f x + 2 d e + f) e^{-2 dx-2 c}}{16 b d^2}$$

$$+ \frac{2 a^2 f c \ln(e^{dx+c})}{b^3 d^2} - \frac{a^2 f c \ln(b e^{2 dx+2 c} + 2 a e^{dx+c} - b)}{b^3 d^2} - \frac{2 a^2 e \ln(e^{dx+c})}{b^3 d} + \frac{a^2 e \ln(b e^{2 dx+2 c} + 2 a e^{dx+c} - b)}{b^3 d} - \frac{2 a^2 f c x}{b^3 d} - \frac{a^2 f c^2}{b^3 d^2}$$

$$+ \frac{a^2 f \ln \left( \frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}} \right) x}{b^3 d} + \frac{a^2 f \ln \left( \frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}} \right) c}{b^3 d^2} + \frac{a^2 f \ln \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right) x}{b^3 d}$$

$$+ \frac{a^2 f \ln \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right) c}{b^3 d^2} + \frac{a^2 f \text{dilog} \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right)}{b^3 d^2} + \frac{a^2 f \text{dilog} \left( \frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}} \right)}{b^3 d^2}$$

Problem 100: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \cosh(dx + c)^2 \sinh(dx + c)^2}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 367 leaves, 19 steps):

$$\begin{aligned} & -\frac{a^3 ex}{b^4} - \frac{a ex}{2b^2} - \frac{a^3 fx^2}{2b^4} - \frac{afx^2}{4b^2} + \frac{a^2 (fx + e) \cosh(dx + c)}{b^3 d} + \frac{af \cosh(dx + c)^2}{4b^2 d^2} + \frac{(fx + e) \cosh(dx + c)^3}{3bd} - \frac{a^2 f \sinh(dx + c)}{b^3 d^2} - \frac{f \sinh(dx + c)}{3bd^2} \\ & - \frac{a (fx + e) \cosh(dx + c) \sinh(dx + c)}{2b^2 d} - \frac{f \sinh(dx + c)^3}{9bd^2} + \frac{a^2 (fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^4 d} \\ & - \frac{a^2 (fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^4 d} + \frac{a^2 f \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^4 d^2} - \frac{a^2 f \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^4 d^2} \end{aligned}$$

Result (type 4, 1127 leaves):

$$\begin{aligned} & -\frac{a(2dfx + 2de - f)e^{2dx+2c}}{16b^2 d^2} + \frac{a(2dfx + 2de + f)e^{-2dx-2c}}{16b^2 d^2} + \frac{(4a^2 + b^2)(dfx + de + f)e^{-dx-c}}{8b^3 d^2} - \frac{a^3 fx^2}{2b^4} - \frac{afx^2}{4b^2} - \frac{a^3 ex}{b^4} - \frac{a ex}{2b^2} \\ & - \frac{2a^4 e \operatorname{arctanh}\left(\frac{2e^{dx+c}b + 2a}{2\sqrt{a^2 + b^2}}\right)}{b^4 d \sqrt{a^2 + b^2}} + \frac{a^4 f \operatorname{dilog}\left(\frac{-e^{dx+c}b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right)}{b^4 d^2 \sqrt{a^2 + b^2}} - \frac{a^4 f \operatorname{dilog}\left(\frac{e^{dx+c}b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right)}{b^4 d^2 \sqrt{a^2 + b^2}} \\ & + \frac{a^2 f \ln\left(\frac{-e^{dx+c}b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) x}{b^2 d \sqrt{a^2 + b^2}} + \frac{a^2 f \ln\left(\frac{-e^{dx+c}b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) c}{b^2 d^2 \sqrt{a^2 + b^2}} - \frac{a^2 f \ln\left(\frac{e^{dx+c}b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) x}{b^2 d \sqrt{a^2 + b^2}} \\ & - \frac{a^2 f \ln\left(\frac{e^{dx+c}b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) c}{b^2 d^2 \sqrt{a^2 + b^2}} + \frac{2a^2 c f \operatorname{arctanh}\left(\frac{2e^{dx+c}b + 2a}{2\sqrt{a^2 + b^2}}\right)}{b^2 d^2 \sqrt{a^2 + b^2}} - \frac{2a^2 e \operatorname{arctanh}\left(\frac{2e^{dx+c}b + 2a}{2\sqrt{a^2 + b^2}}\right)}{b^2 d \sqrt{a^2 + b^2}} \\ & + \frac{a^2 f \operatorname{dilog}\left(\frac{-e^{dx+c}b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right)}{b^2 d^2 \sqrt{a^2 + b^2}} - \frac{a^2 f \operatorname{dilog}\left(\frac{e^{dx+c}b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right)}{b^2 d^2 \sqrt{a^2 + b^2}} + \frac{(3dfx + 3de - f)e^{3dx+3c}}{72d^2 b} + \frac{(3dfx + 3de + f)e^{-3dx-3c}}{72d^2 b} \\ & + \frac{a^4 f \ln\left(\frac{-e^{dx+c}b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) x}{b^4 d \sqrt{a^2 + b^2}} + \frac{a^4 f \ln\left(\frac{-e^{dx+c}b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) c}{b^4 d^2 \sqrt{a^2 + b^2}} - \frac{a^4 f \ln\left(\frac{e^{dx+c}b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) x}{b^4 d \sqrt{a^2 + b^2}} \end{aligned}$$

$$-\frac{a^4 f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) c}{b^4 d^2 \sqrt{a^2 + b^2}} + \frac{2 a^4 f c \operatorname{arctanh}\left(\frac{2 e^{dx+c} b + 2 a}{2 \sqrt{a^2 + b^2}}\right)}{b^4 d^2 \sqrt{a^2 + b^2}} + \frac{(4 a^2 d f x + b^2 d f x + 4 a^2 d e + b^2 d e - 4 a^2 f - b^2 f) e^{dx+c}}{8 b^3 d^2}$$

Problem 101: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(dx+c)^3 \sinh(dx+c)^2}{a + b \sinh(dx+c)} dx$$

Optimal (type 3, 107 leaves, 4 steps):

$$\frac{a^2 (a^2 + b^2) \ln(a + b \sinh(dx+c))}{b^5 d} - \frac{a (a^2 + b^2) \sinh(dx+c)}{b^4 d} + \frac{(a^2 + b^2) \sinh(dx+c)^2}{2 b^3 d} - \frac{a \sinh(dx+c)^3}{3 b^2 d} + \frac{\sinh(dx+c)^4}{4 b d}$$

Result (type 3, 613 leaves):

$$\begin{aligned} & \frac{5}{8 d b \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^2} + \frac{5}{8 d b \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2} + \frac{1}{4 d b \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^4} + \frac{1}{2 d b \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^3} \\ & + \frac{1}{4 d b \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^4} - \frac{1}{2 d b \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^3} + \frac{3}{8 d b \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} - \frac{3}{8 d b \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)} \\ & + \frac{a}{d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right) a^2}{d b^3} + \frac{a}{d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right) a^2}{d b^3} \\ & + \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)^2 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b - a}{d b^3} a^2 + \frac{a}{3 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^3} + \frac{a^2}{2 d b^3 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^2} \\ & + \frac{a}{2 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^2} + \frac{a^3}{d b^4 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} + \frac{a^2}{2 d b^3 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} - \frac{a^4 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)}{d b^5} \\ & + \frac{a}{3 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^3} + \frac{a^2}{2 d b^3 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2} - \frac{a}{2 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2} + \frac{a^3}{d b^4 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)} \\ & - \frac{a^2}{2 d b^3 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)} - \frac{a^4 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)}{d b^5} + \frac{a^4 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)^2 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b - a}{d b^5} \end{aligned}$$

Problem 102: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(dx+c) \tanh(dx+c)}{a+b \sinh(dx+c)} dx$$

Optimal (type 3, 74 leaves, 7 steps):

$$-\frac{a \arctan(\sinh(dx+c))}{(a^2+b^2)d} + \frac{b \ln(\cosh(dx+c))}{(a^2+b^2)d} + \frac{a^2 \ln(a+b \sinh(dx+c))}{b(a^2+b^2)d}$$

Result (type 3, 152 leaves):

$$\begin{aligned} & -\frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)}{db} + \frac{4b \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)}{d(4a^2 + 4b^2)} - \frac{8a \arctan\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)}{d(4a^2 + 4b^2)} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)}{db} \\ & + \frac{a^2 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b - a\right)}{db(a^2 + b^2)} \end{aligned}$$

Problem 103: Unable to integrate problem.

$$\int \frac{(fx+e)^3 \tanh(dx+c)^2}{a+b \sinh(dx+c)} dx$$

Optimal (type 4, 1048 leaves, 45 steps):

$$\begin{aligned} & \frac{6Ia^2 f^2 (fx+e) \operatorname{polylog}(2, -Ie^{dx+c})}{b(a^2+b^2)d^3} - \frac{3a^3 f (fx+e)^2 \ln(1+e^{2dx+2c})}{b^2(a^2+b^2)d^2} + \frac{6If^2 (fx+e) \operatorname{polylog}(2, Ie^{dx+c})}{bd^3} - \frac{3a^3 f^2 (fx+e) \operatorname{polylog}(2, -e^{2dx+2c})}{b^2(a^2+b^2)d^3} \\ & - \frac{6Ia^2 f^3 \operatorname{polylog}(3, -Ie^{dx+c})}{b(a^2+b^2)d^4} - \frac{6a^2 f (fx+e)^2 \arctan(e^{dx+c})}{b(a^2+b^2)d^2} + \frac{a^2 (fx+e)^3 \ln\left(1 + \frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{(a^2+b^2)^{3/2}d} - \frac{a^2 (fx+e)^3 \ln\left(1 + \frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{(a^2+b^2)^{3/2}d} \\ & + \frac{6a^2 f^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{(a^2+b^2)^{3/2}d^4} - \frac{6a^2 f^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{(a^2+b^2)^{3/2}d^4} + \frac{3af (fx+e)^2 \ln(1+e^{2dx+2c})}{b^2 d^2} \\ & + \frac{3a^2 f (fx+e)^2 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{(a^2+b^2)^{3/2}d^2} - \frac{3a^2 f (fx+e)^2 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{(a^2+b^2)^{3/2}d^2} - \frac{6a^2 f^2 (fx+e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a - \sqrt{a^2+b^2}}\right)}{(a^2+b^2)^{3/2}d^3} \\ & + \frac{6a^2 f^2 (fx+e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a + \sqrt{a^2+b^2}}\right)}{(a^2+b^2)^{3/2}d^3} + \frac{3af^2 (fx+e) \operatorname{polylog}(2, -e^{2dx+2c})}{b^2 d^3} + \frac{6If^3 \operatorname{polylog}(3, -Ie^{dx+c})}{bd^4} + \frac{3a^3 f^3 \operatorname{polylog}(3, -e^{2dx+2c})}{2b^2(a^2+b^2)d^4} \\ & + \frac{a^2 (fx+e)^3 \operatorname{sech}(dx+c)}{b(a^2+b^2)d} + \frac{a^3 (fx+e)^3 \tanh(dx+c)}{b^2(a^2+b^2)d} - \frac{6If^2 (fx+e) \operatorname{polylog}(2, -Ie^{dx+c})}{bd^3} - \frac{(fx+e)^3 \operatorname{sech}(dx+c)}{bd} - \frac{a (fx+e)^3}{b^2 d} \end{aligned}$$

$$\begin{aligned}
& + \frac{6 I a^2 f^3 \operatorname{polylog}(3, I e^{dx+c})}{b (a^2 + b^2) d^4} - \frac{6 I a^2 f^2 (fx + e) \operatorname{polylog}(2, I e^{dx+c})}{b (a^2 + b^2) d^3} - \frac{a (fx + e)^3 \tanh(dx + c)}{b^2 d} - \frac{6 I f^3 \operatorname{polylog}(3, I e^{dx+c})}{b d^4} + \frac{a^3 (fx + e)^3}{b^2 (a^2 + b^2) d} \\
& + \frac{6 f (fx + e)^2 \arctan(e^{dx+c})}{b d^2} - \frac{3 a f^3 \operatorname{polylog}(3, -e^{2dx+2c})}{2 b^2 d^4}
\end{aligned}$$

Result(type 8, 489 leaves):

$$\begin{aligned}
& \frac{2 (f^3 x^3 + 3 e f^2 x^2 + 3 e^2 f x + e^3) (-e^{dx+c} b + a)}{d (a^2 + b^2) ((e^{dx+c})^2 + 1)} + \int \frac{1}{((e^{dx+c})^2 + 1) (a^2 + b^2) (b (e^{dx+c})^2 + 2 a e^{dx+c} - b) d} (2 (a^2 d f^3 x^3 (e^{dx+c})^3 \\
& + 3 a^2 d e f^2 x^2 (e^{dx+c})^3 + 3 a^2 d e^2 f x (e^{dx+c})^3 + a^2 d f^3 x^3 e^{dx+c} + 3 b^2 f^3 x^2 (e^{dx+c})^3 + a^2 d e^3 (e^{dx+c})^3 + 3 a^2 d e f^2 x^2 e^{dx+c} + 3 a b f^3 x^2 (e^{dx+c})^2 \\
& + 6 b^2 e f^2 x (e^{dx+c})^3 + 3 a^2 d e^2 f x e^{dx+c} - 6 a^2 f^3 x^2 e^{dx+c} + 6 a b e f^2 x (e^{dx+c})^2 + 3 b^2 e^2 f (e^{dx+c})^3 - 3 b^2 f^3 x^2 e^{dx+c} + a^2 d e^3 e^{dx+c} - 12 a^2 e f^2 x e^{dx+c} \\
& + 3 a b e^2 f (e^{dx+c})^2 + 3 a b f^3 x^2 - 6 b^2 e f^2 x e^{dx+c} - 6 a^2 e^2 f e^{dx+c} + 6 a b e f^2 x - 3 b^2 e^2 f e^{dx+c} + 3 a b e^2 f) dx
\end{aligned}$$

Problem 104: Unable to integrate problem.

$$\int \frac{(fx + e)^2 \tanh(dx + c)^2}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 728 leaves, 37 steps):

$$\begin{aligned}
& - \frac{a (fx + e)^2}{b^2 d} + \frac{a^3 (fx + e)^2}{b^2 (a^2 + b^2) d} + \frac{4 f (fx + e) \arctan(e^{dx+c})}{b d^2} - \frac{4 a^2 f (fx + e) \arctan(e^{dx+c})}{b (a^2 + b^2) d^2} + \frac{2 a f (fx + e) \ln(1 + e^{2dx+2c})}{b^2 d^2} \\
& - \frac{2 a^3 f (fx + e) \ln(1 + e^{2dx+2c})}{b^2 (a^2 + b^2) d^2} + \frac{a^2 (fx + e)^2 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d} - \frac{a^2 (fx + e)^2 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d} - \frac{2 I a^2 f^2 \operatorname{polylog}(2, I e^{dx+c})}{b (a^2 + b^2) d^3} \\
& - \frac{2 I f^2 \operatorname{polylog}(2, -I e^{dx+c})}{b d^3} + \frac{2 I a^2 f^2 \operatorname{polylog}(2, -I e^{dx+c})}{b (a^2 + b^2) d^3} + \frac{2 I f^2 \operatorname{polylog}(2, I e^{dx+c})}{b d^3} + \frac{a f^2 \operatorname{polylog}(2, -e^{2dx+2c})}{b^2 d^3} - \frac{a^3 f^2 \operatorname{polylog}(2, -e^{2dx+2c})}{b^2 (a^2 + b^2) d^3} \\
& + \frac{2 a^2 f (fx + e) \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d^2} - \frac{2 a^2 f (fx + e) \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d^2} - \frac{2 a^2 f^2 \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d^3} \\
& + \frac{2 a^2 f^2 \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{3/2} d^3} - \frac{(fx + e)^2 \operatorname{sech}(dx + c)}{b d} + \frac{a^2 (fx + e)^2 \operatorname{sech}(dx + c)}{b (a^2 + b^2) d} - \frac{a (fx + e)^2 \tanh(dx + c)}{b^2 d} \\
& + \frac{a^3 (fx + e)^2 \tanh(dx + c)}{b^2 (a^2 + b^2) d}
\end{aligned}$$

Result(type 8, 338 leaves):

$$\frac{2 (x^2 f^2 + 2 e f x + e^2) (-e^{dx+c} b + a)}{d (a^2 + b^2) ((e^{dx+c})^2 + 1)} + \int \frac{1}{((e^{dx+c})^2 + 1) (a^2 + b^2) (b (e^{dx+c})^2 + 2 a e^{dx+c} - b) d} (2 ((e^{dx+c})^3 a^2 d f^2 x^2 + 2 (e^{dx+c})^3 a^2 d e f x$$

$$+ (e^{dx+c})^3 a^2 d e^2 + e^{dx+c} a^2 d f^2 x^2 + 2 (e^{dx+c})^3 b^2 f^2 x + 2 e^{dx+c} a^2 d e f x + 2 (e^{dx+c})^2 a b f^2 x + 2 (e^{dx+c})^3 b^2 e f + e^{dx+c} a^2 d e^2 - 4 e^{dx+c} a^2 f^2 x + 2 (e^{dx+c})^2 a b e f - 2 e^{dx+c} b^2 f^2 x - 4 e^{dx+c} a^2 e f + 2 a b f^2 x - 2 e^{dx+c} b^2 e f + 2 a b e f) dx$$

Problem 105: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \operatorname{sech}(dx + c) \tanh(dx + c)^2}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 701 leaves, 42 steps):

$$\begin{aligned} & -\frac{a (fx + e) \arctan(e^{dx+c})}{b^2 d} + \frac{2 a^3 (fx + e) \arctan(e^{dx+c})}{(a^2 + b^2)^2 d} + \frac{a^3 (fx + e) \arctan(e^{dx+c})}{b^2 (a^2 + b^2) d} - \frac{a^2 b (fx + e) \ln(1 + e^{2dx+2c})}{(a^2 + b^2)^2 d} \\ & + \frac{a^2 b (fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^2 d} + \frac{a^2 b (fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^2 d} - \frac{I a f \operatorname{polylog}(2, I e^{dx+c})}{2 b^2 d^2} + \frac{I a^3 f \operatorname{polylog}(2, I e^{dx+c})}{(a^2 + b^2)^2 d^2} \\ & + \frac{I a f \operatorname{polylog}(2, -I e^{dx+c})}{2 b^2 d^2} + \frac{I a^3 f \operatorname{polylog}(2, I e^{dx+c})}{2 b^2 (a^2 + b^2) d^2} - \frac{I a^3 f \operatorname{polylog}(2, -I e^{dx+c})}{(a^2 + b^2)^2 d^2} - \frac{I a^3 f \operatorname{polylog}(2, -I e^{dx+c})}{2 b^2 (a^2 + b^2) d^2} - \frac{a^2 b f \operatorname{polylog}(2, -e^{2dx+2c})}{2 (a^2 + b^2)^2 d^2} \\ & + \frac{a^2 b f \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^2 d^2} + \frac{a^2 b f \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^2 d^2} - \frac{a f \operatorname{sech}(dx + c)}{2 b^2 d^2} + \frac{a^3 f \operatorname{sech}(dx + c)}{2 b^2 (a^2 + b^2) d^2} - \frac{(fx + e) \operatorname{sech}(dx + c)^2}{2 b d} \\ & + \frac{a^2 (fx + e) \operatorname{sech}(dx + c)^2}{2 b (a^2 + b^2) d} + \frac{f \tanh(dx + c)}{2 b d^2} - \frac{a^2 f \tanh(dx + c)}{2 b (a^2 + b^2) d^2} - \frac{a (fx + e) \operatorname{sech}(dx + c) \tanh(dx + c)}{2 b^2 d} \\ & + \frac{a^3 (fx + e) \operatorname{sech}(dx + c) \tanh(dx + c)}{2 b^2 (a^2 + b^2) d} \end{aligned}$$

Result (type ?, 2067 leaves): Display of huge result suppressed!

Problem 107: Unable to integrate problem.

$$\int \frac{(fx + e)^2 \cosh(dx + c) \sinh(dx + c)^3}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 538 leaves, 22 steps):

$$\begin{aligned} & -\frac{a e f x}{2 b^2 d} - \frac{a f^2 x^2}{4 b^2 d} + \frac{a^3 (fx + e)^3}{3 b^4 f} - \frac{2 a^2 f (fx + e) \cosh(dx + c)}{b^3 d^2} + \frac{4 f (fx + e) \cosh(dx + c)}{9 b d^2} - \frac{a^3 (fx + e)^2 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^4 d} \\ & - \frac{a^3 (fx + e)^2 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^4 d} - \frac{2 a^3 f (fx + e) \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^4 d^2} - \frac{2 a^3 f (fx + e) \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^4 d^2} \end{aligned}$$



$$\begin{aligned}
& + \frac{2 a^3 f^2 \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^4 d^3} + \frac{2 a^3 f^2 \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^4 d^3} + \frac{2 a^2 f^2 \sinh(dx+c)}{b^3 d^3} - \frac{4 f^2 \sinh(dx+c)}{9 b d^3} \\
& + \frac{a^2 (fx+e)^2 \sinh(dx+c)}{b^3 d} + \frac{af(fx+e) \cosh(dx+c) \sinh(dx+c)}{2 b^2 d^2} - \frac{a f^2 \sinh(dx+c)^2}{4 b^2 d^3} - \frac{a (fx+e)^2 \sinh(dx+c)^2}{2 b^2 d} \\
& - \frac{2f(fx+e) \cosh(dx+c) \sinh(dx+c)^2}{9 b d^2} + \frac{2f^2 \sinh(dx+c)^3}{27 b d^3} + \frac{(fx+e)^2 \sinh(dx+c)^3}{3 b d}
\end{aligned}$$

Result(type 8, 574 leaves):

$$\begin{aligned}
& - \frac{a^3 \left(\frac{1}{3} x^3 f^2 + e f x^2 + e^2 x\right)}{b^4} + \frac{(9 d^2 f^2 x^2 + 18 d^2 e f x + 9 d^2 e^2 - 6 d f^2 x - 6 e f d + 2 f^2) (e^{dx+c})^3}{216 b d^3} \\
& - \frac{a (2 d^2 f^2 x^2 + 4 d^2 e f x + 2 d^2 e^2 - 2 d f^2 x - 2 e f d + f^2) (e^{dx+c})^2}{16 b^2 d^3} \\
& + \frac{(4 a^2 d^2 f^2 x^2 - b^2 d^2 f^2 x^2 + 8 a^2 d^2 e f x - 2 b^2 d^2 e f x + 4 a^2 d^2 e^2 - 8 a^2 d f^2 x - b^2 d^2 e^2 + 2 b^2 d f^2 x - 8 a^2 d e f + 2 e f d b^2 + 8 a^2 f^2 - 2 b^2 f^2) e^{dx+c}}{8 b^3 d^3} \\
& - \frac{(4 a^2 - b^2) (d^2 f^2 x^2 + 2 d^2 e f x + d^2 e^2 + 2 d f^2 x + 2 e f d + 2 f^2)}{8 b^3 d^3 e^{dx+c}} - \frac{a (2 d^2 f^2 x^2 + 4 d^2 e f x + 2 d^2 e^2 + 2 d f^2 x + 2 e f d + f^2)}{16 b^2 d^3 (e^{dx+c})^2} \\
& - \frac{9 d^2 f^2 x^2 + 18 d^2 e f x + 9 d^2 e^2 + 6 d f^2 x + 6 e f d + 2 f^2}{216 b d^3 (e^{dx+c})^3} + \int \frac{2 a^3 (a f^2 x^2 e^{dx+c} + 2 a e f x e^{dx+c} - b f^2 x^2 + a e^2 e^{dx+c} - 2 b e f x - b e^2)}{(b (e^{dx+c})^2 + 2 a e^{dx+c} - b) b^4} dx
\end{aligned}$$

Problem 108: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx+e) \cosh(dx+c)^3 \sinh(dx+c)^3}{a + b \sinh(dx+c)} dx$$

Optimal(type 4, 593 leaves, 31 steps):

$$\begin{aligned}
& - \frac{a^3 f x}{4 b^4 d} + \frac{3 a f x}{32 b^2 d} + \frac{a^3 (a^2 + b^2) (fx+e)^2}{2 b^6 f} - \frac{a^4 f \cosh(dx+c)}{b^5 d^2} - \frac{2 a^2 f \cosh(dx+c)}{3 b^3 d^2} + \frac{f \cosh(dx+c)}{8 b d^2} - \frac{a^2 f \cosh(dx+c)^3}{9 b^3 d^2} \\
& - \frac{a (fx+e) \cosh(dx+c)^4}{4 b^2 d} - \frac{f \cosh(3 dx+3 c)}{144 b d^2} - \frac{f \cosh(5 dx+5 c)}{400 b d^2} - \frac{a^3 (a^2 + b^2) (fx+e) \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^6 d} \\
& - \frac{a^3 (a^2 + b^2) (fx+e) \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^6 d} - \frac{a^3 (a^2 + b^2) f \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^6 d^2} - \frac{a^3 (a^2 + b^2) f \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^6 d^2} \\
& + \frac{a^4 (fx+e) \sinh(dx+c)}{b^5 d} + \frac{2 a^2 (fx+e) \sinh(dx+c)}{3 b^3 d} - \frac{(fx+e) \sinh(dx+c)}{8 b d} + \frac{a^3 f \cosh(dx+c) \sinh(dx+c)}{4 b^4 d^2}
\end{aligned}$$

$$\begin{aligned}
& + \frac{3 a f \cosh(dx+c) \sinh(dx+c)}{32 b^2 d^2} + \frac{a^2 (fx+e) \cosh(dx+c)^2 \sinh(dx+c)}{3 b^3 d} + \frac{a f \cosh(dx+c)^3 \sinh(dx+c)}{16 b^2 d^2} - \frac{a^3 (fx+e) \sinh(dx+c)^2}{2 b^4 d} \\
& + \frac{(fx+e) \sinh(3 dx+3 c)}{48 b d} + \frac{(fx+e) \sinh(5 dx+5 c)}{80 b d}
\end{aligned}$$

Result(type 4, 1362 leaves):

$$\begin{aligned}
& - \frac{a^3 e \ln(b e^{2 dx+2 c} + 2 a e^{dx+c} - b)}{b^4 d} - \frac{a^3 f \operatorname{dilog}\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right)}{b^4 d^2} - \frac{a^3 f \operatorname{dilog}\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right)}{b^4 d^2} + \frac{2 a^3 e \ln(e^{dx+c})}{b^4 d} + \frac{a^3 f c^2}{b^4 d^2} \\
& - \frac{a (2 a^2 + b^2) (2 d f x + 2 d e + f) e^{-2 dx-2 c}}{32 b^4 d^2} + \frac{a^3 f x^2}{2 b^4} - \frac{a^3 e x}{b^4} + \frac{a^5 f c^2}{b^6 d^2} + \frac{2 a^5 e \ln(e^{dx+c})}{b^6 d} - \frac{a^5 e \ln(b e^{2 dx+2 c} + 2 a e^{dx+c} - b)}{b^6 d} \\
& - \frac{a^5 f \operatorname{dilog}\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right)}{b^6 d^2} - \frac{a^5 f \operatorname{dilog}\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right)}{b^6 d^2} + \frac{2 a^5 f c x}{b^6 d} - \frac{a^5 f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) x}{b^6 d} \\
& - \frac{a^5 f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) c}{b^6 d^2} - \frac{a^5 f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) x}{b^6 d} - \frac{a^5 f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) c}{b^6 d^2} - \frac{2 a^5 f c \ln(e^{dx+c})}{b^6 d^2} \\
& + \frac{a^5 f c \ln(b e^{2 dx+2 c} + 2 a e^{dx+c} - b)}{b^6 d^2} + \frac{a^5 f x^2}{2 b^6} - \frac{a^5 e x}{b^6} \\
& + \frac{(8 a^4 d f x + 6 a^2 b^2 d f x - b^4 d f x + 8 a^4 d e + 6 a^2 b^2 d e - b^4 d e - 8 a^4 f - 6 a^2 b^2 f + b^4 f) e^{dx+c}}{16 b^5 d^2} + \frac{(5 d f x + 5 d e - f) e^{5 dx+5 c}}{800 b d^2} \\
& + \frac{(12 a^2 d f x + 3 b^2 d f x + 12 a^2 d e + 3 b^2 d e - 4 a^2 f - b^2 f) e^{3 dx+3 c}}{288 b^3 d^2} - \frac{(5 d f x + 5 d e + f) e^{-5 dx-5 c}}{800 b d^2} - \frac{a (4 d f x + 4 d e - f) e^{4 dx+4 c}}{256 b^2 d^2} \\
& - \frac{a (4 a^2 d f x + 2 b^2 d f x + 4 a^2 d e + 2 b^2 d e - 2 a^2 f - b^2 f) e^{2 dx+2 c}}{32 b^4 d^2} - \frac{(8 a^4 + 6 b^2 a^2 - b^4) (d f x + d e + f) e^{-dx-c}}{16 b^5 d^2} \\
& - \frac{(4 a^2 + b^2) (3 d f x + 3 d e + f) e^{-3 dx-3 c}}{288 b^3 d^2} - \frac{a (4 d f x + 4 d e + f) e^{-4 dx-4 c}}{256 b^2 d^2} + \frac{2 a^3 f c x}{b^4 d} - \frac{a^3 f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) x}{b^4 d} \\
& - \frac{a^3 f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) c}{b^4 d^2} - \frac{a^3 f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) x}{b^4 d} - \frac{a^3 f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) c}{b^4 d^2} - \frac{2 a^3 f c \ln(e^{dx+c})}{b^4 d^2} \\
& + \frac{a^3 f c \ln(b e^{2 dx+2 c} + 2 a e^{dx+c} - b)}{b^4 d^2}
\end{aligned}$$

Problem 109: Unable to integrate problem.

$$\int \frac{(fx + e)^2 \sinh(dx + c)^2 \tanh(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 1004 leaves, 50 steps):

$$\begin{aligned} & \frac{2Ia^4 f(fx + e) \operatorname{polylog}(2, -Ie^{dx+c})}{b^3 (a^2 + b^2) d^2} - \frac{2a^3 f(fx + e) \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^2 (a^2 + b^2) d^2} - \frac{2a^3 f(fx + e) \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^2 (a^2 + b^2) d^2} \\ & + \frac{2If(fx + e) \operatorname{polylog}(2, -Ie^{dx+c})}{bd^2} + \frac{a^3 f(fx + e) \operatorname{polylog}(2, -e^{2dx+2c})}{b^2 (a^2 + b^2) d^2} + \frac{2Ia^2 f^2 \operatorname{polylog}(3, -Ie^{dx+c})}{b^3 d^3} - \frac{2Ia^2 f(fx + e) \operatorname{polylog}(2, -Ie^{dx+c})}{b^3 d^2} \\ & - \frac{2Ia^4 f^2 \operatorname{polylog}(3, -Ie^{dx+c})}{b^3 (a^2 + b^2) d^3} - \frac{a(fx + e)^2 \ln(1 + e^{2dx+2c})}{b^2 d} + \frac{a^3 (fx + e)^2 \ln(1 + e^{2dx+2c})}{b^2 (a^2 + b^2) d} - \frac{a^3 (fx + e)^2 \ln\left(1 + \frac{be^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^2 (a^2 + b^2) d} \\ & - \frac{a^3 (fx + e)^2 \ln\left(1 + \frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^2 (a^2 + b^2) d} + \frac{2a^3 f^2 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{b^2 (a^2 + b^2) d^3} + \frac{2a^3 f^2 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{b^2 (a^2 + b^2) d^3} - \frac{2Ia^2 f^2 \operatorname{polylog}(3, Ie^{dx+c})}{b^3 d^3} \\ & - \frac{2a^4 (fx + e)^2 \arctan(e^{dx+c})}{b^3 (a^2 + b^2) d} - \frac{af(fx + e) \operatorname{polylog}(2, -e^{2dx+2c})}{b^2 d^2} + \frac{2If^2 \operatorname{polylog}(3, Ie^{dx+c})}{bd^3} - \frac{a^3 f^2 \operatorname{polylog}(3, -e^{2dx+2c})}{2b^2 (a^2 + b^2) d^3} \\ & - \frac{2If(fx + e) \operatorname{polylog}(2, Ie^{dx+c})}{bd^2} + \frac{2f^2 \sinh(dx + c)}{bd^3} + \frac{(fx + e)^2 \sinh(dx + c)}{bd} - \frac{2(fx + e)^2 \arctan(e^{dx+c})}{bd} + \frac{a(fx + e)^3}{3b^2 f} \\ & + \frac{2Ia^2 f(fx + e) \operatorname{polylog}(2, Ie^{dx+c})}{b^3 d^2} + \frac{2Ia^4 f^2 \operatorname{polylog}(3, Ie^{dx+c})}{b^3 (a^2 + b^2) d^3} - \frac{2Ia^4 f(fx + e) \operatorname{polylog}(2, Ie^{dx+c})}{b^3 (a^2 + b^2) d^2} + \frac{2a^2 (fx + e)^2 \arctan(e^{dx+c})}{b^3 d} \\ & + \frac{af^2 \operatorname{polylog}(3, -e^{2dx+2c})}{2b^2 d^3} - \frac{2If^2 \operatorname{polylog}(3, -Ie^{dx+c})}{bd^3} - \frac{2f(fx + e) \cosh(dx + c)}{bd^2} \end{aligned}$$

Result (type 8, 445 leaves):

$$\begin{aligned} & -\frac{a\left(\frac{1}{3}x^3 f^2 + efx^2 + e^2 x\right)}{b^2} + \frac{(d^2 f^2 x^2 + 2d^2 efx + d^2 e^2 - 2df^2 x - 2efd + 2f^2) e^{dx+c}}{2d^3 b} - \frac{d^2 f^2 x^2 + 2d^2 efx + d^2 e^2 + 2df^2 x + 2efd + 2f^2}{2d^3 b e^{dx+c}} + \\ & \int \frac{1}{b^2 (b (e^{dx+c})^4 + 2a (e^{dx+c})^3 + 2a e^{dx+c} - b)} \left( 2(a^2 f^2 x^2 (e^{dx+c})^3 - b^2 f^2 x^2 (e^{dx+c})^3 + 2a^2 efx (e^{dx+c})^3 - abf^2 x^2 (e^{dx+c})^2 - 2b^2 efx (e^{dx+c})^3 \right. \\ & \left. + a^2 e^2 (e^{dx+c})^3 + a^2 f^2 x^2 e^{dx+c} - 2abefx (e^{dx+c})^2 - b^2 e^2 (e^{dx+c})^3 + b^2 f^2 x^2 e^{dx+c} + 2a^2 efx e^{dx+c} - abe^2 (e^{dx+c})^2 - abf^2 x^2 + 2b^2 efx e^{dx+c} \right. \\ & \left. + a^2 e^2 e^{dx+c} - 2abefx + b^2 e^2 e^{dx+c} - abe^2 \right) dx \end{aligned}$$

Problem 111: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \tanh(dx + c)^3}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 820 leaves, 55 steps):

$$\begin{aligned}
& -\frac{I a^4 f \text{polylog}(2, I e^{dx+c})}{b (a^2 + b^2)^2 d^2} - \frac{I a^4 f \text{polylog}(2, I e^{dx+c})}{2 b^3 (a^2 + b^2) d^2} + \frac{I a^4 f \text{polylog}(2, -I e^{dx+c})}{b (a^2 + b^2)^2 d^2} + \frac{I a^2 f \text{polylog}(2, I e^{dx+c})}{2 b^3 d^2} - \frac{a^4 (fx + e) \operatorname{sech}(dx + c) \tanh(dx + c)}{2 b^3 (a^2 + b^2) d} \\
& + \frac{a^3 (fx + e) \ln(1 + e^{2dx+2c})}{(a^2 + b^2)^2 d} - \frac{a^3 (fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^2 d} - \frac{a^3 (fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^2 d} - \frac{a^3 f \text{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^2 d^2} \\
& - \frac{a^3 f \text{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^2 d^2} - \frac{2 a^4 (fx + e) \arctan(e^{dx+c})}{b (a^2 + b^2)^2 d} - \frac{a^4 (fx + e) \arctan(e^{dx+c})}{b^3 (a^2 + b^2) d} + \frac{I f \text{polylog}(2, I e^{dx+c})}{2 b d^2} - \frac{a^4 f \operatorname{sech}(dx + c)}{2 b^3 (a^2 + b^2) d^2} \\
& - \frac{a^3 (fx + e) \operatorname{sech}(dx + c)^2}{2 b^2 (a^2 + b^2) d} + \frac{a^3 f \tanh(dx + c)}{2 b^2 (a^2 + b^2) d^2} + \frac{a^2 (fx + e) \operatorname{sech}(dx + c) \tanh(dx + c)}{2 b^3 d} - \frac{I a^2 f \text{polylog}(2, -I e^{dx+c})}{2 b^3 d^2} + \frac{(fx + e) \arctan(e^{dx+c})}{b d} \\
& - \frac{f \operatorname{sech}(dx + c)}{2 b d^2} + \frac{I a^4 f \text{polylog}(2, -I e^{dx+c})}{2 b^3 (a^2 + b^2) d^2} + \frac{a^2 (fx + e) \arctan(e^{dx+c})}{b^3 d} + \frac{a^3 f \text{polylog}(2, -e^{2dx+2c})}{2 (a^2 + b^2)^2 d^2} + \frac{a^2 f \operatorname{sech}(dx + c)}{2 b^3 d^2} \\
& + \frac{a (fx + e) \operatorname{sech}(dx + c)^2}{2 b^2 d} - \frac{a f \tanh(dx + c)}{2 b^2 d^2} - \frac{(fx + e) \operatorname{sech}(dx + c) \tanh(dx + c)}{2 b d} - \frac{I f \text{polylog}(2, -I e^{dx+c})}{2 b d^2}
\end{aligned}$$

Result(type ?, 2283 leaves): Display of huge result suppressed!

Problem 112: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx + e) \operatorname{coth}(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 191 leaves, 12 steps):

$$\begin{aligned}
& \frac{(fx + e) \ln(1 - e^{2dx+2c})}{a d} - \frac{(fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a d} - \frac{(fx + e) \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a d} + \frac{f \text{polylog}(2, e^{2dx+2c})}{2 a d^2} \\
& - \frac{f \text{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a d^2} - \frac{f \text{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a d^2}
\end{aligned}$$

Result(type 4, 450 leaves):

$$\begin{aligned}
& -\frac{f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) x}{d a} - \frac{f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) c}{d^2 a} + \frac{\ln(1 + e^{dx+c}) f x}{a d} - \frac{f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) x}{d a} \\
& - \frac{f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) c}{d^2 a} - \frac{f \operatorname{dilog}(e^{dx+c})}{d^2 a} - \frac{f \operatorname{dilog}\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right)}{d^2 a} - \frac{f \operatorname{dilog}\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right)}{d^2 a}
\end{aligned}$$

$$\begin{aligned}
& + \frac{f \operatorname{dilog}(1 + e^{dx+c})}{a d^2} + \frac{e \ln(e^{dx+c} - 1)}{a d} - \frac{e \ln(b e^{2dx+2c} + 2 a e^{dx+c} - b)}{d a} + \frac{e \ln(1 + e^{dx+c})}{a d} - \frac{c f \ln(e^{dx+c} - 1)}{a d^2} \\
& + \frac{c f \ln(b e^{2dx+2c} + 2 a e^{dx+c} - b)}{d^2 a}
\end{aligned}$$

Problem 113: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \cosh(dx + c) \coth(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 589 leaves, 33 steps):

$$\begin{aligned}
& \frac{(fx + e)^4}{4 b f} - \frac{2 (fx + e)^3 \operatorname{arctanh}(e^{dx+c})}{a d} - \frac{3 f (fx + e)^2 \operatorname{polylog}(2, -e^{dx+c})}{a d^2} + \frac{3 f (fx + e)^2 \operatorname{polylog}(2, e^{dx+c})}{a d^2} + \frac{6 f^2 (fx + e) \operatorname{polylog}(3, -e^{dx+c})}{a d^3} \\
& - \frac{6 f^2 (fx + e) \operatorname{polylog}(3, e^{dx+c})}{a d^3} - \frac{6 f^3 \operatorname{polylog}(4, -e^{dx+c})}{a d^4} + \frac{6 f^3 \operatorname{polylog}(4, e^{dx+c})}{a d^4} - \frac{(fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{a b d} \\
& + \frac{(fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{a b d} - \frac{3 f (fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{a b d^2} \\
& + \frac{3 f (fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{a b d^2} + \frac{6 f^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{a b d^3} \\
& - \frac{6 f^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{a b d^3} - \frac{6 f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{a b d^4} + \frac{6 f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{a b d^4}
\end{aligned}$$

Result (type 8, 240 leaves):

$$\begin{aligned}
& \frac{\frac{1}{4} x^4 f^3 + e f^2 x^3 + \frac{3}{2} e^2 f x^2 + e^3 x}{b} + \int -\frac{1}{(b (e^{dx+c})^2 + 2 a e^{dx+c} - b) b ((e^{dx+c})^2 - 1)} (2 e^{dx+c} (a f^3 x^3 (e^{dx+c})^2 + 3 a e f^2 x^2 (e^{dx+c})^2 - 2 b f^3 x^3 e^{dx+c} \\
& + 3 a e^2 f x (e^{dx+c})^2 - a f^3 x^3 - 6 b e f^2 x^2 e^{dx+c} + a e^3 (e^{dx+c})^2 - 3 a e f^2 x^2 - 6 b e^2 f x e^{dx+c} - 3 a e^2 f x - 2 b e^3 e^{dx+c} - a e^3) dx
\end{aligned}$$

Problem 114: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \cosh(dx + c)^2 \coth(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 622 leaves, 34 steps):

$$\begin{aligned}
& -\frac{(fx+e)^4}{4af} + \frac{(a^2+b^2)(fx+e)^4}{4ab^2f} - \frac{6f^3 \cosh(dx+c)}{bd^4} - \frac{3f(fx+e)^2 \cosh(dx+c)}{bd^2} + \frac{(fx+e)^3 \ln(1-e^{2dx+2c})}{ad} \\
& - \frac{(a^2+b^2)(fx+e)^3 \ln\left(1 + \frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{ab^2d} - \frac{(a^2+b^2)(fx+e)^3 \ln\left(1 + \frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{ab^2d} + \frac{3f(fx+e)^2 \operatorname{polylog}(2, e^{2dx+2c})}{2ad^2} \\
& - \frac{3(a^2+b^2)f(fx+e)^2 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{ab^2d^2} - \frac{3(a^2+b^2)f(fx+e)^2 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{ab^2d^2} - \frac{3f^2(fx+e) \operatorname{polylog}(3, e^{2dx+2c})}{2ad^3} \\
& + \frac{6(a^2+b^2)f^2(fx+e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{ab^2d^3} + \frac{6(a^2+b^2)f^2(fx+e) \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{ab^2d^3} + \frac{3f^3 \operatorname{polylog}(4, e^{2dx+2c})}{4ad^4} \\
& - \frac{6(a^2+b^2)f^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{ab^2d^4} - \frac{6(a^2+b^2)f^3 \operatorname{polylog}\left(4, -\frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{ab^2d^4} + \frac{6f^2(fx+e) \sinh(dx+c)}{bd^3} \\
& + \frac{(fx+e)^3 \sinh(dx+c)}{bd}
\end{aligned}$$

Result(type 8, 673 leaves):

$$\begin{aligned}
& -\frac{a\left(\frac{1}{4}x^4f^3 + e^2fx^3 + \frac{3}{2}e^2fx^2 + e^3x\right)}{b^2} + \frac{(f^3x^3d^3 + 3d^3ef^2x^2 + 3d^3e^2fx - 3d^2f^3x^2 + e^3d^3 - 6d^2ef^2x - 3d^2e^2f + 6df^3x + 6def^2 - 6f^3)e^{dx+c}}{2bd^4} \\
& - \frac{f^3x^3d^3 + 3d^3ef^2x^2 + 3d^3e^2fx + 3d^2f^3x^2 + e^3d^3 + 6d^2ef^2x + 3d^2e^2f + 6df^3x + 6def^2 + 6f^3}{2bd^4e^{dx+c}} + \\
& \int \frac{1}{b^2(b(e^{dx+c})^4 + 2a(e^{dx+c})^3 - 2b(e^{dx+c})^2 - 2ae^{dx+c} + b)} \left( 2(a^2f^3x^3(e^{dx+c})^3 + b^2f^3x^3(e^{dx+c})^3 + 3a^2ef^2x^2(e^{dx+c})^3 - abf^3x^3(e^{dx+c})^2 \right. \\
& + 3b^2ef^2x^2(e^{dx+c})^3 + 3a^2e^2fx(e^{dx+c})^3 - a^2f^3x^3e^{dx+c} - 3abef^2x^2(e^{dx+c})^2 + 3b^2e^2fx(e^{dx+c})^3 + b^2f^3x^3e^{dx+c} + a^2e^3(e^{dx+c})^3 \\
& - 3a^2ef^2x^2e^{dx+c} - 3abef^2fx(e^{dx+c})^2 + abf^3x^3 + b^2e^3(e^{dx+c})^3 + 3b^2ef^2x^2e^{dx+c} - 3a^2e^2fxe^{dx+c} - abe^3(e^{dx+c})^2 + 3abef^2x^2 \\
& \left. + 3b^2e^2fxe^{dx+c} - a^2e^3e^{dx+c} + 3abef^2fx + b^2e^3e^{dx+c} + be^3a \right) dx
\end{aligned}$$

Problem 115: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx+e) \cosh(dx+c)^2 \coth(dx+c)}{a+b \sinh(dx+c)} dx$$

Optimal(type 4, 304 leaves, 22 steps):

$$\begin{aligned}
& -\frac{(fx+e)^2}{2af} + \frac{(a^2+b^2)(fx+e)^2}{2ab^2f} - \frac{f \cosh(dx+c)}{bd^2} + \frac{(fx+e) \ln(1-e^{2dx+2c})}{ad} - \frac{(a^2+b^2)(fx+e) \ln\left(1 + \frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{ab^2d} \\
& - \frac{(a^2+b^2)(fx+e) \ln\left(1 + \frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{ab^2d} + \frac{f \operatorname{polylog}(2, e^{2dx+2c})}{2ad^2} - \frac{(a^2+b^2) f \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{ab^2d^2} \\
& - \frac{(a^2+b^2) f \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{ab^2d^2} + \frac{(fx+e) \sinh(dx+c)}{bd}
\end{aligned}$$

Result (type 4, 931 leaves):

$$\begin{aligned}
& -\frac{ae \ln(b e^{2dx+2c} + 2a e^{dx+c} - b)}{b^2 d} - \frac{a f \operatorname{dilog}\left(\frac{e^{dx+c} b + \sqrt{a^2+b^2} + a}{a + \sqrt{a^2+b^2}}\right)}{b^2 d^2} - \frac{a f \operatorname{dilog}\left(\frac{-e^{dx+c} b + \sqrt{a^2+b^2} - a}{-a + \sqrt{a^2+b^2}}\right)}{b^2 d^2} + \frac{a f c^2}{b^2 d^2} + \frac{2 a e \ln(e^{dx+c})}{b^2 d} \\
& + \frac{c f \ln(b e^{2dx+2c} + 2a e^{dx+c} - b)}{d^2 a} - \frac{f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2+b^2} + a}{a + \sqrt{a^2+b^2}}\right) x}{da} - \frac{f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2+b^2} + a}{a + \sqrt{a^2+b^2}}\right) c}{d^2 a} - \frac{f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2+b^2} - a}{-a + \sqrt{a^2+b^2}}\right) x}{da} \\
& - \frac{f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2+b^2} - a}{-a + \sqrt{a^2+b^2}}\right) c}{d^2 a} + \frac{(dfx+de-f) e^{dx+c}}{2bd^2} - \frac{(dfx+de+f) e^{-dx-c}}{2bd^2} + \frac{afx^2}{2b^2} - \frac{aex}{b^2} + \frac{2afcx}{b^2 d} - \frac{2afc \ln(e^{dx+c})}{b^2 d^2} \\
& + \frac{afc \ln(b e^{2dx+2c} + 2a e^{dx+c} - b)}{b^2 d^2} - \frac{a f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2+b^2} - a}{-a + \sqrt{a^2+b^2}}\right) x}{b^2 d} - \frac{a f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2+b^2} - a}{-a + \sqrt{a^2+b^2}}\right) c}{b^2 d^2} \\
& - \frac{a f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2+b^2} + a}{a + \sqrt{a^2+b^2}}\right) x}{b^2 d} - \frac{a f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2+b^2} + a}{a + \sqrt{a^2+b^2}}\right) c}{b^2 d^2} + \frac{e \ln(e^{dx+c} - 1)}{ad} + \frac{e \ln(1 + e^{dx+c})}{ad} + \frac{\ln(1 + e^{dx+c}) fx}{ad} \\
& - \frac{c f \ln(e^{dx+c} - 1)}{ad^2} - \frac{f \operatorname{dilog}(e^{dx+c})}{ad^2} + \frac{f \operatorname{dilog}(1 + e^{dx+c})}{ad^2} - \frac{f \operatorname{dilog}\left(\frac{-e^{dx+c} b + \sqrt{a^2+b^2} - a}{-a + \sqrt{a^2+b^2}}\right)}{d^2 a} - \frac{f \operatorname{dilog}\left(\frac{e^{dx+c} b + \sqrt{a^2+b^2} + a}{a + \sqrt{a^2+b^2}}\right)}{d^2 a} \\
& - \frac{e \ln(b e^{2dx+2c} + 2a e^{dx+c} - b)}{da}
\end{aligned}$$

Problem 117: Unable to integrate problem.

$$\int \frac{(fx+e)^2 \operatorname{csch}(dx+c) \operatorname{sech}(dx+c)}{a+b \sinh(dx+c)} dx$$

Optimal (type 4, 692 leaves, 33 steps):

$$\begin{aligned} & -\frac{2b(fx+e)^2 \arctan(e^{dx+c})}{(a^2+b^2)d} - \frac{2(fx+e)^2 \operatorname{arctanh}(e^{2dx+2c})}{ad} + \frac{b^2(fx+e)^2 \ln(1+e^{2dx+2c})}{a(a^2+b^2)d} - \frac{b^2(fx+e)^2 \ln\left(1 + \frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{a(a^2+b^2)d} \\ & - \frac{b^2(fx+e)^2 \ln\left(1 + \frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{a(a^2+b^2)d} + \frac{2Ibf^2 \operatorname{polylog}(3, Ie^{dx+c})}{(a^2+b^2)d^3} - \frac{2Ibf(fx+e) \operatorname{polylog}(2, Ie^{dx+c})}{(a^2+b^2)d^2} + \frac{b^2f(fx+e) \operatorname{polylog}(2, -e^{2dx+2c})}{a(a^2+b^2)d^2} \\ & - \frac{f(fx+e) \operatorname{polylog}(2, -e^{2dx+2c})}{ad^2} + \frac{f(fx+e) \operatorname{polylog}(2, e^{2dx+2c})}{ad^2} - \frac{2b^2f(fx+e) \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{a(a^2+b^2)d^2} \\ & - \frac{2b^2f(fx+e) \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{a(a^2+b^2)d^2} - \frac{2Ibf^2 \operatorname{polylog}(3, -Ie^{dx+c})}{(a^2+b^2)d^3} + \frac{2Ibf(fx+e) \operatorname{polylog}(2, -Ie^{dx+c})}{(a^2+b^2)d^2} - \frac{b^2f^2 \operatorname{polylog}(3, -e^{2dx+2c})}{2a(a^2+b^2)d^3} \\ & + \frac{f^2 \operatorname{polylog}(3, -e^{2dx+2c})}{2ad^3} - \frac{f^2 \operatorname{polylog}(3, e^{2dx+2c})}{2ad^3} + \frac{2b^2f^2 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{a(a^2+b^2)d^3} + \frac{2b^2f^2 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{a(a^2+b^2)d^3} \end{aligned}$$

Result (type 8, 34 leaves):

$$\int \frac{(fx+e)^2 \operatorname{csch}(dx+c) \operatorname{sech}(dx+c)}{a+b \sinh(dx+c)} dx$$

Problem 118: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx+e) \operatorname{csch}(dx+c) \operatorname{sech}(dx+c)}{a+b \sinh(dx+c)} dx$$

Optimal (type 4, 411 leaves, 26 steps):

$$\begin{aligned} & -\frac{2b(fx+e) \arctan(e^{dx+c})}{(a^2+b^2)d} - \frac{2(fx+e) \operatorname{arctanh}(e^{2dx+2c})}{ad} + \frac{b^2(fx+e) \ln(1+e^{2dx+2c})}{a(a^2+b^2)d} - \frac{b^2(fx+e) \ln\left(1 + \frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{a(a^2+b^2)d} \\ & - \frac{b^2(fx+e) \ln\left(1 + \frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{a(a^2+b^2)d} + \frac{Ibf \operatorname{polylog}(2, -Ie^{dx+c})}{(a^2+b^2)d^2} - \frac{Ibf \operatorname{polylog}(2, Ie^{dx+c})}{(a^2+b^2)d^2} + \frac{b^2f \operatorname{polylog}(2, -e^{2dx+2c})}{2a(a^2+b^2)d^2} \end{aligned}$$



$$-\frac{f \operatorname{polylog}(2, -e^{2dx+2c})}{2ad^2} + \frac{f \operatorname{polylog}(2, e^{2dx+2c})}{2ad^2} - \frac{b^2 f \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a-\sqrt{a^2+b^2}}\right)}{a(a^2+b^2)d^2} - \frac{b^2 f \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a+\sqrt{a^2+b^2}}\right)}{a(a^2+b^2)d^2}$$

Result (type 4, 1064 leaves):

$$\begin{aligned} & -\frac{fb^2 \ln\left(\frac{e^{dx+c}b + \sqrt{a^2+b^2} + a}{a + \sqrt{a^2+b^2}}\right)}{d(a^2+b^2)a} - \frac{fb^2 \ln\left(\frac{e^{dx+c}b + \sqrt{a^2+b^2} + a}{a + \sqrt{a^2+b^2}}\right)}{d^2(a^2+b^2)a} + \frac{cfb^2 \ln(b e^{2dx+2c} + 2a e^{dx+c} - b)}{d^2(a^2+b^2)a} \\ & -\frac{fb^2 \ln\left(\frac{-e^{dx+c}b + \sqrt{a^2+b^2} - a}{-a + \sqrt{a^2+b^2}}\right)}{d(a^2+b^2)a} - \frac{fb^2 \ln\left(\frac{-e^{dx+c}b + \sqrt{a^2+b^2} - a}{-a + \sqrt{a^2+b^2}}\right)}{d^2(a^2+b^2)a} + \frac{4I f \ln(1 + I e^{dx+c}) b x}{d(4a^2+4b^2)} + \frac{4I f \ln(1 + I e^{dx+c}) b c}{d^2(4a^2+4b^2)} \\ & -\frac{4I f \ln(1 - I e^{dx+c}) b x}{d(4a^2+4b^2)} - \frac{4I f \ln(1 - I e^{dx+c}) b c}{d^2(4a^2+4b^2)} + \frac{e \ln(e^{dx+c} - 1)}{ad} + \frac{e \ln(1 + e^{dx+c})}{ad} + \frac{\ln(1 + e^{dx+c}) f x}{ad} - \frac{c f \ln(e^{dx+c} - 1)}{ad^2} \\ & -\frac{f \operatorname{dilog}(e^{dx+c})}{ad^2} + \frac{f \operatorname{dilog}(1 + e^{dx+c})}{ad^2} - \frac{4f \ln(1 + I e^{dx+c}) a x}{d(4a^2+4b^2)} - \frac{4f \ln(1 + I e^{dx+c}) a c}{d^2(4a^2+4b^2)} - \frac{4f \ln(1 - I e^{dx+c}) a x}{d(4a^2+4b^2)} - \frac{4f \ln(1 - I e^{dx+c}) a c}{d^2(4a^2+4b^2)} \\ & + \frac{4cfa \ln(1 + e^{2dx+2c})}{d^2(4a^2+4b^2)} - \frac{fb^2 \operatorname{dilog}\left(\frac{-e^{dx+c}b + \sqrt{a^2+b^2} - a}{-a + \sqrt{a^2+b^2}}\right)}{d^2(a^2+b^2)a} - \frac{fb^2 \operatorname{dilog}\left(\frac{e^{dx+c}b + \sqrt{a^2+b^2} + a}{a + \sqrt{a^2+b^2}}\right)}{d^2(a^2+b^2)a} + \frac{8cfb \arctan(e^{dx+c})}{d^2(4a^2+4b^2)} \\ & -\frac{eb^2 \ln(b e^{2dx+2c} + 2a e^{dx+c} - b)}{d(a^2+b^2)a} + \frac{4I f \operatorname{dilog}(1 + I e^{dx+c}) b}{d^2(4a^2+4b^2)} - \frac{4I f \operatorname{dilog}(1 - I e^{dx+c}) b}{d^2(4a^2+4b^2)} - \frac{4f \operatorname{dilog}(1 - I e^{dx+c}) a}{d^2(4a^2+4b^2)} - \frac{4f \operatorname{dilog}(1 + I e^{dx+c}) a}{d^2(4a^2+4b^2)} \\ & -\frac{4ea \ln(1 + e^{2dx+2c})}{d(4a^2+4b^2)} - \frac{8eb \arctan(e^{dx+c})}{d(4a^2+4b^2)} \end{aligned}$$

Problem 121: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(dx+c) \operatorname{sech}(dx+c)^3}{a+b \sinh(dx+c)} dx$$

Optimal (type 3, 156 leaves, 9 steps):

$$\begin{aligned} & -\frac{b^3 \arctan(\sinh(dx+c))}{(a^2+b^2)^2 d} - \frac{b \arctan(\sinh(dx+c))}{2(a^2+b^2)d} - \frac{a(a^2+2b^2) \ln(\cosh(dx+c))}{(a^2+b^2)^2 d} + \frac{\ln(\sinh(dx+c))}{ad} - \frac{b^4 \ln(a+b \sinh(dx+c))}{a(a^2+b^2)^2 d} \\ & + \frac{\operatorname{sech}(dx+c)^2 (a-b \sinh(dx+c))}{2(a^2+b^2)d} \end{aligned}$$

Result (type 3, 529 leaves):

$$\begin{aligned}
& \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 a^2 b}{d(a^4 + 2b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 b^3}{d(a^4 + 2b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} - \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a^3}{d(a^4 + 2b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} \\
& - \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a b^2}{d(a^4 + 2b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a^2 b}{d(a^4 + 2b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} \\
& - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^3}{d(a^4 + 2b^2 a^2 + b^4) \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right) a^3}{d(a^4 + 2b^2 a^2 + b^4)} - \frac{2 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right) b^2 a}{d(a^4 + 2b^2 a^2 + b^4)} \\
& - \frac{\arctan\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right) a^2 b}{d(a^4 + 2b^2 a^2 + b^4)} - \frac{3 \arctan\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right) b^3}{d(a^4 + 2b^2 a^2 + b^4)} + \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)}{d a} \\
& - \frac{b^4 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b - a\right)}{d a (a^4 + 2b^2 a^2 + b^4)}
\end{aligned}$$

Problem 124: Unable to integrate problem.

$$\int \frac{(fx + e)^2 \cosh(dx + c) \coth(dx + c)^2}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 491 leaves, 37 steps):

$$\begin{aligned}
& \frac{b(fx + e)^3}{3a^2 f} - \frac{(a^2 + b^2)(fx + e)^3}{3a^2 b f} - \frac{4f(fx + e) \operatorname{arctanh}(e^{dx+c})}{a d^2} - \frac{(fx + e)^2 \operatorname{csch}(dx + c)}{a d} - \frac{b(fx + e)^2 \ln(1 - e^{2dx+2c})}{a^2 d} \\
& + \frac{(a^2 + b^2)(fx + e)^2 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^2 b d} + \frac{(a^2 + b^2)(fx + e)^2 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^2 b d} - \frac{2f^2 \operatorname{polylog}(2, -e^{dx+c})}{a d^3} + \frac{2f^2 \operatorname{polylog}(2, e^{dx+c})}{a d^3} \\
& - \frac{bf(fx + e) \operatorname{polylog}(2, e^{2dx+2c})}{a^2 d^2} + \frac{2(a^2 + b^2)f(fx + e) \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^2 b d^2} + \frac{2(a^2 + b^2)f(fx + e) \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^2 b d^2} \\
& + \frac{bf^2 \operatorname{polylog}(3, e^{2dx+2c})}{2a^2 d^3} - \frac{2(a^2 + b^2)f^2 \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^2 b d^3} - \frac{2(a^2 + b^2)f^2 \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^2 b d^3}
\end{aligned}$$

Result (type 8, 482 leaves):

$$\frac{\frac{1}{3} x^3 f^2 + e f x^2 + e^2 x}{b} - \frac{2(x^2 f^2 + 2 e f x + e^2) e^{d x+c}}{d a ((e^{d x+c})^2 - 1)} + \int -\frac{1}{a ((e^{d x+c})^2 - 1) d (b (e^{d x+c})^2 + 2 a e^{d x+c} - b) b} (2 ((e^{d x+c})^3 a^2 d f^2 x^2 + b^2 d f^2 x^2 (e^{d x+c})^3 + 2 (e^{d x+c})^3 a^2 d e f x - a b d f^2 x^2 (e^{d x+c})^2 + 2 b^2 d e f x (e^{d x+c})^3 + (e^{d x+c})^3 a^2 d e^2 - e^{d x+c} a^2 d f^2 x^2 - 2 a b d e f x (e^{d x+c})^2 + b^2 d e^2 (e^{d x+c})^3 + b^2 d f^2 x^2 e^{d x+c} - 2 (e^{d x+c})^3 b^2 f^2 x - 2 e^{d x+c} a^2 d e f x - a b d e^2 (e^{d x+c})^2 + a b d f^2 x^2 - 4 (e^{d x+c})^2 a b f^2 x + 2 b^2 d e f x e^{d x+c} - 2 (e^{d x+c})^3 b^2 e f - e^{d x+c} a^2 d e^2 + 2 a b d e f x - 4 (e^{d x+c})^2 a b e f + b^2 d e^2 e^{d x+c} + 2 e^{d x+c} b^2 f^2 x + a b d e^2 + 2 e^{d x+c} b^2 e f) dx$$

Problem 125: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(dx+c) \coth(dx+c)^2}{a+b \sinh(dx+c)} dx$$

Optimal (type 3, 59 leaves, 4 steps):

$$-\frac{\operatorname{csch}(dx+c)}{a d} - \frac{b \ln(\sinh(dx+c))}{a^2 d} + \frac{(a^2+b^2) \ln(a+b \sinh(dx+c))}{a^2 b d}$$

Result (type 3, 171 leaves):

$$\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{2 d a} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)}{d b} - \frac{1}{2 d a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)} - \frac{b \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)}{d a^2} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)}{d b} + \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b - a\right)}{d b} + \frac{b \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b - a\right)}{d a^2}$$

Problem 131: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(dx+c)^2 \operatorname{sech}(dx+c)^3}{a+b \sinh(dx+c)} dx$$

Optimal (type 3, 176 leaves, 9 steps):

$$-\frac{a \arctan(\sinh(dx+c))}{2(a^2+b^2)d} - \frac{a(a^2+2b^2) \arctan(\sinh(dx+c))}{(a^2+b^2)^2 d} - \frac{\operatorname{csch}(dx+c)}{a d} + \frac{b(a^2+2b^2) \ln(\cosh(dx+c))}{(a^2+b^2)^2 d} - \frac{b \ln(\sinh(dx+c))}{a^2 d} + \frac{b^5 \ln(a+b \sinh(dx+c))}{a^2(a^2+b^2)^2 d} - \frac{\operatorname{sech}(dx+c)^2(b+a \sinh(dx+c))}{2(a^2+b^2)d}$$

Result (type 3, 477 leaves):

$$\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{2 d a} + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 a^3}{d(a^2+b^2)^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2} + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 b^2 a}{d(a^2+b^2)^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2} + \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a^2 b}{d(a^2+b^2)^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2}$$

$$\begin{aligned}
& + \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 b^3}{d(a^2 + b^2)^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a^3}{d(a^2 + b^2)^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^2 a}{d(a^2 + b^2)^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^2} \\
& + \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right) a^2 b}{d(a^2 + b^2)^2} + \frac{2 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right) b^3}{d(a^2 + b^2)^2} - \frac{3 \arctan\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right) a^3}{d(a^2 + b^2)^2} - \frac{5 \arctan\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right) b^2 a}{d(a^2 + b^2)^2} \\
& - \frac{1}{2 d a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)} - \frac{b \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)}{d a^2} + \frac{b^5 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b - a\right)}{d(a^2 + b^2)^2 a^2}
\end{aligned}$$

Problem 132: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \coth(dx + c) \operatorname{csch}(dx + c)^2}{a + b \sinh(dx + c)} dx$$

Optimal (type 4, 709 leaves, 34 steps):

$$\begin{aligned}
& - \frac{3f(fx + e)^2}{2 a d^2} + \frac{6 b f(fx + e)^2 \operatorname{arctanh}(e^{dx+c})}{a^2 d^2} - \frac{3f(fx + e)^2 \coth(dx + c)}{2 a d^2} + \frac{b(fx + e)^3 \operatorname{csch}(dx + c)}{a^2 d} - \frac{(fx + e)^3 \operatorname{csch}(dx + c)^2}{2 a d} \\
& + \frac{3f^2(fx + e) \ln(1 - e^{2dx+2c})}{a d^3} + \frac{b^2(fx + e)^3 \ln(1 - e^{2dx+2c})}{a^3 d} - \frac{b^2(fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 d} - \frac{b^2(fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 d} \\
& + \frac{6 b f^2(fx + e) \operatorname{polylog}(2, -e^{dx+c})}{a^2 d^3} - \frac{6 b f^2(fx + e) \operatorname{polylog}(2, e^{dx+c})}{a^2 d^3} + \frac{3 f^3 \operatorname{polylog}(2, e^{2dx+2c})}{2 a d^4} + \frac{3 b^2 f(fx + e)^2 \operatorname{polylog}(2, e^{2dx+2c})}{2 a^3 d^2} \\
& - \frac{3 b^2 f(fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 d^2} - \frac{3 b^2 f(fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 d^2} - \frac{6 b f^3 \operatorname{polylog}(3, -e^{dx+c})}{a^2 d^4} \\
& + \frac{6 b f^3 \operatorname{polylog}(3, e^{dx+c})}{a^2 d^4} - \frac{3 b^2 f^2(fx + e) \operatorname{polylog}(3, e^{2dx+2c})}{2 a^3 d^3} + \frac{6 b^2 f^2(fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 d^3} \\
& + \frac{6 b^2 f^2(fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 d^3} + \frac{3 b^2 f^3 \operatorname{polylog}(4, e^{2dx+2c})}{4 a^3 d^4} - \frac{6 b^2 f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 d^4} \\
& - \frac{6 b^2 f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 d^4}
\end{aligned}$$

Result(type 8, 741 leaves):

$$\begin{aligned}
& -\frac{1}{a^2 d^2 \left( (e^{dx+c})^2 - 1 \right)^2} \left( -2 b d f^3 x^3 (e^{dx+c})^3 + 2 a d f^3 x^3 (e^{dx+c})^2 - 6 b d e f^2 x^2 (e^{dx+c})^3 + 6 a d e f^2 x^2 (e^{dx+c})^2 - 6 b d e^2 f x (e^{dx+c})^3 + 2 b d f^3 x^3 e^{dx+c} \right. \\
& \quad + 6 a d e^2 f x (e^{dx+c})^2 + 3 a f^3 x^2 (e^{dx+c})^2 - 2 b d e^3 (e^{dx+c})^3 + 6 b d e f^2 x^2 e^{dx+c} + 2 a d e^3 (e^{dx+c})^2 + 6 a e f^2 x (e^{dx+c})^2 + 6 b d e^2 f x e^{dx+c} \\
& \quad \left. + 3 a e^2 f (e^{dx+c})^2 - 3 a f^3 x^2 + 2 b d e^3 e^{dx+c} - 6 a e f^2 x - 3 a e^2 f \right) + 4 \left( \right. \\
& \quad \int \frac{1}{2 a^2 \left( (e^{dx+c})^2 - 1 \right) d^2 \left( b (e^{dx+c})^2 + 2 a e^{dx+c} - b \right)} \left( b^2 d^2 f^3 x^3 (e^{dx+c})^3 + 3 b^2 d^2 e f^2 x^2 (e^{dx+c})^3 + 3 b^2 d^2 e^2 f x (e^{dx+c})^3 + b^2 d^2 f^3 x^3 e^{dx+c} \right. \\
& \quad - 3 b^2 d f^3 x^2 (e^{dx+c})^3 - 6 a b d f^3 x^2 (e^{dx+c})^2 + b^2 d^2 e^3 (e^{dx+c})^3 + 3 b^2 d^2 e f^2 x^2 e^{dx+c} - 6 b^2 d e f^2 x (e^{dx+c})^3 - 12 a b d e f^2 x (e^{dx+c})^2 \\
& \quad + 3 b^2 d^2 e^2 f x e^{dx+c} - 3 b^2 d e^2 f (e^{dx+c})^3 + 3 b^2 d f^3 x^2 e^{dx+c} - 6 a b d e^2 f (e^{dx+c})^2 + 3 a b f^3 x (e^{dx+c})^2 + b^2 d^2 e^3 e^{dx+c} + 6 b^2 d e f^2 x e^{dx+c} \\
& \quad \left. + 6 a^2 f^3 x e^{dx+c} + 3 a b e f^2 (e^{dx+c})^2 + 3 b^2 d e^2 f e^{dx+c} + 6 a^2 e f^2 e^{dx+c} - 3 a b f^3 x - 3 a b e f^2 \right) dx
\end{aligned}$$

Problem 134: Unable to integrate problem.

$$\int \frac{(fx + e)^3 \operatorname{csch}(dx + c)^3 \operatorname{sech}(dx + c)}{a + b \sinh(dx + c)} dx$$

Optimal(type 4, 1674 leaves, 87 steps):

$$\begin{aligned}
& \frac{3 I b^3 f (fx + e)^2 \operatorname{polylog}\left(2, -I e^{dx+c}\right)}{a^2 (a^2 + b^2) d^2} + \frac{6 I b^3 f^2 (fx + e) \operatorname{polylog}\left(3, I e^{dx+c}\right)}{a^2 (a^2 + b^2) d^3} - \frac{3 b^4 f (fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d^2} \\
& - \frac{3 b^4 f (fx + e)^2 \operatorname{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d^2} + \frac{6 b^4 f^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d^3} + \frac{6 b^4 f^2 (fx + e) \operatorname{polylog}\left(3, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d^3} \\
& + \frac{3 b^4 f (fx + e)^2 \operatorname{polylog}\left(2, -e^{2 dx+2 c}\right)}{2 a^3 (a^2 + b^2) d^2} - \frac{3 b^4 f^2 (fx + e) \operatorname{polylog}\left(3, -e^{2 dx+2 c}\right)}{2 a^3 (a^2 + b^2) d^3} + \frac{6 I b f^3 \operatorname{polylog}\left(4, I e^{dx+c}\right)}{a^2 d^4} \\
& - \frac{3 I b f (fx + e)^2 \operatorname{polylog}\left(2, -I e^{dx+c}\right)}{a^2 d^2} - \frac{6 I b f^2 (fx + e) \operatorname{polylog}\left(3, I e^{dx+c}\right)}{a^2 d^3} - \frac{6 I b^3 f^3 \operatorname{polylog}\left(4, I e^{dx+c}\right)}{a^2 (a^2 + b^2) d^4} + \frac{3 f^2 (fx + e) \ln\left(1 - e^{2 dx+2 c}\right)}{a d^3} \\
& - \frac{6 b^4 f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d^4} - \frac{6 b^4 f^3 \operatorname{polylog}\left(4, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d^4} + \frac{b^4 (fx + e)^3 \ln\left(1 + e^{2 dx+2 c}\right)}{a^3 (a^2 + b^2) d} \\
& - \frac{b^4 (fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d} - \frac{b^4 (fx + e)^3 \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d} + \frac{3 b^2 f^2 (fx + e) \operatorname{polylog}\left(3, -e^{2 dx+2 c}\right)}{2 a^3 d^3}
\end{aligned}$$

$$\begin{aligned}
& + \frac{3b^4 f^3 \operatorname{polylog}(4, -e^{2dx+2c})}{4a^3(a^2+b^2)d^4} - \frac{6Ibf^3 \operatorname{polylog}(4, -Ie^{dx+c})}{a^2 d^4} + \frac{6bf(fx+e)^2 \operatorname{arctanh}(e^{dx+c})}{a^2 d^2} + \frac{6bf^2(fx+e) \operatorname{polylog}(2, -e^{dx+c})}{a^2 d^3} \\
& - \frac{6bf^2(fx+e) \operatorname{polylog}(2, e^{dx+c})}{a^2 d^3} + \frac{3b^2 f(fx+e)^2 \operatorname{polylog}(2, e^{2dx+2c})}{2a^3 d^2} - \frac{3b^2 f^2(fx+e) \operatorname{polylog}(3, e^{2dx+2c})}{2a^3 d^3} - \frac{2b^3(fx+e)^3 \operatorname{arctan}(e^{dx+c})}{a^2(a^2+b^2)d} \\
& - \frac{3b^2 f(fx+e)^2 \operatorname{polylog}(2, -e^{2dx+2c})}{2a^3 d^2} + \frac{3f^3 \operatorname{polylog}(4, -e^{2dx+2c})}{4a d^4} - \frac{3f^3 \operatorname{polylog}(4, e^{2dx+2c})}{4a d^4} - \frac{3f(fx+e)^2}{2a d^2} + \frac{3f^3 \operatorname{polylog}(2, e^{2dx+2c})}{2a d^4} \\
& + \frac{2(fx+e)^3 \operatorname{arctanh}(e^{2dx+2c})}{a d} - \frac{(fx+e)^3 \operatorname{coth}(dx+c)^2}{2a d} + \frac{3Ibf(fx+e)^2 \operatorname{polylog}(2, Ie^{dx+c})}{a^2 d^2} + \frac{6Ibf^2(fx+e) \operatorname{polylog}(3, -Ie^{dx+c})}{a^2 d^3} \\
& + \frac{6Ib^3 f^3 \operatorname{polylog}(4, -Ie^{dx+c})}{a^2(a^2+b^2)d^4} - \frac{3Ib^3 f(fx+e)^2 \operatorname{polylog}(2, Ie^{dx+c})}{a^2(a^2+b^2)d^2} - \frac{6Ib^3 f^2(fx+e) \operatorname{polylog}(3, -Ie^{dx+c})}{a^2(a^2+b^2)d^3} - \frac{3f(fx+e)^2 \operatorname{coth}(dx+c)}{2a d^2} \\
& - \frac{6bf^3 \operatorname{polylog}(3, -e^{dx+c})}{a^2 d^4} + \frac{6bf^3 \operatorname{polylog}(3, e^{dx+c})}{a^2 d^4} + \frac{3b^2 f^3 \operatorname{polylog}(4, e^{2dx+2c})}{4a^3 d^4} + \frac{2b(fx+e)^3 \operatorname{arctan}(e^{dx+c})}{a^2 d} \\
& - \frac{2b^2(fx+e)^3 \operatorname{arctanh}(e^{2dx+2c})}{a^3 d} + \frac{b(fx+e)^3 \operatorname{csch}(dx+c)}{a^2 d} + \frac{3f(fx+e)^2 \operatorname{polylog}(2, -e^{2dx+2c})}{2a d^2} - \frac{3f^2(fx+e) \operatorname{polylog}(3, -e^{2dx+2c})}{2a d^3} \\
& - \frac{3b^2 f^3 \operatorname{polylog}(4, -e^{2dx+2c})}{4a^3 d^4} - \frac{3f(fx+e)^2 \operatorname{polylog}(2, e^{2dx+2c})}{2a d^2} + \frac{3f^2(fx+e) \operatorname{polylog}(3, e^{2dx+2c})}{2a d^3} + \frac{(fx+e)^3}{2a d}
\end{aligned}$$

Result(type 8, 1015 leaves):

$$\begin{aligned}
& - \frac{1}{a^2 d^2 ((e^{dx+c})^2 - 1)^2} \left( -2bd f^3 x^3 (e^{dx+c})^3 + 2adf^3 x^3 (e^{dx+c})^2 - 6bde f^2 x^2 (e^{dx+c})^3 + 6ade f^2 x^2 (e^{dx+c})^2 - 6bd e^2 f x (e^{dx+c})^3 + 2bd f^3 x^3 e^{dx+c} \right. \\
& \quad + 6ad e^2 f x (e^{dx+c})^2 + 3af^3 x^2 (e^{dx+c})^2 - 2bde^3 (e^{dx+c})^3 + 6bde f^2 x^2 e^{dx+c} + 2ade^3 (e^{dx+c})^2 + 6ae f^2 x (e^{dx+c})^2 + 6bd e^2 f x e^{dx+c} \\
& \quad \left. + 3ae^2 f (e^{dx+c})^2 - 3af^3 x^2 + 2bde^3 e^{dx+c} - 6ae f^2 x - 3ae^2 f \right) + 16 \left( \int \right. \\
& - \frac{1}{8a^2 ((e^{dx+c})^2 + 1) ((e^{dx+c})^2 - 1) d^2 (b(e^{dx+c})^2 + 2ae^{dx+c} - b)} \left( -3(e^{dx+c})^4 ab f^3 x - 3(e^{dx+c})^4 ab e f^2 - 3b^2 d e^2 f e^{dx+c} \right. \\
& \quad - b^2 d^2 f^3 x^3 (e^{dx+c})^5 + 4a^2 d^2 f^3 x^3 (e^{dx+c})^3 + 3b^2 d f^3 x^2 (e^{dx+c})^5 + 3b^2 d e^2 f (e^{dx+c})^5 - 2b^2 d^2 f^3 x^3 (e^{dx+c})^3 - b^2 d^2 f^3 x^3 e^{dx+c} - 3b^2 d f^3 x^2 e^{dx+c} \\
& \quad - 3b^2 d^2 e f^2 x^2 (e^{dx+c})^5 - 3b^2 d^2 e^2 f x (e^{dx+c})^5 + 12a^2 d^2 e f^2 x^2 (e^{dx+c})^3 + 6ab d f^3 x^2 (e^{dx+c})^4 + 6b^2 d e f^2 x (e^{dx+c})^5 + 12a^2 d^2 e^2 f x (e^{dx+c})^3 \\
& \quad + 6ab d e^2 f (e^{dx+c})^4 + 12ab d e f^2 x (e^{dx+c})^4 + 12ab d e f^2 x (e^{dx+c})^2 + 3ab f^3 x + 3ab e f^2 - 2b^2 d^2 e^3 (e^{dx+c})^3 - b^2 d^2 e^3 e^{dx+c} - 6a^2 f^3 x e^{dx+c} \\
& \quad - 6a^2 e f^2 e^{dx+c} - b^2 d^2 e^3 (e^{dx+c})^5 + 4a^2 d^2 e^3 (e^{dx+c})^3 - 6(e^{dx+c})^3 a^2 f^3 x - 6(e^{dx+c})^3 a^2 e f^2 - 6b^2 d^2 e f^2 x^2 (e^{dx+c})^3 - 6b^2 d^2 e^2 f x (e^{dx+c})^3 \\
& \quad \left. + 6ab d f^3 x^2 (e^{dx+c})^2 - 3b^2 d^2 e f^2 x^2 e^{dx+c} - 3b^2 d^2 e^2 f x e^{dx+c} + 6abd e^2 f (e^{dx+c})^2 - 6b^2 d e f^2 x e^{dx+c} \right) dx
\end{aligned}$$

Problem 135: Result more than twice size of optimal antiderivative.

$$\int \frac{(fx+e) \operatorname{csch}(dx+c)^3 \operatorname{sech}(dx+c)}{a+b \sinh(dx+c)} dx$$

Optimal(type 4, 714 leaves, 49 steps):

$$\begin{aligned}
& \frac{I b^3 f \text{polylog}(2, -I e^{dx+c})}{a^2 (a^2 + b^2) d^2} - \frac{I b^3 f \text{polylog}(2, I e^{dx+c})}{a^2 (a^2 + b^2) d^2} + \frac{f x \ln(\tanh(dx+c))}{a d} + \frac{b^4 (fx+e) \ln(1+e^{2dx+2c})}{a^3 (a^2 + b^2) d} - \frac{b^4 (fx+e) \ln\left(1 + \frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d} \\
& - \frac{b^4 (fx+e) \ln\left(1 + \frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d} - \frac{b^4 f \text{polylog}\left(2, -\frac{b e^{dx+c}}{a - \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d^2} - \frac{b^4 f \text{polylog}\left(2, -\frac{b e^{dx+c}}{a + \sqrt{a^2 + b^2}}\right)}{a^3 (a^2 + b^2) d^2} - \frac{I b f \text{polylog}(2, -I e^{dx+c})}{a^2 d^2} \\
& + \frac{2 b f x \arctan(e^{dx+c})}{a^2 d} - \frac{2 b^3 (fx+e) \arctan(e^{dx+c})}{a^2 (a^2 + b^2) d} - \frac{b f x \arctan(\sinh(dx+c))}{a^2 d} + \frac{I b f \text{polylog}(2, I e^{dx+c})}{a^2 d^2} + \frac{b^4 f \text{polylog}(2, -e^{2dx+2c})}{2 a^3 (a^2 + b^2) d^2} \\
& - \frac{(fx+e) \ln(\tanh(dx+c))}{a d} - \frac{f \coth(dx+c)}{2 a d^2} - \frac{(fx+e) \coth(dx+c)^2}{2 a d} + \frac{f \text{polylog}(2, -e^{2dx+2c})}{2 a d^2} - \frac{f \text{polylog}(2, e^{2dx+2c})}{2 a d^2} + \frac{f x}{2 a d} \\
& + \frac{b (fx+e) \arctan(\sinh(dx+c))}{a^2 d} + \frac{2 f x \operatorname{arctanh}(e^{2dx+2c})}{a d} - \frac{2 b^2 (fx+e) \operatorname{arctanh}(e^{2dx+2c})}{a^3 d} + \frac{b f \operatorname{arctanh}(\cosh(dx+c))}{a^2 d^2} \\
& + \frac{b (fx+e) \operatorname{csch}(dx+c)}{a^2 d} - \frac{b^2 f \text{polylog}(2, -e^{2dx+2c})}{2 a^3 d^2} + \frac{b^2 f \text{polylog}(2, e^{2dx+2c})}{2 a^3 d^2}
\end{aligned}$$

Result(type 4, 1477 leaves):

$$\begin{aligned}
& \frac{b^2 f \operatorname{arctanh}\left(\frac{2 e^{dx+c} b + 2 a}{2 \sqrt{a^2 + b^2}}\right)}{d^2 (a^2 + b^2)^{3/2}} + \frac{b^2 e \ln(1+e^{dx+c})}{a^3 d} + \frac{b^2 e \ln(e^{dx+c} - 1)}{a^3 d} - \frac{b^2 f \operatorname{dilog}(e^{dx+c})}{a^3 d^2} + \frac{b^2 f \operatorname{dilog}(1+e^{dx+c})}{a^3 d^2} - \frac{b f \ln(e^{dx+c} - 1)}{a^2 d^2} \\
& + \frac{b f \ln(1+e^{dx+c})}{a^2 d^2} - \frac{e \ln(e^{dx+c} - 1)}{a d} - \frac{e \ln(1+e^{dx+c})}{a d} - \frac{b^4 f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) x}{a^3 d (a^2 + b^2)} - \frac{b^4 f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) c}{a^3 d^2 (a^2 + b^2)} \\
& - \frac{b^4 f \ln\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right) c}{a^3 d^2 (a^2 + b^2)} + \frac{b^4 f c \ln(b e^{2dx+2c} + 2 a e^{dx+c} - b)}{a^3 d^2 (a^2 + b^2)} - \frac{b^4 f \ln\left(\frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}}\right) x}{a^3 d (a^2 + b^2)} + \frac{4 I f \ln(1 - I e^{dx+c}) b x}{d (4 a^2 + 4 b^2)} \\
& - \frac{4 I f \ln(1 + I e^{dx+c}) b x}{d (4 a^2 + 4 b^2)} + \frac{4 I f \ln(1 - I e^{dx+c}) b c}{d^2 (4 a^2 + 4 b^2)} - \frac{4 I f \ln(1 + I e^{dx+c}) b c}{d^2 (4 a^2 + 4 b^2)} - \frac{\ln(1+e^{dx+c}) f x}{a d} + \frac{c \ln(e^{dx+c} - 1)}{a d^2} + \frac{f \operatorname{dilog}(e^{dx+c})}{a d^2} \\
& - \frac{f \operatorname{dilog}(1+e^{dx+c})}{a d^2} - \frac{b^2 c \ln(e^{dx+c} - 1)}{a^3 d^2} + \frac{b^2 f \ln(1+e^{dx+c}) x}{a^3 d} - \frac{b^2 f \operatorname{arctanh}\left(\frac{2 e^{dx+c} b + 2 a}{2 \sqrt{a^2 + b^2}}\right)}{a^2 d^2 \sqrt{a^2 + b^2}} + \frac{b^4 f \operatorname{arctanh}\left(\frac{2 e^{dx+c} b + 2 a}{2 \sqrt{a^2 + b^2}}\right)}{a^2 d^2 (a^2 + b^2)^{3/2}} \\
& - \frac{b^4 e \ln(b e^{2dx+2c} + 2 a e^{dx+c} - b)}{a^3 d (a^2 + b^2)} - \frac{4 I f \operatorname{dilog}(1 + I e^{dx+c}) b}{d^2 (4 a^2 + 4 b^2)} + \frac{4 I f \operatorname{dilog}(1 - I e^{dx+c}) b}{d^2 (4 a^2 + 4 b^2)} - \frac{b^4 f \operatorname{dilog}\left(\frac{-e^{dx+c} b + \sqrt{a^2 + b^2} - a}{-a + \sqrt{a^2 + b^2}}\right)}{a^3 d^2 (a^2 + b^2)}
\end{aligned}$$

$$\begin{aligned}
& - \frac{b^4 f \operatorname{dilog} \left( \frac{e^{dx+c} b + \sqrt{a^2 + b^2} + a}{a + \sqrt{a^2 + b^2}} \right)}{a^3 d^2 (a^2 + b^2)} \\
& - \frac{-2 b d f x e^{3 dx+3 c} + 2 a d f x e^{2 dx+2 c} - 2 b d e e^{3 dx+3 c} + 2 a d e e^{2 dx+2 c} + 2 b d f x e^{dx+c} + a f e^{2 dx+2 c} + 2 b d e e^{dx+c} - a f}{d^2 a^2 (e^{2 dx+2 c} - 1)^2} + \frac{4 f \ln(1 + I e^{dx+c}) a x}{d (4 a^2 + 4 b^2)} \\
& + \frac{4 f \ln(1 + I e^{dx+c}) a c}{d^2 (4 a^2 + 4 b^2)} + \frac{4 f \ln(1 - I e^{dx+c}) a x}{d (4 a^2 + 4 b^2)} + \frac{4 f \ln(1 - I e^{dx+c}) a c}{d^2 (4 a^2 + 4 b^2)} - \frac{4 c f a \ln(1 + e^{2 dx+2 c})}{d^2 (4 a^2 + 4 b^2)} - \frac{8 c f b \arctan(e^{dx+c})}{d^2 (4 a^2 + 4 b^2)} \\
& + \frac{4 f \operatorname{dilog}(1 - I e^{dx+c}) a}{d^2 (4 a^2 + 4 b^2)} + \frac{4 f \operatorname{dilog}(1 + I e^{dx+c}) a}{d^2 (4 a^2 + 4 b^2)} + \frac{4 e a \ln(1 + e^{2 dx+2 c})}{d (4 a^2 + 4 b^2)} + \frac{8 e b \arctan(e^{dx+c})}{d (4 a^2 + 4 b^2)}
\end{aligned}$$

Test results for the 30 problems in "6.1.3 (e x)^m (a+b sinh(c+d x^n))^p.txt"

Problem 12: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh\left(a + \frac{b}{x}\right)}{x^4} dx$$

Optimal(type 3, 46 leaves, 4 steps):

$$-\frac{2 \cosh\left(a + \frac{b}{x}\right)}{b^3} - \frac{\cosh\left(a + \frac{b}{x}\right)}{b x^2} + \frac{2 \sinh\left(a + \frac{b}{x}\right)}{b^2 x}$$

Result(type 3, 93 leaves):

$$-\frac{\left(a + \frac{b}{x}\right)^2 \cosh\left(a + \frac{b}{x}\right) - 2 \left(a + \frac{b}{x}\right) \sinh\left(a + \frac{b}{x}\right) + 2 \cosh\left(a + \frac{b}{x}\right) - 2 a \left( \left(a + \frac{b}{x}\right) \cosh\left(a + \frac{b}{x}\right) - \sinh\left(a + \frac{b}{x}\right) \right) + a^2 \cosh\left(a + \frac{b}{x}\right)}{b^3}$$

Problem 13: Result unnecessarily involves higher level functions.

$$\int (e x)^m \sinh\left(a + \frac{b}{x}\right) dx$$

Optimal(type 4, 61 leaves, 4 steps):

$$-\frac{b e^a \left(-\frac{b}{x}\right)^m (e x)^m \Gamma\left(-1 - m, -\frac{b}{x}\right)}{2} - \frac{b \left(\frac{b}{x}\right)^m (e x)^m \Gamma\left(-1 - m, \frac{b}{x}\right)}{2 e^a}$$

Result(type 5, 69 leaves):

$$\frac{(e x)^m b \operatorname{hypergeom}\left(\left[\left[-\frac{m}{2}\right], \left[\frac{3}{2}, 1 - \frac{m}{2}\right], \frac{b^2}{4 x^2}\right], \cosh(a)\right)}{m} + \frac{(e x)^m x \operatorname{hypergeom}\left(\left[\left[-\frac{m}{2} - \frac{1}{2}\right], \left[\frac{1}{2}, \frac{1}{2} - \frac{m}{2}\right], \frac{b^2}{4 x^2}\right], \sinh(a)\right)}{1 + m}$$



Problem 19: Result unnecessarily involves higher level functions.

$$\int x \sinh(a + b x^n) dx$$

Optimal(type 4, 73 leaves, 3 steps):

$$-\frac{e^a x^2 \Gamma\left(\frac{2}{n}, -b x^n\right)}{2 n (-b x^n)^{\frac{2}{n}}} + \frac{x^2 \Gamma\left(\frac{2}{n}, b x^n\right)}{2 e^a n (b x^n)^{\frac{2}{n}}}$$

Result(type 5, 68 leaves):

$$\frac{x^2 \operatorname{hypergeom}\left(\left[\frac{1}{n}\right], \left[\frac{1}{2}, 1 + \frac{1}{n}\right], \frac{x^{2n} b^2}{4}\right) \sinh(a)}{2} + \frac{x^{n+2} b \operatorname{hypergeom}\left(\left[\frac{1}{2} + \frac{1}{n}\right], \left[\frac{3}{2}, \frac{3}{2} + \frac{1}{n}\right], \frac{x^{2n} b^2}{4}\right) \cosh(a)}{n+2}$$

Problem 20: Unable to integrate problem.

$$\int x^2 \sinh(a + b x^n)^2 dx$$

Optimal(type 4, 101 leaves, 5 steps):

$$-\frac{x^3}{6} - \frac{2^{-2-\frac{3}{n}} e^{2a} x^3 \Gamma\left(\frac{3}{n}, -2 b x^n\right)}{n (-b x^n)^{\frac{3}{n}}} - \frac{2^{-2-\frac{3}{n}} x^3 \Gamma\left(\frac{3}{n}, 2 b x^n\right)}{e^{2a} n (b x^n)^{\frac{3}{n}}}$$

Result(type 8, 16 leaves):

$$\int x^2 \sinh(a + b x^n)^2 dx$$

Problem 21: Unable to integrate problem.

$$\int x \sinh(a + b x^n)^2 dx$$

Optimal(type 4, 101 leaves, 5 steps):

$$-\frac{x^2}{4} - \frac{4^{-1-\frac{1}{n}} e^{2a} x^2 \Gamma\left(\frac{2}{n}, -2 b x^n\right)}{n (-b x^n)^{\frac{2}{n}}} - \frac{4^{-1-\frac{1}{n}} x^2 \Gamma\left(\frac{2}{n}, 2 b x^n\right)}{e^{2a} n (b x^n)^{\frac{2}{n}}}$$

Result(type 8, 14 leaves):

$$\int x \sinh(a + b x^n)^2 dx$$

Problem 22: Unable to integrate problem.

$$\int \sinh(a + bx^n)^2 dx$$

Optimal(type 4, 87 leaves, 5 steps):

$$-\frac{x}{2} - \frac{2^{-2-\frac{1}{n}} e^{2a} x \Gamma\left(\frac{1}{n}, -2bx^n\right)}{n(-bx^n)^{\frac{1}{n}}} - \frac{2^{-2-\frac{1}{n}} x \Gamma\left(\frac{1}{n}, 2bx^n\right)}{e^{2a} n (bx^n)^{\frac{1}{n}}}$$

Result(type 8, 12 leaves):

$$\int \sinh(a + bx^n)^2 dx$$

Problem 23: Unable to integrate problem.

$$\int x \sinh(a + bx^n)^3 dx$$

Optimal(type 4, 164 leaves, 8 steps):

$$-\frac{e^{3a} x^2 \Gamma\left(\frac{2}{n}, -3bx^n\right)}{89^{\frac{1}{n}} n (-bx^n)^{\frac{2}{n}}} + \frac{3 e^a x^2 \Gamma\left(\frac{2}{n}, -bx^n\right)}{8 n (-bx^n)^{\frac{2}{n}}} - \frac{3 x^2 \Gamma\left(\frac{2}{n}, bx^n\right)}{8 e^a n (bx^n)^{\frac{2}{n}}} + \frac{x^2 \Gamma\left(\frac{2}{n}, 3bx^n\right)}{89^{\frac{1}{n}} e^{3a} n (bx^n)^{\frac{2}{n}}}$$

Result(type 8, 14 leaves):

$$\int x \sinh(a + bx^n)^3 dx$$

Problem 24: Unable to integrate problem.

$$\int (ex)^m \sinh(a + bx^n)^3 dx$$

Optimal(type 4, 216 leaves, 8 steps):

$$-\frac{e^{3a} (ex)^{1+m} \Gamma\left(\frac{1+m}{n}, -3bx^n\right)}{83^{\frac{1+m}{n}} e n (-bx^n)^{\frac{1+m}{n}}} + \frac{3 e^a (ex)^{1+m} \Gamma\left(\frac{1+m}{n}, -bx^n\right)}{8 e n (-bx^n)^{\frac{1+m}{n}}} - \frac{3 (ex)^{1+m} \Gamma\left(\frac{1+m}{n}, bx^n\right)}{8 e e^a n (bx^n)^{\frac{1+m}{n}}} + \frac{(ex)^{1+m} \Gamma\left(\frac{1+m}{n}, 3bx^n\right)}{83^{\frac{1+m}{n}} e e^{3a} n (bx^n)^{\frac{1+m}{n}}}$$

Result(type 8, 18 leaves):

$$\int (ex)^m \sinh(a + bx^n)^3 dx$$

Problem 25: Unable to integrate problem.

$$\int (ex)^m \sinh(a + bx^n)^2 dx$$

Optimal(type 4, 145 leaves, 5 steps):

$$-\frac{(ex)^{1+m}}{2e(1+m)} - \frac{e^{2a}(ex)^{1+m}\Gamma\left(\frac{1+m}{n}, -2bx^n\right)}{2\frac{1+m+2n}{n}en(-bx^n)^{\frac{1+m}{n}}} - \frac{(ex)^{1+m}\Gamma\left(\frac{1+m}{n}, 2bx^n\right)}{2\frac{1+m+2n}{n}e^2an(bx^n)^{\frac{1+m}{n}}}$$

Result(type 8, 18 leaves):

$$\int (ex)^m \sinh(a + bx^n)^2 dx$$

Problem 29: Unable to integrate problem.

$$\int \frac{\sinh(a + b(dx+c)^{1/3})}{x} dx$$

Optimal(type 4, 180 leaves, 13 steps):

$$-\cosh(a + bc^{1/3}) \operatorname{Shi}(b(c^{1/3} - (dx+c)^{1/3})) - \cosh(a + (-1)^{2/3}bc^{1/3}) \operatorname{Shi}(b((-1)^{2/3}c^{1/3} - (dx+c)^{1/3})) + \cosh(a - (-1)^{1/3}bc^{1/3}) \operatorname{Shi}(b((-1)^{1/3}c^{1/3} + (dx+c)^{1/3})) + \operatorname{Chi}(b(c^{1/3} - (dx+c)^{1/3})) \sinh(a + bc^{1/3}) + \operatorname{Chi}(b((-1)^{1/3}c^{1/3} + (dx+c)^{1/3})) \sinh(a - (-1)^{1/3}bc^{1/3}) + \operatorname{Chi}(-b((-1)^{2/3}c^{1/3} - (dx+c)^{1/3})) \sinh(a + (-1)^{2/3}bc^{1/3})$$

Result(type 8, 18 leaves):

$$\int \frac{\sinh(a + b(dx+c)^{1/3})}{x} dx$$

Problem 30: Unable to integrate problem.

$$\int \frac{\sinh(a + b(dx+c)^{1/3})}{x^2} dx$$

Optimal(type 4, 243 leaves, 14 steps):

$$\frac{bd\operatorname{Chi}(b(c^{1/3} - (dx+c)^{1/3})) \cosh(a + bc^{1/3})}{3c^{2/3}} - \frac{(-1)^{1/3}bd\operatorname{Chi}(b((-1)^{1/3}c^{1/3} + (dx+c)^{1/3})) \cosh(a - (-1)^{1/3}bc^{1/3})}{3c^{2/3}} + \frac{(-1)^{2/3}bd\operatorname{Chi}(-b((-1)^{2/3}c^{1/3} - (dx+c)^{1/3})) \cosh(a + (-1)^{2/3}bc^{1/3})}{3c^{2/3}} - \frac{bd\operatorname{Shi}(b(c^{1/3} - (dx+c)^{1/3})) \sinh(a + bc^{1/3})}{3c^{2/3}} - \frac{(-1)^{1/3}bd\operatorname{Shi}(b((-1)^{1/3}c^{1/3} + (dx+c)^{1/3})) \sinh(a - (-1)^{1/3}bc^{1/3})}{3c^{2/3}} - \frac{(-1)^{2/3}bd\operatorname{Shi}(b((-1)^{2/3}c^{1/3} - (dx+c)^{1/3})) \sinh(a + (-1)^{2/3}bc^{1/3})}{3c^{2/3}} - \frac{\sinh(a + b(dx+c)^{1/3})}{x}$$

Result(type 8, 18 leaves):

$$\int \frac{\sinh(a + b(dx+c)^{1/3})}{x^2} dx$$

Test results for the 11 problems in "6.1.4 (d+e x)^m sinh(a+b x+c x^2)^n.txt"

Problem 4: Unable to integrate problem.

$$\int \left( -\frac{b \cosh(-cx^2 + bx + a)}{x} + \frac{\sinh(-cx^2 + bx + a)}{x^2} \right) dx$$

Optimal(type 4, 82 leaves, 7 steps):

$$-\frac{\sinh(-cx^2 + bx + a)}{x} + \frac{e^{a + \frac{b^2}{4c}} \operatorname{erf}\left(\frac{-2cx + b}{2\sqrt{c}}\right) \sqrt{c} \sqrt{\pi}}{2} + \frac{e^{-a - \frac{b^2}{4c}} \operatorname{erfi}\left(\frac{-2cx + b}{2\sqrt{c}}\right) \sqrt{c} \sqrt{\pi}}{2}$$

Result(type 8, 37 leaves):

$$\int \left( -\frac{b \cosh(-cx^2 + bx + a)}{x} + \frac{\sinh(-cx^2 + bx + a)}{x^2} \right) dx$$

Problem 11: Result more than twice size of optimal antiderivative.

$$\int (ex + d) \sinh(cx^2 + bx + a) dx$$

Optimal(type 4, 100 leaves, 6 steps):

$$\frac{e \cosh(cx^2 + bx + a)}{2c} - \frac{(-be + 2dc) e^{-a + \frac{b^2}{4c}} \operatorname{erf}\left(\frac{2cx + b}{2\sqrt{c}}\right) \sqrt{\pi}}{8c^3/2} + \frac{(-be + 2dc) e^{a - \frac{b^2}{4c}} \operatorname{erfi}\left(\frac{2cx + b}{2\sqrt{c}}\right) \sqrt{\pi}}{8c^3/2}$$

Result(type 4, 210 leaves):

$$-\frac{d\sqrt{\pi} e^{-\frac{4ac-b^2}{4c}} \operatorname{erf}\left(\sqrt{c}x + \frac{b}{2\sqrt{c}}\right)}{4\sqrt{c}} + \frac{e e^{-cx^2 - bx - a}}{4c} + \frac{eb\sqrt{\pi} e^{-\frac{4ac-b^2}{4c}} \operatorname{erf}\left(\sqrt{c}x + \frac{b}{2\sqrt{c}}\right)}{8c^3/2} - \frac{d\sqrt{\pi} e^{\frac{4ac-b^2}{4c}} \operatorname{erf}\left(-\sqrt{-c}x + \frac{b}{2\sqrt{-c}}\right)}{4\sqrt{-c}} + \frac{e e^{cx^2 + bx + a}}{4c} + \frac{eb\sqrt{\pi} e^{\frac{4ac-b^2}{4c}} \operatorname{erf}\left(-\sqrt{-c}x + \frac{b}{2\sqrt{-c}}\right)}{8c\sqrt{-c}}$$

Test results for the 100 problems in "6.1.5 Hyperbolic sine functions.txt"

Problem 12: Unable to integrate problem.

$$\int \frac{1}{(b \sinh(dx + c))^2/3} dx$$

Optimal(type 5, 50 leaves, 1 step):

$$\frac{3 \cosh(dx + c) \operatorname{hypergeom}\left(\left[\frac{1}{6}, \frac{1}{2}\right], \left[\frac{7}{6}\right], -\sinh(dx + c)^2\right) (b \sinh(dx + c))^1 / 3}{bd \sqrt{\cosh(dx + c)^2}}$$

Result(type 8, 12 leaves):

$$\int \frac{1}{(b \sinh(dx + c))^2 / 3} dx$$

Problem 13: Unable to integrate problem.

$$\int (-I \sinh(dx + c))^n dx$$

Optimal(type 5, 64 leaves, 1 step):

$$\frac{I \cosh(dx + c) \operatorname{hypergeom}\left(\left[\frac{1}{2}, \frac{n}{2} + \frac{1}{2}\right], \left[\frac{3}{2} + \frac{n}{2}\right], -\sinh(dx + c)^2\right) (-I \sinh(dx + c))^{n+1}}{d(n+1) \sqrt{\cosh(dx + c)^2}}$$

Result(type 8, 13 leaves):

$$\int (-I \sinh(dx + c))^n dx$$

Problem 14: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(x)^3}{I + \sinh(x)} dx$$

Optimal(type 3, 30 leaves, 2 steps):

$$-\frac{3x}{2} - 2I \cosh(x) + \frac{3 \cosh(x) \sinh(x)}{2} - \frac{\cosh(x) \sinh(x)^2}{I + \sinh(x)}$$

Result(type 3, 92 leaves):

$$\begin{aligned} & \frac{1}{2 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)} + \frac{I}{\tanh\left(\frac{x}{2}\right) - 1} + \frac{1}{2 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^2} + \frac{3 \ln\left(\tanh\left(\frac{x}{2}\right) - 1\right)}{2} + \frac{2}{\tanh\left(\frac{x}{2}\right) + I} + \frac{1}{2 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)} - \frac{I}{\tanh\left(\frac{x}{2}\right) + 1} \\ & - \frac{1}{2 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^2} - \frac{3 \ln\left(\tanh\left(\frac{x}{2}\right) + 1\right)}{2} \end{aligned}$$

Problem 17: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(x)^3}{(I + \sinh(x))^2} dx$$

Optimal(type 3, 36 leaves, 6 steps):

$$-2Ix + \frac{4 \cosh(x)}{3} - \frac{\cosh(x) \sinh(x)^2}{3 (1 + \sinh(x))^2} + \frac{2 I \cosh(x)}{1 + \sinh(x)}$$

Result(type 3, 74 leaves):

$$2I \ln\left(\tanh\left(\frac{x}{2}\right) - 1\right) - \frac{1}{\tanh\left(\frac{x}{2}\right) - 1} + \frac{4I}{3\left(\tanh\left(\frac{x}{2}\right) + 1\right)^3} + \frac{4I}{\tanh\left(\frac{x}{2}\right) + 1} - \frac{2}{\left(\tanh\left(\frac{x}{2}\right) + 1\right)^2} - 2I \ln\left(\tanh\left(\frac{x}{2}\right) + 1\right) + \frac{1}{\tanh\left(\frac{x}{2}\right) + 1}$$

Problem 20: Unable to integrate problem.

$$\int \frac{\sinh(x)}{\sqrt{a + I a \sinh(x)}} dx$$

Optimal(type 3, 44 leaves, 3 steps):

$$-\frac{\operatorname{arctanh}\left(\frac{\cosh(x) \sqrt{a} \sqrt{2}}{2\sqrt{a + I a \sinh(x)}}\right) \sqrt{2}}{\sqrt{a}} + \frac{2 \cosh(x)}{\sqrt{a + I a \sinh(x)}}$$

Result(type 8, 113 leaves):

$$\frac{(e^x - 1)^2 \sqrt{2}}{\sqrt{\frac{a (I (e^x)^2 + 2 e^x - 1)}{e^x}} e^x} + \frac{\left(\int -\frac{2}{\sqrt{a (I (e^x)^2 + 2 e^x - 1)} e^x} dx\right) \sqrt{2} \sqrt{a (I (e^x)^2 + 2 e^x - 1)} e^x}{2 \sqrt{\frac{a (I (e^x)^2 + 2 e^x - 1)}{e^x}} e^x}$$

Problem 21: Unable to integrate problem.

$$\int \frac{\sinh(x)}{\sqrt{a - I a \sinh(x)}} dx$$

Optimal(type 3, 44 leaves, 3 steps):

$$-\frac{\operatorname{arctanh}\left(\frac{\cosh(x) \sqrt{a} \sqrt{2}}{2\sqrt{a - I a \sinh(x)}}\right) \sqrt{2}}{\sqrt{a}} + \frac{2 \cosh(x)}{\sqrt{a - I a \sinh(x)}}$$

Result(type 8, 117 leaves):

$$\frac{(e^x + 1)^2 \sqrt{2}}{\sqrt{-\frac{a (I (e^x)^2 - 2 e^x - 1)}{e^x}} e^x} + \frac{\left(\int -\frac{2}{\sqrt{-a (I (e^x)^2 - 2 e^x - 1)} e^x} dx\right) \sqrt{2} \sqrt{-a (I (e^x)^2 - 2 e^x - 1)} e^x}{2 \sqrt{-\frac{a (I (e^x)^2 - 2 e^x - 1)}{e^x}} e^x}$$

Problem 22: Unable to integrate problem.

$$\int (a + I a \sinh(dx + c))^{5/2} dx$$

Optimal(type 3, 86 leaves, 3 steps):

$$\frac{2 I a \cosh(dx + c) (a + I a \sinh(dx + c))^{3/2}}{5 d} + \frac{64 I a^3 \cosh(dx + c)}{15 d \sqrt{a + I a \sinh(dx + c)}} + \frac{16 I a^2 \cosh(dx + c) \sqrt{a + I a \sinh(dx + c)}}{15 d}$$

Result(type 8, 16 leaves):

$$\int (a + I a \sinh(dx + c))^{5/2} dx$$

Problem 23: Unable to integrate problem.

$$\int \frac{1}{(a + I a \sinh(dx + c))^{3/2}} dx$$

Optimal(type 3, 68 leaves, 3 steps):

$$\frac{I \cosh(dx + c)}{2 d (a + I a \sinh(dx + c))^{3/2}} + \frac{I \operatorname{arctanh}\left(\frac{\cosh(dx + c) \sqrt{a} \sqrt{2}}{2 \sqrt{a + I a \sinh(dx + c)}}\right) \sqrt{2}}{4 a^{3/2} d}$$

Result(type 8, 16 leaves):

$$\int \frac{1}{(a + I a \sinh(dx + c))^{3/2}} dx$$

Problem 31: Unable to integrate problem.

$$\int (a + I a \sinh(x))^{3/2} (A + B \sinh(x)) dx$$

Optimal(type 3, 64 leaves, 3 steps):

$$\frac{2 B \cosh(x) (a + I a \sinh(x))^{3/2}}{5} + \frac{8 a^2 (5 I A + 3 B) \cosh(x)}{15 \sqrt{a + I a \sinh(x)}} + \frac{2 a (5 I A + 3 B) \cosh(x) \sqrt{a + I a \sinh(x)}}{15}$$

Result(type 8, 19 leaves):

$$\int (a + I a \sinh(x))^{3/2} (A + B \sinh(x)) dx$$

Problem 37: Unable to integrate problem.

$$\int \frac{A + B \sinh(x)}{(a + I a \sinh(x))^{3/2}} dx$$

Optimal(type 3, 60 leaves, 3 steps):

$$\frac{(IA - B) \cosh(x)}{2(a + Ia \sinh(x))^3 \sqrt{2}} + \frac{(IA + 3B) \operatorname{arctanh}\left(\frac{\cosh(x) \sqrt{a} \sqrt{2}}{2\sqrt{a + Ia \sinh(x)}}\right) \sqrt{2}}{4a^3 \sqrt{2}}$$

Result(type 8, 19 leaves):

$$\int \frac{A + B \sinh(x)}{(a + Ia \sinh(x))^3 \sqrt{2}} dx$$

Problem 38: Result more than twice size of optimal antiderivative.

$$\int (a + b \sinh(x))^5 \sqrt{2} (A + B \sinh(x)) dx$$

Optimal(type 4, 279 leaves, 8 steps):

$$\begin{aligned} & \frac{2(7Ab + 5aB) \cosh(x) (a + b \sinh(x))^3 \sqrt{2}}{35} + \frac{2B \cosh(x) (a + b \sinh(x))^5 \sqrt{2}}{7} + \frac{2(56aAb + 15a^2B - 25b^2B) \cosh(x) \sqrt{a + b \sinh(x)}}{105} \\ & + \frac{2I(161a^2Ab - 63Ab^3 + 15a^3B - 145ab^2B) \sqrt{\sin\left(\frac{\pi}{4} + \frac{Ix}{2}\right)^2} \operatorname{EllipticE}\left(\cos\left(\frac{\pi}{4} + \frac{Ix}{2}\right), \sqrt{2} \sqrt{\frac{b}{Ia + b}}\right) \sqrt{a + b \sinh(x)}}{105 \sin\left(\frac{\pi}{4} + \frac{Ix}{2}\right) b \sqrt{\frac{a + b \sinh(x)}{a - Ib}}} \\ & - \frac{2I(a^2 + b^2) (56aAb + 15a^2B - 25b^2B) \sqrt{\sin\left(\frac{\pi}{4} + \frac{Ix}{2}\right)^2} \operatorname{EllipticF}\left(\cos\left(\frac{\pi}{4} + \frac{Ix}{2}\right), \sqrt{2} \sqrt{\frac{b}{Ia + b}}\right) \sqrt{\frac{a + b \sinh(x)}{a - Ib}}}{105 \sin\left(\frac{\pi}{4} + \frac{Ix}{2}\right) b \sqrt{a + b \sinh(x)}} \end{aligned}$$

Result(type 4, 1892 leaves):

$$\begin{aligned} & \frac{1}{105b^2 \cosh(x) \sqrt{a + b \sinh(x)}} \left( 2 \left( 63A \sqrt{-\frac{a + b \sinh(x)}{Ib - a}} \operatorname{EllipticE}\left(\sqrt{-\frac{a + b \sinh(x)}{Ib - a}}, \sqrt{-\frac{Ib - a}{Ib + a}}\right) \sqrt{\frac{(I - \sinh(x)) b}{Ib + a}} \sqrt{\frac{(I + \sinh(x)) b}{Ib - a}} b^5 \right. \right. \\ & - 15B \sqrt{-\frac{a + b \sinh(x)}{Ib - a}} \operatorname{EllipticE}\left(\sqrt{-\frac{a + b \sinh(x)}{Ib - a}}, \sqrt{-\frac{Ib - a}{Ib + a}}\right) \sqrt{\frac{(I - \sinh(x)) b}{Ib + a}} \sqrt{\frac{(I + \sinh(x)) b}{Ib - a}} a^5 \\ & - 63A \sqrt{-\frac{a + b \sinh(x)}{Ib - a}} \operatorname{EllipticF}\left(\sqrt{-\frac{a + b \sinh(x)}{Ib - a}}, \sqrt{-\frac{Ib - a}{Ib + a}}\right) \sqrt{\frac{(I - \sinh(x)) b}{Ib + a}} \sqrt{\frac{(I + \sinh(x)) b}{Ib - a}} b^5 + 15Bb^5 \sinh(x)^5 + 21Ab^5 \sinh(x)^4 \\ & - 10Bb^5 \sinh(x)^3 + 21Ab^5 \sinh(x)^2 - 25Bb^5 \sinh(x) + 60Bab^4 \sinh(x)^4 + 98Aab^4 \sinh(x)^3 + 90Ba^2b^3 \sinh(x)^3 + 77Aa^2b^3 \sinh(x)^2 \\ & + 45Ba^3b^2 \sinh(x)^2 + 35Bab^4 \sinh(x)^2 + 98Aab^4 \sinh(x) + 90Ba^2b^3 \sinh(x) + 15IB \sqrt{-\frac{a + b \sinh(x)}{Ib - a}} \operatorname{EllipticF}\left(\sqrt{-\frac{a + b \sinh(x)}{Ib - a}}, \right. \\ & \left. \sqrt{-\frac{Ib - a}{Ib + a}}\right) \sqrt{\frac{(I - \sinh(x)) b}{Ib + a}} \sqrt{\frac{(I + \sinh(x)) b}{Ib - a}} a^4 b - 10IB \sqrt{-\frac{a + b \sinh(x)}{Ib - a}} \operatorname{EllipticF}\left(\sqrt{-\frac{a + b \sinh(x)}{Ib - a}}, \right. \end{aligned}$$



$$\begin{aligned}
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a^2 b^3 + 56 IA \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticF}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a^3 b^2 - 25 IB \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticF}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} b^5 + 42 A \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticF}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a^2 b^3 - 98 A \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticE}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a^2 b^3 - 120 B \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticF}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a^3 b^2 - 120 B \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticF}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a b^4 + 130 B \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticE}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a^3 b^2 + 145 B \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticE}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a b^4 + 105 A \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticF}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a^4 b - 161 A \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticE}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a^4 b + 56 IA \sqrt{-\frac{a+b\sinh(x)}{Ib-a}} \operatorname{EllipticF}\left(\sqrt{-\frac{a+b\sinh(x)}{Ib-a}}, \right. \\
& \left. \left. \sqrt{-\frac{Ib-a}{Ib+a}} \sqrt{\frac{(I-\sinh(x))b}{Ib+a}} \sqrt{\frac{(I+\sinh(x))b}{Ib-a}} a b^4 + 77 A a^2 b^3 + 45 B a^3 b^2 - 25 B a b^4 \right) \right)
\end{aligned}$$

Problem 39: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \sinh(x)}{(a + b \sinh(x))^3} dx$$

Optimal (type 3, 118 leaves, 6 steps):

$$-\frac{(2a^2A - Ab^2 + 3abB) \operatorname{arctanh}\left(\frac{b - a \tanh\left(\frac{x}{2}\right)}{\sqrt{a^2 + b^2}}\right)}{(a^2 + b^2)^{5/2}} - \frac{(Ab - aB) \cosh(x)}{2(a^2 + b^2)(a + b \sinh(x))^2} - \frac{(3aAb - a^2B + 2b^2B) \cosh(x)}{2(a^2 + b^2)^2(a + b \sinh(x))}$$

Result (type 3, 313 leaves):

$$\begin{aligned}
& - \frac{1}{\left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)^2} \left( 2 \left( - \frac{b(5a^2Ab + 2Ab^3 - 3a^3B) \tanh\left(\frac{x}{2}\right)^3}{2a(a^4 + 2b^2a^2 + b^4)} \right. \right. \\
& - \frac{(4Aa^4b - 7Aa^2b^3 - 2Ab^5 - 2Ba^5 + 5Ba^3b^2 - 2Bab^4) \tanh\left(\frac{x}{2}\right)^2}{2(a^4 + 2b^2a^2 + b^4)a^2} + \frac{b(11a^2Ab + 2Ab^3 - 5a^3B + 4ab^2B) \tanh\left(\frac{x}{2}\right)}{2(a^4 + 2b^2a^2 + b^4)a} \\
& \left. \left. + \frac{4a^2Ab + Ab^3 - 2a^3B + ab^2B}{2(a^4 + 2b^2a^2 + b^4)} \right) \right) + \frac{(2a^2A - Ab^2 + 3abB) \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2 + b^2}}\right)}{(a^4 + 2b^2a^2 + b^4)\sqrt{a^2 + b^2}}
\end{aligned}$$

Problem 42: Unable to integrate problem.

$$\int (a \sinh(x)^3)^{3/2} dx$$

Optimal (type 4, 89 leaves, 5 steps):

$$- \frac{14a \cosh(x) \sqrt{a \sinh(x)^3}}{45} + \frac{2a \cosh(x) \sinh(x)^2 \sqrt{a \sinh(x)^3}}{9} + \frac{14Ia \operatorname{csch}(x) \sqrt{\sin\left(\frac{\pi}{4} + \frac{Ix}{2}\right)^2} \operatorname{EllipticE}\left(\cos\left(\frac{\pi}{4} + \frac{Ix}{2}\right), \sqrt{2}\right) \sqrt{a \sinh(x)^3}}{15 \sin\left(\frac{\pi}{4} + \frac{Ix}{2}\right) \sqrt{I \sinh(x)}}$$

Result (type 8, 10 leaves):

$$\int (a \sinh(x)^3)^{3/2} dx$$

Problem 43: Unable to integrate problem.

$$\int \sqrt{a \sinh(x)^3} dx$$

Optimal (type 4, 72 leaves, 4 steps):

$$\frac{2 \coth(x) \sqrt{a \sinh(x)^3}}{3} - \frac{2I \operatorname{csch}(x)^2 \sqrt{\sin\left(\frac{\pi}{4} + \frac{Ix}{2}\right)^2} \operatorname{EllipticF}\left(\cos\left(\frac{\pi}{4} + \frac{Ix}{2}\right), \sqrt{2}\right) \sqrt{I \sinh(x)} \sqrt{a \sinh(x)^3}}{3 \sin\left(\frac{\pi}{4} + \frac{Ix}{2}\right)}$$

Result (type 8, 10 leaves):

$$\int \sqrt{a \sinh(x)^3} dx$$

Problem 45: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{a \sinh(x)^4}} dx$$

Optimal(type 3, 14 leaves, 3 steps):

$$-\frac{\cosh(x) \sinh(x)}{\sqrt{a \sinh(x)^4}}$$

Result(type 3, 49 leaves):

$$-\frac{\sqrt{a(-1 + \cosh(2x))} (\cosh(2x) + 1) \sqrt{a \sinh(2x)^2}}{a \sinh(2x) \sqrt{a(-1 + \cosh(2x))^2}}$$

Problem 48: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(x)^2}{1 + \sinh(x)} dx$$

Optimal(type 3, 18 leaves, 3 steps):

$$-\frac{I \operatorname{sech}(x)}{3(1 + \sinh(x))} - \frac{2I \tanh(x)}{3}$$

Result(type 3, 48 leaves):

$$-\frac{1}{\left(\tanh\left(\frac{x}{2}\right) + 1\right)^2} + \frac{2I}{3\left(\tanh\left(\frac{x}{2}\right) + 1\right)^3} - \frac{3I}{2\left(\tanh\left(\frac{x}{2}\right) + 1\right)} - \frac{I}{2\left(\tanh\left(\frac{x}{2}\right) - 1\right)}$$

Problem 49: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(x)^6}{a + b \sinh(x)} dx$$

Optimal(type 3, 132 leaves, 7 steps):

$$-\frac{a(8a^4 + 20b^2a^2 + 15b^4)x}{8b^6} - \frac{2(a^2 + b^2)^{5/2} \operatorname{arctanh}\left(\frac{b - a \tanh\left(\frac{x}{2}\right)}{\sqrt{a^2 + b^2}}\right)}{b^6} + \frac{\cosh(x)^5}{5b} + \frac{\cosh(x)^3(4a^2 + 4b^2 - 3ab \sinh(x))}{12b^3} + \frac{\cosh(x)(8(a^2 + b^2)^2 - ab(4a^2 + 7b^2) \sinh(x))}{8b^5}$$

Result(type 3, 673 leaves):

$$\begin{aligned}
& \frac{a^4}{b^5 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)} - \frac{a^3}{2 b^4 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)} + \frac{5 a^2}{2 b^3 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)} - \frac{9 a}{8 b^2 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)} - \frac{a^5 \ln\left(\tanh\left(\frac{x}{2}\right) + 1\right)}{b^6} - \frac{5 a^3 \ln\left(\tanh\left(\frac{x}{2}\right) + 1\right)}{2 b^4} \\
& - \frac{a}{4 b^2 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^4} - \frac{a^2}{3 b^3 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^3} - \frac{a}{2 b^2 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^3} - \frac{a^3}{2 b^4 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^2} - \frac{a^2}{2 b^3 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^2} \\
& - \frac{11 a}{8 b^2 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^2} - \frac{a^4}{b^5 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)} - \frac{a^3}{2 b^4 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)} - \frac{5 a^2}{2 b^3 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)} - \frac{9 a}{8 b^2 \left( \tanh\left(\frac{x}{2}\right) - 1 \right)} \\
& + \frac{a^5 \ln\left(\tanh\left(\frac{x}{2}\right) - 1\right)}{b^6} + \frac{5 a^3 \ln\left(\tanh\left(\frac{x}{2}\right) - 1\right)}{2 b^4} + \frac{15 a \ln\left(\tanh\left(\frac{x}{2}\right) - 1\right)}{8 b^2} - \frac{15 a \ln\left(\tanh\left(\frac{x}{2}\right) + 1\right)}{8 b^2} + \frac{a}{4 b^2 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^4} \\
& + \frac{a^2}{3 b^3 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^3} - \frac{a}{2 b^2 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^3} + \frac{a^3}{2 b^4 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^2} - \frac{a^2}{2 b^3 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^2} + \frac{11 a}{8 b^2 \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^2} \\
& - \frac{13}{12 b \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^3} + \frac{13}{12 b \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^3} - \frac{1}{5 b \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^5} + \frac{1}{5 b \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^5} - \frac{15}{8 b \left( \tanh\left(\frac{x}{2}\right) - 1 \right)} \\
& + \frac{15}{8 b \left( \tanh\left(\frac{x}{2}\right) + 1 \right)} - \frac{9}{8 b \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^2} - \frac{9}{8 b \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^2} - \frac{1}{2 b \left( \tanh\left(\frac{x}{2}\right) - 1 \right)^4} - \frac{1}{2 b \left( \tanh\left(\frac{x}{2}\right) + 1 \right)^4} \\
& + \frac{2 \operatorname{arctanh}\left(\frac{2 a \tanh\left(\frac{x}{2}\right) - 2 b}{2 \sqrt{a^2 + b^2}}\right)}{\sqrt{a^2 + b^2}} + \frac{6 a^2 \operatorname{arctanh}\left(\frac{2 a \tanh\left(\frac{x}{2}\right) - 2 b}{2 \sqrt{a^2 + b^2}}\right)}{b^2 \sqrt{a^2 + b^2}} + \frac{2 \operatorname{arctanh}\left(\frac{2 a \tanh\left(\frac{x}{2}\right) - 2 b}{2 \sqrt{a^2 + b^2}}\right)}{b^6 \sqrt{a^2 + b^2}} a^6 \\
& + \frac{6 \operatorname{arctanh}\left(\frac{2 a \tanh\left(\frac{x}{2}\right) - 2 b}{2 \sqrt{a^2 + b^2}}\right)}{b^4 \sqrt{a^2 + b^2}} a^4
\end{aligned}$$

Problem 50: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(x)^4}{a + b \sinh(x)} dx$$

Optimal (type 3, 86 leaves, 6 steps):

$$-\frac{a(2a^2+3b^2)x}{2b^4} - \frac{2(a^2+b^2)^{3/2} \operatorname{arctanh}\left(\frac{b-a \tanh\left(\frac{x}{2}\right)}{\sqrt{a^2+b^2}}\right)}{b^4} + \frac{\cosh(x)^3}{3b} + \frac{\cosh(x)(2a^2+2b^2-ab \sinh(x))}{2b^3}$$

Result (type 3, 335 leaves):

$$\begin{aligned} & -\frac{1}{3b \left(\tanh\left(\frac{x}{2}\right) - 1\right)^3} - \frac{a}{2b^2 \left(\tanh\left(\frac{x}{2}\right) - 1\right)^2} - \frac{1}{2b \left(\tanh\left(\frac{x}{2}\right) - 1\right)^2} - \frac{a^2}{b^3 \left(\tanh\left(\frac{x}{2}\right) - 1\right)} - \frac{a}{2b^2 \left(\tanh\left(\frac{x}{2}\right) - 1\right)} - \frac{3}{2b \left(\tanh\left(\frac{x}{2}\right) - 1\right)} \\ & + \frac{a^3 \ln\left(\tanh\left(\frac{x}{2}\right) - 1\right)}{b^4} + \frac{3a \ln\left(\tanh\left(\frac{x}{2}\right) - 1\right)}{2b^2} + \frac{1}{3b \left(\tanh\left(\frac{x}{2}\right) + 1\right)^3} + \frac{a}{2b^2 \left(\tanh\left(\frac{x}{2}\right) + 1\right)^2} - \frac{1}{2b \left(\tanh\left(\frac{x}{2}\right) + 1\right)^2} \\ & + \frac{a^2}{b^3 \left(\tanh\left(\frac{x}{2}\right) + 1\right)} - \frac{a}{2b^2 \left(\tanh\left(\frac{x}{2}\right) + 1\right)} + \frac{3}{2b \left(\tanh\left(\frac{x}{2}\right) + 1\right)} - \frac{a^3 \ln\left(\tanh\left(\frac{x}{2}\right) + 1\right)}{b^4} - \frac{3a \ln\left(\tanh\left(\frac{x}{2}\right) + 1\right)}{2b^2} \\ & + \frac{2 \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2+b^2}}\right)}{b^4 \sqrt{a^2+b^2}} + \frac{4a^2 \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2+b^2}}\right)}{b^2 \sqrt{a^2+b^2}} + \frac{2 \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2+b^2}}\right)}{\sqrt{a^2+b^2}} \end{aligned}$$

Problem 51: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(x)^4}{a+b \sinh(x)} dx$$

Optimal (type 3, 90 leaves, 6 steps):

$$-\frac{2b^4 \operatorname{arctanh}\left(\frac{b-a \tanh\left(\frac{x}{2}\right)}{\sqrt{a^2+b^2}}\right)}{(a^2+b^2)^{5/2}} + \frac{\operatorname{sech}(x)^3 (b+a \sinh(x))}{3(a^2+b^2)} + \frac{\operatorname{sech}(x) (3b^3+a(2a^2+5b^2) \sinh(x))}{3(a^2+b^2)^2}$$

Result (type 3, 181 leaves):

$$-\frac{1}{(a^4+2b^2a^2+b^4) \left(\tanh\left(\frac{x}{2}\right)^2+1\right)^3} \left( 2 \left( (-a^3-2b^2a) \tanh\left(\frac{x}{2}\right)^5 + (-a^2b-2b^3) \tanh\left(\frac{x}{2}\right)^4 + \left(-\frac{2}{3}a^3-\frac{8}{3}b^2a\right) \tanh\left(\frac{x}{2}\right)^3 - 2 \tanh\left(\frac{x}{2}\right)^2 b^3 \right) \right)$$

$$+ \left( -a^3 - 2b^2 a \right) \tanh\left(\frac{x}{2}\right) - \frac{a^2 b}{3} - \frac{4b^3}{3} \Big) + \frac{2b^4 \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2 + b^2}}\right)}{(a^4 + 2b^2 a^2 + b^4) \sqrt{a^2 + b^2}}$$

Problem 52: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(x)^4}{(a + b \sinh(x))^2} dx$$

Optimal (type 3, 84 leaves, 6 steps):

$$\frac{3(2a^2 + b^2)x}{2b^4} - \frac{3 \cosh(x)(2a - b \sinh(x))}{2b^3} - \frac{\cosh(x)^3}{b(a + b \sinh(x))} + \frac{6a \operatorname{arctanh}\left(\frac{b - a \tanh\left(\frac{x}{2}\right)}{\sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{b^4}$$

Result (type 3, 289 leaves):

$$\begin{aligned} & \frac{1}{2b^2 \left(\tanh\left(\frac{x}{2}\right) - 1\right)^2} + \frac{1}{2b^2 \left(\tanh\left(\frac{x}{2}\right) - 1\right)} + \frac{2a}{b^3 \left(\tanh\left(\frac{x}{2}\right) - 1\right)} - \frac{3 \ln\left(\tanh\left(\frac{x}{2}\right) - 1\right) a^2}{b^4} - \frac{3 \ln\left(\tanh\left(\frac{x}{2}\right) - 1\right)}{2b^2} - \frac{1}{2b^2 \left(\tanh\left(\frac{x}{2}\right) + 1\right)^2} \\ & + \frac{1}{2b^2 \left(\tanh\left(\frac{x}{2}\right) + 1\right)} - \frac{2a}{b^3 \left(\tanh\left(\frac{x}{2}\right) + 1\right)} + \frac{3 \ln\left(\tanh\left(\frac{x}{2}\right) + 1\right) a^2}{b^4} + \frac{3 \ln\left(\tanh\left(\frac{x}{2}\right) + 1\right)}{2b^2} + \frac{2a \tanh\left(\frac{x}{2}\right)}{b^2 \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)} \\ & + \frac{2 \tanh\left(\frac{x}{2}\right)}{\left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right) a} + \frac{2a^2}{b^3 \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)} + \frac{2}{b \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)} \\ & - \frac{6a \sqrt{a^2 + b^2} \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2 + b^2}}\right)}{b^4} \end{aligned}$$

Problem 55: Result more than twice size of optimal antiderivative.

$$\int \frac{\tanh(x)^4}{1 + \sinh(x)} dx$$

Optimal (type 3, 24 leaves, 6 steps):

$$-\operatorname{sech}(x) + \frac{2 \operatorname{sech}(x)^3}{3} - \frac{\operatorname{sech}(x)^5}{5} - \frac{I \tanh(x)^5}{5}$$

Result(type 3, 92 leaves):

$$\frac{I}{3 \left( \tanh\left(\frac{x}{2}\right) + I \right)^3} - \frac{2I}{5 \left( \tanh\left(\frac{x}{2}\right) + I \right)^5} - \frac{3I}{8 \left( \tanh\left(\frac{x}{2}\right) + I \right)} + \frac{1}{\left( \tanh\left(\frac{x}{2}\right) + I \right)^4} + \frac{1}{2 \left( \tanh\left(\frac{x}{2}\right) + I \right)^2} + \frac{3I}{8 \left( \tanh\left(\frac{x}{2}\right) - I \right)}$$

$$+ \frac{I}{6 \left( \tanh\left(\frac{x}{2}\right) - I \right)^3} + \frac{1}{4 \left( \tanh\left(\frac{x}{2}\right) - I \right)^2}$$

Problem 56: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{coth}(x)^6}{I + \sinh(x)} dx$$

Optimal(type 3, 27 leaves, 6 steps):

$$-\frac{3 \operatorname{arctanh}(\cosh(x))}{8} + \frac{I \operatorname{coth}(x)^5}{5} - \frac{3 \operatorname{coth}(x) \operatorname{csch}(x)}{8} - \frac{\operatorname{coth}(x)^3 \operatorname{csch}(x)}{4}$$

Result(type 3, 92 leaves):

$$\frac{I \tanh\left(\frac{x}{2}\right)}{16} + \frac{I \tanh\left(\frac{x}{2}\right)^5}{160} + \frac{\tanh\left(\frac{x}{2}\right)^4}{64} + \frac{I \tanh\left(\frac{x}{2}\right)^3}{32} + \frac{\tanh\left(\frac{x}{2}\right)^2}{8} + \frac{I}{160 \tanh\left(\frac{x}{2}\right)^5} - \frac{1}{64 \tanh\left(\frac{x}{2}\right)^4} + \frac{3 \ln\left(\tanh\left(\frac{x}{2}\right)\right)}{8} - \frac{1}{8 \tanh\left(\frac{x}{2}\right)^2}$$

$$+ \frac{I}{32 \tanh\left(\frac{x}{2}\right)^3} + \frac{I}{16 \tanh\left(\frac{x}{2}\right)}$$

Problem 57: Result more than twice size of optimal antiderivative.

$$\int \frac{\tanh(x)^2}{(I + \sinh(x))^2} dx$$

Optimal(type 3, 27 leaves, 10 steps):

$$\frac{2I \operatorname{sech}(x)^3}{3} - \frac{2I \operatorname{sech}(x)^5}{5} - \frac{\tanh(x)^3}{3} + \frac{2 \tanh(x)^5}{5}$$

Result(type 3, 69 leaves):

$$\frac{2I}{\left( \tanh\left(\frac{x}{2}\right) + I \right)^4} - \frac{I}{2 \left( \tanh\left(\frac{x}{2}\right) + I \right)^2} + \frac{4}{5 \left( \tanh\left(\frac{x}{2}\right) + I \right)^5} - \frac{5}{3 \left( \tanh\left(\frac{x}{2}\right) + I \right)^3} - \frac{1}{4 \left( \tanh\left(\frac{x}{2}\right) + I \right)} + \frac{1}{4 \left( \tanh\left(\frac{x}{2}\right) - I \right)}$$

Problem 58: Result more than twice size of optimal antiderivative.

$$\int \frac{\tanh(x)}{(1 + \sinh(x))^2} dx$$

Optimal(type 3, 26 leaves, 4 steps):

$$-\frac{\operatorname{Iarctan}(\sinh(x))}{4} - \frac{1}{4(1 + \sinh(x))^2} - \frac{\operatorname{I}}{4(1 + \sinh(x))}$$

Result(type 3, 65 leaves):

$$\frac{2\operatorname{I}}{\left(\tanh\left(\frac{x}{2}\right) + \operatorname{I}\right)^3} - \frac{\operatorname{I}}{2\left(\tanh\left(\frac{x}{2}\right) + \operatorname{I}\right)} + \frac{1}{\left(\tanh\left(\frac{x}{2}\right) + \operatorname{I}\right)^4} - \frac{3}{2\left(\tanh\left(\frac{x}{2}\right) + \operatorname{I}\right)^2} + \frac{\ln\left(\tanh\left(\frac{x}{2}\right) + \operatorname{I}\right)}{4} - \frac{\ln\left(\tanh\left(\frac{x}{2}\right) - \operatorname{I}\right)}{4}$$

Problem 59: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{coth}(x)^4}{(1 + \sinh(x))^2} dx$$

Optimal(type 3, 24 leaves, 9 steps):

$$-\operatorname{Iarctanh}(\cosh(x)) - 2\operatorname{coth}(x) + \frac{\operatorname{coth}(x)^3}{3} + \operatorname{Icoth}(x)\operatorname{csch}(x)$$

Result(type 3, 57 leaves):

$$-\frac{7\tanh\left(\frac{x}{2}\right)}{8} + \frac{\tanh\left(\frac{x}{2}\right)^3}{24} - \frac{\operatorname{I}\tanh\left(\frac{x}{2}\right)^2}{4} + \operatorname{I}\ln\left(\tanh\left(\frac{x}{2}\right)\right) + \frac{\operatorname{I}}{4\tanh\left(\frac{x}{2}\right)^2} + \frac{1}{24\tanh\left(\frac{x}{2}\right)^3} - \frac{7}{8\tanh\left(\frac{x}{2}\right)}$$

Problem 63: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{coth}(x)^2}{a + b\sinh(x)} dx$$

Optimal(type 3, 50 leaves, 7 steps):

$$\frac{b\operatorname{arctanh}(\cosh(x))}{a^2} - \frac{\operatorname{coth}(x)}{a} - \frac{2\operatorname{arctanh}\left(\frac{b - a\tanh\left(\frac{x}{2}\right)}{\sqrt{a^2 + b^2}}\right)\sqrt{a^2 + b^2}}{a^2}$$

Result(type 3, 106 leaves):



$$-\frac{\tanh\left(\frac{x}{2}\right)}{2a} - \frac{1}{2a \tanh\left(\frac{x}{2}\right)} - \frac{b \ln\left(\tanh\left(\frac{x}{2}\right)\right)}{a^2} + \frac{2 \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2 + b^2}}\right)}{\sqrt{a^2 + b^2}} + \frac{2 \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2 + b^2}}\right)}{a^2 \sqrt{a^2 + b^2}} b^2$$

Problem 65: Result more than twice size of optimal antiderivative.

$$\int \frac{\tanh(x)}{(a + b \sinh(x))^2} dx$$

Optimal (type 3, 85 leaves, 6 steps):

$$\frac{2ab \arctan(\sinh(x))}{(a^2 + b^2)^2} + \frac{(a^2 - b^2) \ln(\cosh(x))}{(a^2 + b^2)^2} - \frac{(a^2 - b^2) \ln(a + b \sinh(x))}{(a^2 + b^2)^2} + \frac{a}{(a^2 + b^2)(a + b \sinh(x))}$$

Result (type 3, 247 leaves):

$$\frac{2 \ln\left(\tanh\left(\frac{x}{2}\right)^2 + 1\right) a^2}{2a^4 + 4b^2 a^2 + 2b^4} - \frac{2 \ln\left(\tanh\left(\frac{x}{2}\right)^2 + 1\right) b^2}{2a^4 + 4b^2 a^2 + 2b^4} + \frac{8ab \arctan\left(\tanh\left(\frac{x}{2}\right)\right)}{2a^4 + 4b^2 a^2 + 2b^4} + \frac{2 \tanh\left(\frac{x}{2}\right) a^2 b}{(a^2 + b^2)^2 \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)}$$

$$+ \frac{2 \tanh\left(\frac{x}{2}\right) b^3}{(a^2 + b^2)^2 \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)} - \frac{\ln\left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right) a^2}{(a^2 + b^2)^2} + \frac{\ln\left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right) b^2}{(a^2 + b^2)^2}$$

Problem 66: Result more than twice size of optimal antiderivative.

$$\int \frac{\coth(x)^3}{(a + b \sinh(x))^2} dx$$

Optimal (type 3, 74 leaves, 3 steps):

$$\frac{2b \operatorname{csch}(x)}{a^3} - \frac{\operatorname{csch}(x)^2}{2a^2} + \frac{(a^2 + 3b^2) \ln(\sinh(x))}{a^4} - \frac{(a^2 + 3b^2) \ln(a + b \sinh(x))}{a^4} + \frac{a^2 + b^2}{a^3(a + b \sinh(x))}$$

Result (type 3, 183 leaves):

$$-\frac{\tanh\left(\frac{x}{2}\right)^2}{8a^2} - \frac{\tanh\left(\frac{x}{2}\right) b}{a^3} - \frac{1}{8a^2 \tanh\left(\frac{x}{2}\right)^2} + \frac{\ln\left(\tanh\left(\frac{x}{2}\right)\right)}{a^2} + \frac{3 \ln\left(\tanh\left(\frac{x}{2}\right)\right) b^2}{a^4} + \frac{b}{a^3 \tanh\left(\frac{x}{2}\right)} + \frac{2 \tanh\left(\frac{x}{2}\right) b}{a^2 \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)}$$

$$+ \frac{2 \tanh\left(\frac{x}{2}\right) b^3}{a^4 \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)} - \frac{\ln\left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)}{a^2} - \frac{3 \ln\left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right) b^2}{a^4}$$

Problem 67: Result more than twice size of optimal antiderivative.

$$\int \frac{\coth(x)^4}{(a + b \sinh(x))^2} dx$$

Optimal (type 3, 147 leaves, 8 steps):

$$\begin{aligned} & \frac{b(3a^2 + 4b^2) \operatorname{arctanh}(\cosh(x))}{a^5} - \frac{(7a^2 + 12b^2) \coth(x)}{3a^4} + \frac{(a^2 + 2b^2) \coth(x) \operatorname{csch}(x)}{a^3 b} - \frac{\left(3 + \frac{4b^2}{a^2}\right) \coth(x) \operatorname{csch}(x)}{3b(a + b \sinh(x))} - \frac{\coth(x) \operatorname{csch}(x)^2}{3a(a + b \sinh(x))} \\ & - \frac{2(a^2 + 4b^2) \operatorname{arctanh}\left(\frac{b - a \tanh\left(\frac{x}{2}\right)}{\sqrt{a^2 + b^2}}\right) \sqrt{a^2 + b^2}}{a^5} \end{aligned}$$

Result (type 3, 356 leaves):

$$\begin{aligned} & - \frac{\tanh\left(\frac{x}{2}\right)^3}{24a^2} - \frac{\tanh\left(\frac{x}{2}\right)^2 b}{4a^3} - \frac{5 \tanh\left(\frac{x}{2}\right)}{8a^2} - \frac{3 \tanh\left(\frac{x}{2}\right) b^2}{2a^4} - \frac{1}{24 \tanh\left(\frac{x}{2}\right)^3 a^2} - \frac{5}{8a^2 \tanh\left(\frac{x}{2}\right)} - \frac{3b^2}{2a^4 \tanh\left(\frac{x}{2}\right)} + \frac{b}{4 \tanh\left(\frac{x}{2}\right)^2 a^3} \\ & - \frac{3b \ln\left(\tanh\left(\frac{x}{2}\right)\right)}{a^3} - \frac{4b^3 \ln\left(\tanh\left(\frac{x}{2}\right)\right)}{a^5} + \frac{2 \tanh\left(\frac{x}{2}\right) b^2}{a^3 \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)} + \frac{2 \tanh\left(\frac{x}{2}\right) b^4}{a^5 \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)} \\ & + \frac{2b}{a^2 \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)} + \frac{2b^3}{a^4 \left(\tanh\left(\frac{x}{2}\right)^2 a - 2 \tanh\left(\frac{x}{2}\right) b - a\right)} + \frac{2 \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2 + b^2}}\right)}{a\sqrt{a^2 + b^2}} \\ & + \frac{10 \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2 + b^2}}\right) b^2}{a^3 \sqrt{a^2 + b^2}} + \frac{8 \operatorname{arctanh}\left(\frac{2a \tanh\left(\frac{x}{2}\right) - 2b}{2\sqrt{a^2 + b^2}}\right) b^4}{a^5 \sqrt{a^2 + b^2}} \end{aligned}$$

Problem 70: Unable to integrate problem.

$$\int \frac{x^2}{a + b \sinh(x)^2} dx$$

Optimal (type 4, 261 leaves, 11 steps):

$$\frac{x^2 \ln\left(1 + \frac{b e^{2x}}{2a - b - 2\sqrt{a}\sqrt{a-b}}\right)}{2\sqrt{a}\sqrt{a-b}} - \frac{x^2 \ln\left(1 + \frac{b e^{2x}}{2a - b + 2\sqrt{a}\sqrt{a-b}}\right)}{2\sqrt{a}\sqrt{a-b}} + \frac{x \operatorname{polylog}\left(2, -\frac{b e^{2x}}{2a - b - 2\sqrt{a}\sqrt{a-b}}\right)}{2\sqrt{a}\sqrt{a-b}} - \frac{x \operatorname{polylog}\left(2, -\frac{b e^{2x}}{2a - b + 2\sqrt{a}\sqrt{a-b}}\right)}{2\sqrt{a}\sqrt{a-b}} - \frac{\operatorname{polylog}\left(3, -\frac{b e^{2x}}{2a - b - 2\sqrt{a}\sqrt{a-b}}\right)}{4\sqrt{a}\sqrt{a-b}} + \frac{\operatorname{polylog}\left(3, -\frac{b e^{2x}}{2a - b + 2\sqrt{a}\sqrt{a-b}}\right)}{4\sqrt{a}\sqrt{a-b}}$$

Result (type 8, 16 leaves):

$$\int \frac{x^2}{a + b \sinh(x)^2} dx$$

Problem 71: Result is not expressed in closed-form.

$$\int \frac{x}{a + b \sinh(x)^2} dx$$

Optimal (type 4, 171 leaves, 9 steps):

$$\frac{x \ln\left(1 + \frac{b e^{2x}}{2a - b - 2\sqrt{a}\sqrt{a-b}}\right)}{2\sqrt{a}\sqrt{a-b}} - \frac{x \ln\left(1 + \frac{b e^{2x}}{2a - b + 2\sqrt{a}\sqrt{a-b}}\right)}{2\sqrt{a}\sqrt{a-b}} + \frac{\operatorname{polylog}\left(2, -\frac{b e^{2x}}{2a - b - 2\sqrt{a}\sqrt{a-b}}\right)}{4\sqrt{a}\sqrt{a-b}} - \frac{\operatorname{polylog}\left(2, -\frac{b e^{2x}}{2a - b + 2\sqrt{a}\sqrt{a-b}}\right)}{4\sqrt{a}\sqrt{a-b}}$$

Result (type 7, 62 leaves):

$$\sum_{R1 = \text{RootOf}(b Z^4 + (4a - 2b) Z^2 + b)} \frac{x \ln\left(\frac{R1 - e^x}{R1}\right) + \operatorname{dilog}\left(\frac{R1 - e^x}{R1}\right)}{R1^2 b + 2a - b}$$

Problem 73: Unable to integrate problem.

$$\int \sinh(a + b \ln(cx^n))^2 dx$$

Optimal (type 3, 88 leaves, 2 steps):

$$\frac{2b^2 n^2 x}{-4b^2 n^2 + 1} - \frac{2bnx \cosh(a + b \ln(cx^n)) \sinh(a + b \ln(cx^n))}{-4b^2 n^2 + 1} + \frac{x \sinh(a + b \ln(cx^n))^2}{-4b^2 n^2 + 1}$$

Result(type 8, 15 leaves):

$$\int \sinh(a + b \ln(cx^n))^2 dx$$

Problem 79: Result more than twice size of optimal antiderivative.

$$\int \sinh\left(\frac{bx+a}{dx+c}\right) dx$$

Optimal(type 4, 101 leaves, 5 steps):

$$\frac{(-ad+cb) \operatorname{Chi}\left(\frac{-ad+cb}{d(dx+c)}\right) \cosh\left(\frac{b}{d}\right)}{d^2} - \frac{(-ad+cb) \operatorname{Shi}\left(\frac{-ad+cb}{d(dx+c)}\right) \sinh\left(\frac{b}{d}\right)}{d^2} + \frac{(dx+c) \sinh\left(\frac{bx+a}{dx+c}\right)}{d}$$

Result(type 4, 346 leaves):

$$\begin{aligned} & -\frac{e^{-\frac{bx+a}{dx+c}} a}{2\left(\frac{da}{dx+c} - \frac{cb}{dx+c}\right)} + \frac{e^{-\frac{bx+a}{dx+c}} cb}{2d\left(\frac{da}{dx+c} - \frac{cb}{dx+c}\right)} + \frac{e^{-\frac{b}{d}} \operatorname{Ei}_1\left(\frac{ad-cb}{d(dx+c)}\right) a}{2d} - \frac{e^{-\frac{b}{d}} \operatorname{Ei}_1\left(\frac{ad-cb}{d(dx+c)}\right) cb}{2d^2} + \frac{\frac{bx+a}{d} e^{\frac{bx+a}{dx+c}} xa}{2(ad-cb)} - \frac{e^{\frac{bx+a}{dx+c}} xcb}{2(ad-cb)} \\ & + \frac{\frac{bx+a}{e^{\frac{bx+a}{dx+c}}} ca}{2(ad-cb)} - \frac{\frac{bx+a}{e^{\frac{bx+a}{dx+c}}} c^2 b}{2d(ad-cb)} + \frac{e^{\frac{b}{d}} \operatorname{Ei}_1\left(-\frac{ad-cb}{d(dx+c)}\right) a}{2d} - \frac{e^{\frac{b}{d}} \operatorname{Ei}_1\left(-\frac{ad-cb}{d(dx+c)}\right) cb}{2d^2} \end{aligned}$$

Problem 80: Result more than twice size of optimal antiderivative.

$$\int \sinh\left(e + \frac{f(bx+a)}{dx+c}\right)^2 dx$$

Optimal(type 4, 131 leaves, 7 steps):

$$\begin{aligned} & -\frac{(-ad+cb) f \cosh\left(2e + \frac{2bf}{d}\right) \operatorname{Shi}\left(\frac{2(-ad+cb)f}{d(dx+c)}\right)}{d^2} + \frac{(-ad+cb) f \operatorname{Chi}\left(\frac{2(-ad+cb)f}{d(dx+c)}\right) \sinh\left(2e + \frac{2bf}{d}\right)}{d^2} \\ & + \frac{(dx+c) \sinh\left(\frac{bfx+dex+af+ce}{dx+c}\right)^2}{d} \end{aligned}$$

Result(type 4, 467 leaves):

$$\begin{aligned} & -\frac{x}{2} + \frac{fe^{-\frac{2(bfx+dex+af+ce)}{dx+c}} a}{4\left(\frac{dfa}{dx+c} - \frac{fcb}{dx+c}\right)} - \frac{fe^{-\frac{2(bfx+dex+af+ce)}{dx+c}} cb}{4d\left(\frac{dfa}{dx+c} - \frac{fcb}{dx+c}\right)} - \frac{fe^{-\frac{2(bf+de)}{d}} \operatorname{Ei}_1\left(\frac{2(ad-cb)f}{d(dx+c)}\right) a}{2d} + \frac{fe^{-\frac{2(bf+de)}{d}} \operatorname{Ei}_1\left(\frac{2(ad-cb)f}{d(dx+c)}\right) cb}{2d^2} \end{aligned}$$

$$\begin{aligned}
& + \frac{fe^{\frac{2(bfx+dex+af+ce)}{dx+c}}}{4d} \left( \frac{fa}{dx+c} - \frac{fcb}{d(dx+c)} \right) a - \frac{fe^{\frac{2(bfx+dex+af+ce)}{dx+c}}}{4d^2} \left( \frac{fa}{dx+c} - \frac{fcb}{d(dx+c)} \right) cb \\
& + \frac{fe^{\frac{2(bf+de)}{d}} \operatorname{Ei}_1 \left( -\frac{2(ad-cb)f}{d(dx+c)} - \frac{2(bf+de)}{d} - \frac{2(-bf-de)}{d} \right) a}{2d} \\
& - \frac{fe^{\frac{2(bf+de)}{d}} \operatorname{Ei}_1 \left( -\frac{2(ad-cb)f}{d(dx+c)} - \frac{2(bf+de)}{d} - \frac{2(-bf-de)}{d} \right) cb}{2d^2}
\end{aligned}$$

Problem 83: Result more than twice size of optimal antiderivative.

$$\int e^x \operatorname{csch}(2x) dx$$

Optimal(type 3, 9 leaves, 5 steps):

$$\arctan(e^x) - \operatorname{arctanh}(e^x)$$

Result(type 3, 33 leaves):

$$\frac{\operatorname{I} \ln(e^x + 1)}{2} - \frac{\operatorname{I} \ln(e^x - 1)}{2} - \frac{\ln(1 + e^x)}{2} + \frac{\ln(e^x - 1)}{2}$$

Problem 85: Unable to integrate problem.

$$\int F^{c(bx+a)} \operatorname{csch}(ex+d)^3 dx$$

Optimal(type 5, 114 leaves, 2 steps):

$$\begin{aligned}
& - \frac{F^{c(bx+a)} \operatorname{coth}(ex+d) \operatorname{csch}(ex+d)}{2e} - \frac{bc F^{c(bx+a)} \operatorname{csch}(ex+d) \ln(F)}{2e^2} \\
& + \frac{e^{ex+d} F^{c(bx+a)} \operatorname{hypergeom} \left( \left[ 1, \frac{e+bc \ln(F)}{2e} \right], \left[ \frac{3}{2} + \frac{bc \ln(F)}{2e} \right], e^{2ex+2d} \right) (e - bc \ln(F))}{e^2}
\end{aligned}$$

Result(type 8, 20 leaves):

$$\int F^{c(bx+a)} \operatorname{csch}(ex+d)^3 dx$$

Test results for the 140 problems in "6.1.7 hyper^m (a+b sinh^n)^p.txt"

Problem 11: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(dx+c)^6}{a+b \sinh(dx+c)^2} dx$$

Optimal(type 3, 107 leaves, 6 steps):

$$\frac{(8a^2 + 4ab + 3b^2)x}{8b^3} - \frac{(4a + 3b) \cosh(dx + c) \sinh(dx + c)}{8b^2 d} + \frac{\cosh(dx + c) \sinh(dx + c)^3}{4bd} - \frac{a^5 / 2 \operatorname{arctanh}\left(\frac{\sqrt{a-b} \tanh(dx + c)}{\sqrt{a}}\right)}{b^3 d \sqrt{a-b}}$$

Result (type 3, 669 leaves):

$$\begin{aligned} & \frac{a^3 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{db^3 \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} + \frac{a^3 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{db^2 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} - \frac{a^3 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{db^3 \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} \\ & + \frac{a^3 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{db^2 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} + \frac{1}{4db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^4} + \frac{1}{2db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^3} \\ & - \frac{a}{2db^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^2} - \frac{1}{8db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^2} - \frac{a}{2db^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} - \frac{3}{8db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} \\ & - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right) a^2}{db^3} - \frac{a \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)}{2db^2} - \frac{3 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)}{8db} - \frac{1}{4db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^4} \\ & + \frac{1}{2db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^3} - \frac{a}{2db^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)} - \frac{3}{8db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)} + \frac{1}{8db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2} \\ & + \frac{a}{2db^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2} + \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right) a^2}{db^3} + \frac{a \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)}{2db^2} + \frac{3 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)}{8db} \end{aligned}$$

Problem 12: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{a + b \sinh(dx + c)^2} dx$$

Optimal (type 3, 32 leaves, 2 steps):

$$\frac{\operatorname{arctanh}\left(\frac{\sqrt{a-b} \tanh(dx + c)}{\sqrt{a}}\right)}{d\sqrt{a} \sqrt{a-b}}$$

Result (type 3, 266 leaves):

$$\begin{aligned}
& - \frac{\arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{d\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} - \frac{\arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right) b}{d\sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} + \frac{\operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{d\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} \\
& - \frac{\operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right) b}{d\sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}
\end{aligned}$$

Problem 13: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(dx+c)^4}{a+b \sinh(dx+c)^2} dx$$

Optimal (type 3, 68 leaves, 4 steps):

$$\frac{(a+b) \operatorname{coth}(dx+c)}{a^2 d} - \frac{\operatorname{coth}(dx+c)^3}{3 a d} + \frac{b^2 \operatorname{arctanh}\left(\frac{\sqrt{a-b} \tanh(dx+c)}{\sqrt{a}}\right)}{a^5 / 2 d \sqrt{a-b}}$$

Result (type 3, 400 leaves):

$$\begin{aligned}
& - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{24 da} + \frac{3 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{8 da} + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b}{2 da^2} - \frac{b^2 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{da^2 \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} \\
& - \frac{b^3 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{da^2 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} + \frac{b^2 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{da^2 \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} \\
& - \frac{b^3 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{da^2 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} - \frac{1}{24 d \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 a} + \frac{3}{8 da \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)} + \frac{b}{2 d \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a^2}
\end{aligned}$$

Problem 14: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(dx+c)^6}{a+b \sinh(dx+c)^2} dx$$

Optimal (type 3, 98 leaves, 4 steps):

$$-\frac{(a^2+ab+b^2) \operatorname{coth}(dx+c)}{a^3 d} + \frac{(2a+b) \operatorname{coth}(dx+c)^3}{3a^2 d} - \frac{\operatorname{coth}(dx+c)^5}{5ad} - \frac{b^3 \operatorname{arctanh}\left(\frac{\sqrt{a-b} \tanh(dx+c)}{\sqrt{a}}\right)}{a^7 / 2 d \sqrt{a-b}}$$

Result (type 3, 518 leaves):

$$\begin{aligned} & -\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^5}{160 da} + \frac{5 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{96 da} + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 b}{24 da^2} - \frac{5 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{16 da} - \frac{3 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b}{8 da^2} - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^2}{2 da^3} \\ & + \frac{b^3 \operatorname{arctan}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b) a}}\right)}{da^3 \sqrt{(2\sqrt{-(a-b)b} - a + 2b) a}} + \frac{b^4 \operatorname{arctan}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b) a}}\right)}{da^3 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b) a}} \\ & - \frac{b^3 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b) a}}\right)}{da^3 \sqrt{(2\sqrt{-(a-b)b} + a - 2b) a}} + \frac{b^4 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b) a}}\right)}{da^3 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b) a}} - \frac{1}{160 da \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^5} \\ & + \frac{5}{96 d \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 a} + \frac{b}{24 da^2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3} - \frac{5}{16 da \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)} - \frac{3b}{8 d \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a^2} - \frac{b^2}{2 da^3 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)} \end{aligned}$$

Problem 15: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(dx+c)}{(a+b \sinh(dx+c)^2)^2} dx$$

Optimal (type 3, 69 leaves, 3 steps):

$$\frac{\cosh(dx+c)}{2(a-b)d(a-b+b \cosh(dx+c)^2)} + \frac{\operatorname{arctan}\left(\frac{\cosh(dx+c)\sqrt{b}}{\sqrt{a-b}}\right)}{2(a-b)^3 / 2 d \sqrt{b}}$$

Result (type 3, 255 leaves):

$$-\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) (a-b)}$$



$$\begin{aligned}
& + \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 b}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) (a-b) a} \\
& + \frac{1}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) (a-b)} + \frac{\arctan\left(\frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 a + 4 b}{4 \sqrt{ab - b^2}}\right)}{2 d (a-b) \sqrt{ab - b^2}}
\end{aligned}$$

Problem 16: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(dx+c)}{(a+b \sinh(dx+c))^2} dx$$

Optimal (type 3, 98 leaves, 5 steps):

$$-\frac{\operatorname{arctanh}(\cosh(dx+c))}{a^2 d} - \frac{b \cosh(dx+c)}{2 a (a-b) d (a-b+b \cosh(dx+c)^2)} - \frac{(3 a-2 b) \arctan\left(\frac{\cosh(dx+c) \sqrt{b}}{\sqrt{a-b}}\right) \sqrt{b}}{2 a^2 (a-b)^{3/2} d}$$

Result (type 3, 349 leaves):

$$\begin{aligned}
& \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 b}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) (a-b) a} \\
& - \frac{2 b^2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{d a^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) (a-b)} \\
& - \frac{b}{d a \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) (a-b)} - \frac{3 b \arctan\left(\frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 a + 4 b}{4 \sqrt{ab - b^2}}\right)}{2 d a (a-b) \sqrt{ab - b^2}} \\
& + \frac{b^2 \arctan\left(\frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 a + 4 b}{4 \sqrt{ab - b^2}}\right)}{d a^2 (a-b) \sqrt{ab - b^2}} + \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)}{d a^2}
\end{aligned}$$

Problem 17: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(dx+c)^3}{(a+b \sinh(dx+c))^2} dx$$

Optimal(type 3, 145 leaves, 6 steps):

$$\frac{(5a-4b)b^{3/2} \arctan\left(\frac{\cosh(dx+c)\sqrt{b}}{\sqrt{a-b}}\right)}{2a^3(a-b)^{3/2}d} + \frac{(a+4b) \operatorname{arctanh}(\cosh(dx+c))}{2a^3d} - \frac{(a-2b)b \cosh(dx+c)}{2a^2(a-b)d(a-b+b \cosh(dx+c)^2)}$$

$$- \frac{\operatorname{coth}(dx+c) \operatorname{csch}(dx+c)}{2ad(a-b+b \cosh(dx+c)^2)}$$

Result(type 3, 414 leaves):

$$\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{8da^2} - \frac{b^2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{da^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) (a-b)}$$

$$+ \frac{2b^3 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{da^3 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) (a-b)}$$

$$+ \frac{b^2}{da^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) (a-b)} + \frac{5b^2 \arctan\left(\frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2a + 4b}{4\sqrt{ab-b^2}}\right)}{2da^2(a-b)\sqrt{ab-b^2}}$$

$$- \frac{2b^3 \arctan\left(\frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2a + 4b}{4\sqrt{ab-b^2}}\right)}{da^3(a-b)\sqrt{ab-b^2}} - \frac{1}{8da^2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)}{2da^2} - \frac{2 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right) b}{da^3}$$

Problem 18: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(dx+c)}{(a+b \sinh(dx+c))^3} dx$$

Optimal(type 3, 152 leaves, 6 steps):

$$- \frac{\operatorname{arctanh}(\cosh(dx+c))}{a^3d} - \frac{b \cosh(dx+c)}{4a(a-b)d(a-b+b \cosh(dx+c)^2)^2} - \frac{(7a-4b)b \cosh(dx+c)}{8a^2(a-b)^2d(a-b+b \cosh(dx+c)^2)}$$

$$\frac{(15a^2 - 20ab + 8b^2) \arctan\left(\frac{\cosh(dx+c)\sqrt{b}}{\sqrt{a-b}}\right)\sqrt{b}}{8a^3(a-b)^{5/2}d}$$

Result (type 3, 1144 leaves):

$$\begin{aligned} & \frac{9b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6}{4d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)^2 (a^2 - 2ab + b^2)} \\ & - \frac{7b^2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6}{da \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)^2 (a^2 - 2ab + b^2)} \\ & + \frac{4b^3 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6}{da^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)^2 (a^2 - 2ab + b^2)} \\ & - \frac{27b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4}{4d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)^2 (a^2 - 2ab + b^2)} \\ & + \frac{45b^2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4}{2da \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)^2 (a^2 - 2ab + b^2)} \\ & - \frac{30b^3 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4}{da^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)^2 (a^2 - 2ab + b^2)} \\ & + \frac{12b^4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4}{da^3 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)^2 (a^2 - 2ab + b^2)} \\ & + \frac{27b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{4d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)^2 (a^2 - 2ab + b^2)} \end{aligned}$$

$$\begin{aligned}
& - \frac{17 b^2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{d a \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a\right)^2 (a^2 - 2 a b + b^2)} \\
& + \frac{8 b^3 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{d a^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a\right)^2 (a^2 - 2 a b + b^2)} \\
& - \frac{9 b}{4 d \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a\right)^2 (a^2 - 2 a b + b^2)} \\
& + \frac{3 b^2}{2 d a \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a\right)^2 (a^2 - 2 a b + b^2)} \\
& - \frac{15 b \arctan\left(\frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 a + 4 b}{4 \sqrt{a b - b^2}}\right)}{8 d a (a^2 - 2 a b + b^2) \sqrt{a b - b^2}} + \frac{5 b^2 \arctan\left(\frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 a + 4 b}{4 \sqrt{a b - b^2}}\right)}{2 d a^2 (a^2 - 2 a b + b^2) \sqrt{a b - b^2}} \\
& - \frac{b^3 \arctan\left(\frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a - 2 a + 4 b}{4 \sqrt{a b - b^2}}\right)}{d a^3 (a^2 - 2 a b + b^2) \sqrt{a b - b^2}} + \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right)}{d a^3}
\end{aligned}$$

Problem 19: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(dx+c)^4}{(a+b \sinh(dx+c)^2)^3} dx$$

Optimal (type 3, 241 leaves, 6 steps):

$$\begin{aligned}
& \frac{b^2 (48 a^2 - 80 a b + 35 b^2) \operatorname{arctanh}\left(\frac{\sqrt{a-b} \tanh(dx+c)}{\sqrt{a}}\right)}{8 a^9 / 2 (a-b)^5 / 2 d} + \frac{(8 a^3 - 4 a^2 b - 45 b^2 a + 35 b^3) \operatorname{coth}(dx+c)}{8 a^4 (a-b)^2 d} - \frac{(8 a^2 - 52 a b + 35 b^2) \operatorname{coth}(dx+c)^3}{24 a^3 (a-b)^2 d} \\
& - \frac{b \operatorname{csch}(dx+c)^3 \operatorname{sech}(dx+c)^3}{4 a (a-b) d (a - (a-b) \tanh(dx+c)^2)^2} - \frac{(10 a - 7 b) b \operatorname{csch}(dx+c)^3 \operatorname{sech}(dx+c)}{8 a^2 (a-b)^2 d (a - (a-b) \tanh(dx+c)^2)^2}
\end{aligned}$$

Result (type ?, 4745 leaves): Display of huge result suppressed!

Problem 20: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(1 - \sinh(x)^2)^2} dx$$

Optimal(type 3, 29 leaves, 4 steps):

$$\frac{\cosh(x) \sinh(x)}{4(1 - \sinh(x)^2)} + \frac{3 \operatorname{arctanh}(\sqrt{2} \tanh(x)) \sqrt{2}}{8}$$

Result(type 3, 91 leaves):

$$\frac{-\frac{\tanh\left(\frac{x}{2}\right)}{4} + \frac{1}{4}}{\tanh\left(\frac{x}{2}\right)^2 + 2 \tanh\left(\frac{x}{2}\right) - 1} + \frac{3\sqrt{2} \operatorname{arctanh}\left(\frac{\left(2 \tanh\left(\frac{x}{2}\right) + 2\right)\sqrt{2}}{4}\right)}{8} - \frac{-\frac{\tanh\left(\frac{x}{2}\right)}{4} - \frac{1}{4}}{\tanh\left(\frac{x}{2}\right)^2 - 2 \tanh\left(\frac{x}{2}\right) - 1} + \frac{3\sqrt{2} \operatorname{arctanh}\left(\frac{\left(2 \tanh\left(\frac{x}{2}\right) - 2\right)\sqrt{2}}{4}\right)}{8}$$

Problem 21: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(1 - \sinh(x)^2)^3} dx$$

Optimal(type 3, 45 leaves, 5 steps):

$$\frac{\cosh(x) \sinh(x)}{8(1 - \sinh(x)^2)^2} + \frac{9 \cosh(x) \sinh(x)}{32(1 - \sinh(x)^2)} + \frac{19 \operatorname{arctanh}(\sqrt{2} \tanh(x)) \sqrt{2}}{64}$$

Result(type 3, 123 leaves):

$$\frac{-\frac{13 \tanh\left(\frac{x}{2}\right)^3}{8} - \frac{11 \tanh\left(\frac{x}{2}\right)^2}{8} + \frac{31 \tanh\left(\frac{x}{2}\right)}{8} - \frac{11}{8}}{4 \left( \tanh\left(\frac{x}{2}\right)^2 + 2 \tanh\left(\frac{x}{2}\right) - 1 \right)^2} + \frac{19\sqrt{2} \operatorname{arctanh}\left(\frac{\left(2 \tanh\left(\frac{x}{2}\right) + 2\right)\sqrt{2}}{4}\right)}{64}$$

$$- \frac{-\frac{13 \tanh\left(\frac{x}{2}\right)^3}{8} + \frac{11 \tanh\left(\frac{x}{2}\right)^2}{8} + \frac{31 \tanh\left(\frac{x}{2}\right)}{8} + \frac{11}{8}}{4 \left( \tanh\left(\frac{x}{2}\right)^2 - 2 \tanh\left(\frac{x}{2}\right) - 1 \right)^2} + \frac{19\sqrt{2} \operatorname{arctanh}\left(\frac{\left(2 \tanh\left(\frac{x}{2}\right) - 2\right)\sqrt{2}}{4}\right)}{64}$$

Problem 22: Result more than twice size of optimal antiderivative.

$$\int \sinh(fx + e)^3 \sqrt{a + b \sinh(fx + e)^2} dx$$

Optimal(type 3, 114 leaves, 5 steps):

$$-\frac{(a-b)(a+3b) \operatorname{arctanh}\left(\frac{\cosh(fx+e)\sqrt{b}}{\sqrt{a-b+b\cosh(fx+e)^2}}\right)}{8b^3/2f} + \frac{\cosh(fx+e)(a-b+b\cosh(fx+e)^2)^{3/2}}{4bf}$$

$$-\frac{(a+3b)\cosh(fx+e)\sqrt{a-b+b\cosh(fx+e)^2}}{8bf}$$

Result (type 3, 338 leaves):

$$\frac{1}{16b^5/2\cosh(fx+e)\sqrt{a+b\sinh(fx+e)^2}f} \left( \sqrt{(a+b\sinh(fx+e)^2)\cosh(fx+e)^2} \left( 4\sqrt{b\cosh(fx+e)^4+(a-b)\cosh(fx+e)^2} b^5/2\cosh(fx+e)^2 \right. \right.$$

$$\left. - 10\sqrt{b\cosh(fx+e)^4+(a-b)\cosh(fx+e)^2} b^5/2 + 2a\sqrt{b\cosh(fx+e)^4+(a-b)\cosh(fx+e)^2} b^3/2 \right.$$

$$\left. - \ln\left(\frac{2b\cosh(fx+e)^2+2\sqrt{b\cosh(fx+e)^4+(a-b)\cosh(fx+e)^2}\sqrt{b}+a-b}{2\sqrt{b}}\right) a^2 b \right.$$

$$\left. - 2a \ln\left(\frac{2b\cosh(fx+e)^2+2\sqrt{b\cosh(fx+e)^4+(a-b)\cosh(fx+e)^2}\sqrt{b}+a-b}{2\sqrt{b}}\right) b^2 \right.$$

$$\left. + 3b^3 \ln\left(\frac{2b\cosh(fx+e)^2+2\sqrt{b\cosh(fx+e)^4+(a-b)\cosh(fx+e)^2}\sqrt{b}+a-b}{2\sqrt{b}}\right) \right)$$

Problem 23: Result more than twice size of optimal antiderivative.

$$\int \operatorname{csch}(fx+e)^5 \sqrt{a+b\sinh(fx+e)^2} dx$$

Optimal (type 3, 128 leaves, 5 steps):

$$-\frac{(a-b)(3a+b) \operatorname{arctanh}\left(\frac{\cosh(fx+e)\sqrt{a}}{\sqrt{a-b+b\cosh(fx+e)^2}}\right)}{8a^3/2f} - \frac{(a-b+b\cosh(fx+e)^2)^{3/2} \operatorname{coth}(fx+e) \operatorname{csch}(fx+e)^3}{4af}$$

$$+ \frac{(3a+b) \operatorname{coth}(fx+e) \operatorname{csch}(fx+e) \sqrt{a-b+b\cosh(fx+e)^2}}{8af}$$

Result (type 3, 380 leaves):

$$\frac{1}{16\sinh(fx+e)^4 a^5/2\cosh(fx+e)\sqrt{a+b\sinh(fx+e)^2}f} \left( \sqrt{(a+b\sinh(fx+e)^2)\cosh(fx+e)^2} \left( 6\sqrt{(a+b\sinh(fx+e)^2)\cosh(fx+e)^2} \sinh(fx \right. \right.$$

$$\left. + e)^2 a^5/2 - 3a^3 \ln\left(\frac{(a+b)\cosh(fx+e)^2+2\sqrt{a}\sqrt{b\cosh(fx+e)^4+(a-b)\cosh(fx+e)^2}+a-b}{\sinh(fx+e)^2}\right) \sinh(fx+e)^4 \right.$$

$$\begin{aligned}
& + 2b \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2 + a - b}}{\sinh(fx+e)^2} \right) \sinh(fx+e)^4 a^2 \\
& + \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2 + a - b}}{\sinh(fx+e)^2} \right) b^2 \sinh(fx+e)^4 a \\
& - 2b \sqrt{(a+b \sinh(fx+e)^2) \cosh(fx+e)^2} \sinh(fx+e)^2 a^3 / 2 - 4 \sqrt{(a+b \sinh(fx+e)^2) \cosh(fx+e)^2} a^5 / 2 \Big)
\end{aligned}$$

Problem 24: Result more than twice size of optimal antiderivative.

$$\int \operatorname{csch}(fx+e)^5 (a+b \sinh(fx+e)^2)^3 / 2 \, dx$$

Optimal (type 3, 119 leaves, 5 steps):

$$\begin{aligned}
& - \frac{(a-b+b \cosh(fx+e)^2)^3 / 2 \operatorname{coth}(fx+e) \operatorname{csch}(fx+e)^3}{4f} - \frac{3(a-b)^2 \operatorname{arctanh} \left( \frac{\cosh(fx+e) \sqrt{a}}{\sqrt{a-b+b \cosh(fx+e)^2}} \right)}{8f\sqrt{a}} \\
& + \frac{3(a-b) \operatorname{coth}(fx+e) \operatorname{csch}(fx+e) \sqrt{a-b+b \cosh(fx+e)^2}}{8f}
\end{aligned}$$

Result (type 3, 378 leaves):

$$\begin{aligned}
& \frac{1}{16 \sinh(fx+e)^4 \sqrt{a} \cosh(fx+e) \sqrt{a+b \sinh(fx+e)^2} f} \left( \sqrt{(a+b \sinh(fx+e)^2) \cosh(fx+e)^2} \left( \right. \right. \\
& - 3 \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2 + a - b}}{\sinh(fx+e)^2} \right) \sinh(fx+e)^4 a^2 \\
& + 6ab \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2 + a - b}}{\sinh(fx+e)^2} \right) \sinh(fx+e)^4 \\
& - 3 \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2 + a - b}}{\sinh(fx+e)^2} \right) b^2 \sinh(fx+e)^4 \\
& + 6 \sqrt{(a+b \sinh(fx+e)^2) \cosh(fx+e)^2} \sinh(fx+e)^2 a^3 / 2 - 10b \sqrt{(a+b \sinh(fx+e)^2) \cosh(fx+e)^2} \sinh(fx+e)^2 \sqrt{a} \\
& \left. \left. - 4a^3 / 2 \sqrt{(a+b \sinh(fx+e)^2) \cosh(fx+e)^2} \right) \right)
\end{aligned}$$

Problem 25: Result more than twice size of optimal antiderivative.

$$\int \operatorname{csch}(fx+e)^7 (a+b \sinh(fx+e)^2)^3 / 2 \, dx$$

Optimal(type 3, 179 leaves, 6 steps):

$$\frac{(a-b)^2 (5a+b) \operatorname{arctanh}\left(\frac{\cosh(fx+e)\sqrt{a}}{\sqrt{a-b+b\cosh(fx+e)^2}}\right)}{16a^3/2f} + \frac{(5a+b)(a-b+b\cosh(fx+e)^2)^{3/2} \coth(fx+e) \operatorname{csch}(fx+e)^3}{24af}$$

$$- \frac{(a-b+b\cosh(fx+e)^2)^{5/2} \coth(fx+e) \operatorname{csch}(fx+e)^5}{6af} - \frac{(a-b)(5a+b) \coth(fx+e) \operatorname{csch}(fx+e) \sqrt{a-b+b\cosh(fx+e)^2}}{16af}$$

Result(type 3, 568 leaves):

$$- \frac{1}{96 \sinh(fx+e)^6 a^5/2 \cosh(fx+e) \sqrt{a+b\sinh(fx+e)^2} f} \left( \sqrt{(a+b\sinh(fx+e)^2) \cosh(fx+e)^2} \left( 30a^7/2 \sqrt{(a+b\sinh(fx+e)^2) \cosh(fx+e)^2} \right. \right.$$

$$\sinh(fx+e)^4 - 44b \sqrt{(a+b\sinh(fx+e)^2) \cosh(fx+e)^2} \sinh(fx+e)^4 a^5/2$$

$$- 15a^4 \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2} + a-b}{\sinh(fx+e)^2} \right) \sinh(fx+e)^6$$

$$+ 27a^3 b \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2} + a-b}{\sinh(fx+e)^2} \right) \sinh(fx+e)^6$$

$$- 9 \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2} + a-b}{\sinh(fx+e)^2} \right) b^2 \sinh(fx+e)^6 a^2$$

$$- 3 \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2} + a-b}{\sinh(fx+e)^2} \right) b^3 \sinh(fx+e)^6 a$$

$$- 20a^7/2 \sqrt{(a+b\sinh(fx+e)^2) \cosh(fx+e)^2} \sinh(fx+e)^2 + 6b^2 \sqrt{(a+b\sinh(fx+e)^2) \cosh(fx+e)^2} \sinh(fx+e)^4 a^3/2$$

$$\left. \left. + 28b \sqrt{(a+b\sinh(fx+e)^2) \cosh(fx+e)^2} \sinh(fx+e)^2 a^5/2 + 16a^7/2 \sqrt{(a+b\sinh(fx+e)^2) \cosh(fx+e)^2} \right) \right)$$

Problem 27: Result more than twice size of optimal antiderivative.

$$\int \sqrt{a+b\sinh(x)^2} dx$$

Optimal(type 4, 49 leaves, 2 steps):

$$\frac{-I\sqrt{\cosh(x)^2} \operatorname{EllipticE}\left(I\sinh(x), \sqrt{\frac{b}{a}}\right) \sqrt{a+b\sinh(x)^2}}{\cosh(x) \sqrt{1 + \frac{b\sinh(x)^2}{a}}}$$

Result(type 4, 108 leaves):



$$\frac{\sqrt{\frac{a+b \sinh(x)^2}{a}} \sqrt{\cosh(x)^2} \left( a \operatorname{EllipticF} \left( \sinh(x) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) - b \operatorname{EllipticF} \left( \sinh(x) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) + b \operatorname{EllipticE} \left( \sinh(x) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) \right)}{\sqrt{-\frac{b}{a}} \cosh(x) \sqrt{a+b \sinh(x)^2}}$$

Problem 28: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(fx+e)}{\sqrt{a+b \sinh(fx+e)^2}} dx$$

Optimal (type 3, 36 leaves, 3 steps):

$$\frac{\operatorname{arctanh} \left( \frac{\cosh(fx+e) \sqrt{a}}{\sqrt{a-b+b \cosh(fx+e)^2}} \right)}{f \sqrt{a}}$$

Result (type 3, 112 leaves):

$$\frac{\sqrt{(a+b \sinh(fx+e)^2) \cosh(fx+e)^2} \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2} + a-b}{\sinh(fx+e)^2} \right)}{2\sqrt{a} \cosh(fx+e) \sqrt{a+b \sinh(fx+e)^2} f}$$

Problem 29: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(fx+e)^3}{\sqrt{a+b \sinh(fx+e)^2}} dx$$

Optimal (type 3, 77 leaves, 4 steps):

$$\frac{(a+b) \operatorname{arctanh} \left( \frac{\cosh(fx+e) \sqrt{a}}{\sqrt{a-b+b \cosh(fx+e)^2}} \right)}{2a^{3/2} f} - \frac{\operatorname{coth}(fx+e) \operatorname{csch}(fx+e) \sqrt{a-b+b \cosh(fx+e)^2}}{2af}$$

Result (type 3, 233 leaves):

$$\frac{1}{4 \sinh(fx+e)^2 a^{5/2} \cosh(fx+e) \sqrt{a+b \sinh(fx+e)^2} f} \left( \sqrt{(a+b \sinh(fx+e)^2) \cosh(fx+e)^2} \left( -\ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2} + a-b}{\sinh(fx+e)^2} \right) \sinh(fx+e)^2 a^2 - b \ln \left( \frac{(a+b) \cosh(fx+e)^2 + 2\sqrt{a} \sqrt{b \cosh(fx+e)^4 + (a-b) \cosh(fx+e)^2} + a-b}{\sinh(fx+e)^2} \right) \sinh(fx+e)^2 a \right) \right)$$

$$\left. + 2 a^3 / 2 \sqrt{(a + b \sinh(fx + e)^2) \cosh(fx + e)^2} \right)$$

Problem 35: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(fx + e)^6}{(a + b \sinh(fx + e)^2)^{5/2}} dx$$

Optimal (type 4, 400 leaves, 7 steps):

$$\begin{aligned} & - \frac{a \cosh(fx + e) \sinh(fx + e)^3}{3(a - b) b f (a + b \sinh(fx + e)^2)^{3/2}} - \frac{2a(2a - 3b) \cosh(fx + e) \sinh(fx + e)}{3(a - b)^2 b^2 f \sqrt{a + b \sinh(fx + e)^2}} \\ & - \frac{(8a^2 - 13ab + 3b^2) \sqrt{\frac{1}{1 + \sinh(fx + e)^2}} \sqrt{1 + \sinh(fx + e)^2} \operatorname{EllipticE}\left(\frac{\sinh(fx + e)}{\sqrt{1 + \sinh(fx + e)^2}}, \sqrt{1 - \frac{b}{a}}\right) \operatorname{sech}(fx + e) \sqrt{a + b \sinh(fx + e)^2}}{3(a - b)^2 b^3 f \sqrt{\frac{\operatorname{sech}(fx + e)^2 (a + b \sinh(fx + e)^2)}{a}}} \\ & + \frac{2(2a - 3b) \sqrt{\frac{1}{1 + \sinh(fx + e)^2}} \sqrt{1 + \sinh(fx + e)^2} \operatorname{EllipticF}\left(\frac{\sinh(fx + e)}{\sqrt{1 + \sinh(fx + e)^2}}, \sqrt{1 - \frac{b}{a}}\right) \operatorname{sech}(fx + e) \sqrt{a + b \sinh(fx + e)^2}}{3(a - b)^2 b^2 f \sqrt{\frac{\operatorname{sech}(fx + e)^2 (a + b \sinh(fx + e)^2)}{a}}} \\ & + \frac{(8a^2 - 13ab + 3b^2) \sqrt{a + b \sinh(fx + e)^2} \tanh(fx + e)}{3(a - b)^2 b^3 f} \end{aligned}$$

Result (type 4, 867 leaves):

$$\begin{aligned} & - \frac{1}{3 \sqrt{-\frac{b}{a}} (a + b \sinh(fx + e)^2)^{3/2} (a - b)^2 b^2 \cosh(fx + e) f} \left( \left( 5 \sqrt{-\frac{b}{a}} a^2 b - 7 \sqrt{-\frac{b}{a}} a b^2 \right) \sinh(fx + e) \cosh(fx + e)^4 + \left( 4 \sqrt{-\frac{b}{a}} a^3 \right. \right. \\ & - 11 \sqrt{-\frac{b}{a}} a^2 b + 7 \sqrt{-\frac{b}{a}} a b^2 \left. \right) \cosh(fx + e)^2 \sinh(fx + e) + \sqrt{\cosh(fx + e)^2} \sqrt{\frac{b \cosh(fx + e)^2}{a} + \frac{a - b}{a}} b \left( 4 \operatorname{EllipticF}\left(\sinh(fx + e) \sqrt{-\frac{b}{a}}, \right. \right. \\ & \left. \left. \sqrt{\frac{a}{b}}\right) a^2 - 7 \operatorname{EllipticF}\left(\sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) a b + 3 \operatorname{EllipticF}\left(\sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) b^2 - 8 \operatorname{EllipticE}\left(\sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) a^2 \right. \\ & \left. + 13 \operatorname{EllipticE}\left(\sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) a b - 3 \operatorname{EllipticE}\left(\sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) b^2 \right) \cosh(fx + e)^2 \\ & + 4 \sqrt{\frac{b \cosh(fx + e)^2}{a} + \frac{a - b}{a}} \sqrt{\cosh(fx + e)^2} \operatorname{EllipticF}\left(\sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) a^3 \end{aligned}$$

$$\begin{aligned}
& -11 \sqrt{\frac{b \cosh(fx+e)^2}{a} + \frac{a-b}{a}} \sqrt{\cosh(fx+e)^2} \operatorname{EllipticF}\left(\sinh(fx+e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) a^2 b \\
& +10 \sqrt{\frac{b \cosh(fx+e)^2}{a} + \frac{a-b}{a}} \sqrt{\cosh(fx+e)^2} \operatorname{EllipticF}\left(\sinh(fx+e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) a b^2 \\
& -3 \sqrt{\frac{b \cosh(fx+e)^2}{a} + \frac{a-b}{a}} \sqrt{\cosh(fx+e)^2} \operatorname{EllipticF}\left(\sinh(fx+e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) b^3 \\
& -8 \sqrt{\frac{b \cosh(fx+e)^2}{a} + \frac{a-b}{a}} \sqrt{\cosh(fx+e)^2} \operatorname{EllipticE}\left(\sinh(fx+e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) a^3 \\
& +21 \sqrt{\frac{b \cosh(fx+e)^2}{a} + \frac{a-b}{a}} \sqrt{\cosh(fx+e)^2} \operatorname{EllipticE}\left(\sinh(fx+e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) a^2 b \\
& -16 \sqrt{\frac{b \cosh(fx+e)^2}{a} + \frac{a-b}{a}} \sqrt{\cosh(fx+e)^2} \operatorname{EllipticE}\left(\sinh(fx+e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) a b^2 \\
& +3 \sqrt{\frac{b \cosh(fx+e)^2}{a} + \frac{a-b}{a}} \sqrt{\cosh(fx+e)^2} \operatorname{EllipticE}\left(\sinh(fx+e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}}\right) b^3
\end{aligned}$$

Problem 36: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(fx+e)^2}{(a+b \sinh(fx+e)^2)^{5/2}} dx$$

Optimal (type 4, 277 leaves, 7 steps):

$$\begin{aligned}
& \frac{\cosh(fx+e) \sinh(fx+e)}{3(a-b)f(a+b \sinh(fx+e)^2)^{3/2}} + \frac{(a+b) \cosh(fx+e) \sinh(fx+e)}{3a(a-b)^2 f \sqrt{a+b \sinh(fx+e)^2}} \\
& + \frac{I(a+b) \sqrt{\cos(Ie+Ifx)^2} \operatorname{EllipticE}\left(\sin(Ie+Ifx), \sqrt{\frac{b}{a}}\right) \sqrt{a+b \sinh(fx+e)^2}}{3 \cos(Ie+Ifx) a (a-b)^2 b f \sqrt{1 + \frac{b \sinh(fx+e)^2}{a}}} \\
& - \frac{I \sqrt{\cos(Ie+Ifx)^2} \operatorname{EllipticF}\left(\sin(Ie+Ifx), \sqrt{\frac{b}{a}}\right) \sqrt{1 + \frac{b \sinh(fx+e)^2}{a}}}{3 \cos(Ie+Ifx) (a-b) b f \sqrt{a+b \sinh(fx+e)^2}}
\end{aligned}$$

Result (type 4, 597 leaves):

$$-\frac{1}{3 \sqrt{-\frac{b}{a}} (a+b \sinh(fx+e)^2)^{3/2} a (a-b)^2 \cosh(fx+e) f} \left( \left( -\sqrt{-\frac{b}{a}} a b - \sqrt{-\frac{b}{a}} b^2 \right) \sinh(fx+e) \cosh(fx+e)^4 + \left( -2 \sqrt{-\frac{b}{a}} a^2 + \sqrt{-\frac{b}{a}} a b \right) \right)$$

$$\begin{aligned}
& + \sqrt{-\frac{b}{a} b^2} \cosh(fx + e)^2 \sinh(fx + e) + \sqrt{\frac{b \cosh(fx + e)^2}{a} + \frac{a - b}{a}} \sqrt{\cosh(fx + e)^2} b \left( a \operatorname{EllipticF} \left( \sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) \right. \\
& - \operatorname{EllipticF} \left( \sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) b + \operatorname{EllipticE} \left( \sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) a + \operatorname{EllipticE} \left( \sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) b \left. \right) \cosh(fx + e)^2 \\
& + \sqrt{\frac{b \cosh(fx + e)^2}{a} + \frac{a - b}{a}} \sqrt{\cosh(fx + e)^2} \operatorname{EllipticF} \left( \sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) a^2 \\
& - 2 \sqrt{\frac{b \cosh(fx + e)^2}{a} + \frac{a - b}{a}} \sqrt{\cosh(fx + e)^2} \operatorname{EllipticF} \left( \sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) a b \\
& + \sqrt{\frac{b \cosh(fx + e)^2}{a} + \frac{a - b}{a}} \sqrt{\cosh(fx + e)^2} \operatorname{EllipticF} \left( \sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) b^2 \\
& + \sqrt{\frac{b \cosh(fx + e)^2}{a} + \frac{a - b}{a}} \sqrt{\cosh(fx + e)^2} \operatorname{EllipticE} \left( \sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) a^2 \\
& - \sqrt{\frac{b \cosh(fx + e)^2}{a} + \frac{a - b}{a}} \sqrt{\cosh(fx + e)^2} \operatorname{EllipticE} \left( \sinh(fx + e) \sqrt{-\frac{b}{a}}, \sqrt{\frac{a}{b}} \right) b^2 \Big)
\end{aligned}$$

Problem 39: Unable to integrate problem.

$$\int \sinh(fx + e)^5 (a + b \sinh(fx + e)^2)^p dx$$

Optimal (type 5, 224 leaves, 5 steps):

$$\begin{aligned}
& - \frac{(3a + 2b(2 + p)) \cosh(fx + e) (a - b + b \cosh(fx + e)^2)^{1+p}}{b^2 f (3 + 2p) (5 + 2p)} \\
& + \frac{(3a^2 + 4ab(1 + p) + 4b^2(p^2 + 3p + 2)) \cosh(fx + e) (a - b + b \cosh(fx + e)^2)^p \operatorname{hypergeom} \left( \left[ \frac{1}{2}, -p \right], \left[ \frac{3}{2} \right], -\frac{b \cosh(fx + e)^2}{a - b} \right)}{b^2 f (3 + 2p) (5 + 2p) \left( 1 + \frac{b \cosh(fx + e)^2}{a - b} \right)^p} \\
& + \frac{\cosh(fx + e) (a - b + b \cosh(fx + e)^2)^{1+p} \sinh(fx + e)^2}{bf(5 + 2p)}
\end{aligned}$$

Result (type 8, 25 leaves):

$$\int \sinh(fx + e)^5 (a + b \sinh(fx + e)^2)^p dx$$

Problem 40: Unable to integrate problem.

$$\int \sinh(fx + e) (a + b \sinh(fx + e)^2)^p dx$$

Optimal (type 5, 76 leaves, 3 steps):

$$\frac{\cosh(fx + e) (a - b + b \cosh(fx + e)^2)^p \operatorname{hypergeom}\left(\left[\frac{1}{2}, -p\right], \left[\frac{3}{2}\right], -\frac{b \cosh(fx + e)^2}{a - b}\right)}{f\left(1 + \frac{b \cosh(fx + e)^2}{a - b}\right)^p}$$

Result(type 8, 23 leaves):

$$\int \sinh(fx + e) (a + b \sinh(fx + e)^2)^p dx$$

Problem 64: Result is not expressed in closed-form.

$$\int \frac{1}{a - b \sinh(dx + c)^4} dx$$

Optimal(type 3, 79 leaves, 4 steps):

$$\frac{\operatorname{arctanh}\left(\frac{\sqrt{\sqrt{a} - \sqrt{b}} \tanh(dx + c)}{a^{1/4}}\right)}{2 a^{3/4} d \sqrt{\sqrt{a} - \sqrt{b}}} + \frac{\operatorname{arctanh}\left(\frac{\sqrt{\sqrt{a} + \sqrt{b}} \tanh(dx + c)}{a^{1/4}}\right)}{2 a^{3/4} d \sqrt{\sqrt{a} + \sqrt{b}}}$$

Result(type 7, 101 leaves):

$$\frac{\sum_{R=\operatorname{RootOf}(a Z^8 - 4 a Z^6 + (6 a - 16 b) Z^4 - 4 a Z^2 + a)} (-_R^6 + 3 _R^4 - 3 _R^2 + 1) \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - _R\right)}{4 d \left(-_R^7 a - 3 _R^5 a + 3 _R^3 a - 8 _R^3 b - _R a\right)}$$

Problem 65: Result is not expressed in closed-form.

$$\int \frac{\operatorname{csch}(dx + c)^2}{a - b \sinh(dx + c)^4} dx$$

Optimal(type 3, 99 leaves, 6 steps):

$$-\frac{\operatorname{coth}(dx + c)}{a d} - \frac{\operatorname{arctanh}\left(\frac{\sqrt{\sqrt{a} - \sqrt{b}} \tanh(dx + c)}{a^{1/4}}\right) \sqrt{b}}{2 a^{5/4} d \sqrt{\sqrt{a} - \sqrt{b}}} + \frac{\operatorname{arctanh}\left(\frac{\sqrt{\sqrt{a} + \sqrt{b}} \tanh(dx + c)}{a^{1/4}}\right) \sqrt{b}}{2 a^{5/4} d \sqrt{\sqrt{a} + \sqrt{b}}}$$

Result(type 7, 134 leaves):

$$-\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{2 d a} - \frac{b \left( \sum_{R=\operatorname{RootOf}(a Z^8 - 4 a Z^6 + (6 a - 16 b) Z^4 - 4 a Z^2 + a)} \frac{(_R^4 - _R^2) \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - _R\right)}{d a \left(-_R^7 a - 3 _R^5 a + 3 _R^3 a - 8 _R^3 b - _R a\right)} \right)}{2 d a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}$$

Problem 66: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(dx+c)^7}{(a-b\sinh(dx+c)^4)^2} dx$$

Optimal(type 3, 164 leaves, 5 steps):

$$\begin{aligned} & -\frac{a \cosh(dx+c) (2 - \cosh(dx+c)^2)}{4(a-b)bd(a-b+2b\cosh(dx+c)^2 - b\cosh(dx+c)^4)} + \frac{\arctan\left(\frac{b^{1/4}\cosh(dx+c)}{\sqrt{\sqrt{a}-\sqrt{b}}}\right) (3\sqrt{a}-4\sqrt{b})}{8b^{7/4}d(\sqrt{a}-\sqrt{b})^{3/2}} \\ & -\frac{\operatorname{arctanh}\left(\frac{b^{1/4}\cosh(dx+c)}{\sqrt{\sqrt{a}+\sqrt{b}}}\right) (3\sqrt{a}+4\sqrt{b})}{8b^{7/4}d(\sqrt{a}+\sqrt{b})^{3/2}} \end{aligned}$$

Result(type 3, 1199 leaves):

$$\begin{aligned} & -\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 \sqrt{ab}}{4db^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - \frac{4\sqrt{ab}\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{a} - 2\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1 \right) (a-b)} \\ & + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 \sqrt{ab}}{2dab \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - \frac{4\sqrt{ab}\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{a} - 2\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1 \right) (a-b)} \\ & - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{4db \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - \frac{4\sqrt{ab}\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{a} - 2\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1 \right) (a-b)} \\ & - \frac{1}{4db \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - \frac{4\sqrt{ab}\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{a} - 2\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1 \right) (a-b)} \\ & + \frac{\sqrt{ab}}{4db^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - \frac{4\sqrt{ab}\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2}{a} - 2\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1 \right) (a-b)} \end{aligned}$$

$$\begin{aligned}
& + \frac{3 a \arctan \left( \frac{-2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 a + 4 \sqrt{ab} + 2 a}{4 \sqrt{-ab - \sqrt{ab} a}} \right) \sqrt{ab} - \arctan \left( \frac{-2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 a + 4 \sqrt{ab} + 2 a}{4 \sqrt{-ab - \sqrt{ab} a}} \right) \sqrt{ab}}{8 db^2 (a-b) \sqrt{-ab - \sqrt{ab} a} - 2 db (a-b) \sqrt{-ab - \sqrt{ab} a}} \\
& + \frac{a \arctan \left( \frac{-2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 a + 4 \sqrt{ab} + 2 a}{4 \sqrt{-ab - \sqrt{ab} a}} \right) + \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 \sqrt{ab}}{4 db^2 \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^4 - 2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + \frac{4 \sqrt{ab} \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2}{a} + 1 \right) (a-b)}}{8 db (a-b) \sqrt{-ab - \sqrt{ab} a}} \\
& - \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 \sqrt{ab}}{2 dab \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^4 - 2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + \frac{4 \sqrt{ab} \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2}{a} + 1 \right) (a-b)} \\
& - \frac{4 db \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^4 - 2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + \frac{4 \sqrt{ab} \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2}{a} + 1 \right) (a-b)}{\sqrt{ab}} \\
& - \frac{4 db^2 \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^4 - 2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + \frac{4 \sqrt{ab} \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2}{a} + 1 \right) (a-b)}{1} \\
& - \frac{4 db \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^4 - 2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + \frac{4 \sqrt{ab} \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2}{a} + 1 \right) (a-b)}{3 a \arctan \left( \frac{2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 a + 4 \sqrt{ab} - 2 a}{4 \sqrt{-ab + \sqrt{ab} a}} \right) \sqrt{ab} - \arctan \left( \frac{2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 a + 4 \sqrt{ab} - 2 a}{4 \sqrt{-ab + \sqrt{ab} a}} \right) \sqrt{ab}} \\
& + \frac{8 db^2 (a-b) \sqrt{-ab + \sqrt{ab} a} - 2 db (a-b) \sqrt{-ab + \sqrt{ab} a}}{8 db^2 (a-b) \sqrt{-ab + \sqrt{ab} a} - 2 db (a-b) \sqrt{-ab + \sqrt{ab} a}}
\end{aligned}$$

$$- \frac{a \arctan \left( \frac{2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 a + 4 \sqrt{ab} - 2a}{4 \sqrt{-ab + \sqrt{ab} a}} \right)}{8db(a-b) \sqrt{-ab + \sqrt{ab} a}}$$

Problem 67: Result more than twice size of optimal antiderivative.

$$\int \frac{\sinh(dx+c)^5}{(a-b \sinh(dx+c)^4)^2} dx$$

Optimal(type 3, 167 leaves, 5 steps):

$$\frac{\cosh(dx+c) (a+b-b \cosh(dx+c)^2)}{4(a-b)bd(a-b+2b \cosh(dx+c)^2-b \cosh(dx+c)^4)} - \frac{\arctan \left( \frac{b^{1/4} \cosh(dx+c)}{\sqrt{\sqrt{a}-\sqrt{b}}} \right) (\sqrt{a}-2\sqrt{b})}{8b^{5/4}d\sqrt{a}(\sqrt{a}-\sqrt{b})^{3/2}}$$

$$- \frac{\operatorname{arctanh} \left( \frac{b^{1/4} \cosh(dx+c)}{\sqrt{\sqrt{a}+\sqrt{b}}} \right) (\sqrt{a}+2\sqrt{b})}{8b^{5/4}d\sqrt{a}(\sqrt{a}+\sqrt{b})^{3/2}}$$

Result(type ?, 3169 leaves): Display of huge result suppressed!

Problem 68: Result is not expressed in closed-form.

$$\int \frac{\sinh(dx+c)^8}{(a-b \sinh(dx+c)^4)^2} dx$$

Optimal(type 3, 240 leaves, 14 steps):

$$\frac{x}{b^2} + \frac{a^{1/4} \operatorname{arctanh} \left( \frac{\sqrt{\sqrt{a}-\sqrt{b}} \tanh(dx+c)}{a^{1/4}} \right)}{8b^{3/2}d(\sqrt{a}-\sqrt{b})^{3/2}} - \frac{a^{1/4} \operatorname{arctanh} \left( \frac{\sqrt{\sqrt{a}+\sqrt{b}} \tanh(dx+c)}{a^{1/4}} \right)}{8b^{3/2}d(\sqrt{a}+\sqrt{b})^{3/2}} - \frac{a^{1/4} \operatorname{arctanh} \left( \frac{\sqrt{\sqrt{a}-\sqrt{b}} \tanh(dx+c)}{a^{1/4}} \right)}{2b^2d\sqrt{\sqrt{a}-\sqrt{b}}}$$

$$- \frac{a^{1/4} \operatorname{arctanh} \left( \frac{\sqrt{\sqrt{a}+\sqrt{b}} \tanh(dx+c)}{a^{1/4}} \right)}{2b^2d\sqrt{\sqrt{a}+\sqrt{b}}} - \frac{\tanh(dx+c)}{4(a-b)bd} + \frac{\tanh(dx+c)^5}{4bd(a-2a \tanh(dx+c)^2+(a-b) \tanh(dx+c)^4)}$$

Result(type 7, 573 leaves):

$$- \frac{\ln \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right) - 1 \right)}{db^2} + \frac{\ln \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right) + 1 \right)}{db^2}$$



$$\begin{aligned}
& - \frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^7}{2db \left( a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^8 - 4a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6 + 6 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 16b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - 4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + a \right) (a-b)} \\
& + \frac{5a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^5}{2db \left( a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^8 - 4a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6 + 6 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 16b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - 4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + a \right) (a-b)} \\
& + \frac{5a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{2db \left( a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^8 - 4a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6 + 6 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 16b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - 4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + a \right) (a-b)} \\
& - \frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{2db \left( a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^8 - 4a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6 + 6 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 16b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - 4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + a \right) (a-b)} \\
& + \frac{1}{16db^2} \left( a \left( \sum_{R=\text{RootOf}(aZ^8-4aZ^6+(6a-16b)Z^4-4aZ^2+a)} \frac{((4a-5b)R^6 + (-12a+19b)R^4 + (12a-19b)R^2 - 4a+5b) \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - R\right)}{(a-b)(R^7a - 3R^5a + 3R^3a - 8R^3b - Ra)} \right) \right)
\end{aligned}$$

Problem 69: Result is not expressed in closed-form.

$$\int \frac{\sinh(dx+c)^2}{(a-b \sinh(dx+c)^4)^2} dx$$

Optimal (type 3, 170 leaves, 5 steps):

$$\begin{aligned}
& - \frac{\operatorname{arctanh}\left(\frac{\sqrt{\sqrt{a}-\sqrt{b}} \tanh(dx+c)}{a^{1/4}}\right) (2\sqrt{a}-\sqrt{b})}{8a^{5/4} d (\sqrt{a}-\sqrt{b})^{3/2} \sqrt{b}} + \frac{\operatorname{arctanh}\left(\frac{\sqrt{\sqrt{a}+\sqrt{b}} \tanh(dx+c)}{a^{1/4}}\right) (2\sqrt{a}+\sqrt{b})}{8a^{5/4} d \sqrt{b} (\sqrt{a}+\sqrt{b})^{3/2}} \\
& + \frac{\tanh(dx+c) (a - (a+b) \tanh(dx+c)^2)}{4a(a-b) d (a - 2a \tanh(dx+c)^2 + (a-b) \tanh(dx+c)^4)}
\end{aligned}$$

Result (type 7, 707 leaves):

$$\begin{aligned}
& \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^7}{2d\left(a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^8 - 4a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6 + 6 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 16b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - 4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + a\right) (a-b)} \\
& - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^5}{2d\left(a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^8 - 4a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6 + 6 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 16b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - 4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + a\right) (a-b)} \\
& - \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^5 b}{d\left(a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^8 - 4a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6 + 6 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 16b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - 4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + a\right) a (a-b)} \\
& - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{2d\left(a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^8 - 4a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6 + 6 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 16b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - 4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + a\right) (a-b)} \\
& - \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 b}{d\left(a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^8 - 4a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6 + 6 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 16b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - 4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + a\right) a (a-b)} \\
& + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{2d\left(a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^8 - 4a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^6 + 6 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 16b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 - 4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + a\right) (a-b)} \\
& - \frac{\sum_{R=\text{RootOf}(a Z^8 - 4a Z^6 + (6a - 16b) Z^4 - 4a Z^2 + a)} \frac{(-a R^6 + (11a - 4b) R^4 + (-11a + 4b) R^2 + a) \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - R\right)}{(a-b) (R^7 a - 3 R^5 a + 3 R^3 a - 8 R^3 b - R a)}}{16da}
\end{aligned}$$

Problem 70: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{csch}(dx+c)}{(a-b \sinh(dx+c))^3} dx$$

Optimal (type 3, 487 leaves, 16 steps):

$$\begin{aligned}
& - \frac{\operatorname{arctanh}(\cosh(dx+c))}{a^3 d} - \frac{b \cosh(dx+c) (2 - \cosh(dx+c)^2)}{8a(a-b)d(a-b+2b \cosh(dx+c)^2 - b \cosh(dx+c)^4)^2} \\
& - \frac{b \cosh(dx+c) (2 - \cosh(dx+c)^2)}{4a^2(a-b)d(a-b+2b \cosh(dx+c)^2 - b \cosh(dx+c)^4)} - \frac{b \cosh(dx+c) (11a+b - (5a+b) \cosh(dx+c)^2)}{32a^2(a-b)^2 d(a-b+2b \cosh(dx+c)^2 - b \cosh(dx+c)^4)}
\end{aligned}$$

$$\begin{aligned}
& - \frac{b^{1/4} \arctan\left(\frac{b^{1/4} \cosh(dx+c)}{\sqrt{\sqrt{a}-\sqrt{b}}}\right) (5\sqrt{a}-2\sqrt{b})}{64a^{5/2}d(\sqrt{a}-\sqrt{b})^{5/2}} - \frac{b^{1/4} \arctan\left(\frac{b^{1/4} \cosh(dx+c)}{\sqrt{\sqrt{a}-\sqrt{b}}}\right)}{8a^{5/2}d(\sqrt{a}-\sqrt{b})^{3/2}} + \frac{b^{1/4} \operatorname{arctanh}\left(\frac{b^{1/4} \cosh(dx+c)}{\sqrt{\sqrt{a}+\sqrt{b}}}\right)}{8a^{5/2}d(\sqrt{a}+\sqrt{b})^{3/2}} \\
& + \frac{b^{1/4} \operatorname{arctanh}\left(\frac{b^{1/4} \cosh(dx+c)}{\sqrt{\sqrt{a}+\sqrt{b}}}\right) (5\sqrt{a}+2\sqrt{b})}{64a^{5/2}d(\sqrt{a}+\sqrt{b})^{5/2}} - \frac{b^{1/4} \arctan\left(\frac{b^{1/4} \cosh(dx+c)}{\sqrt{\sqrt{a}-\sqrt{b}}}\right)}{2a^3d\sqrt{\sqrt{a}-\sqrt{b}}} + \frac{b^{1/4} \operatorname{arctanh}\left(\frac{b^{1/4} \cosh(dx+c)}{\sqrt{\sqrt{a}+\sqrt{b}}}\right)}{2a^3d\sqrt{\sqrt{a}+\sqrt{b}}}
\end{aligned}$$

Result(type ?, 8619 leaves): Display of huge result suppressed!

Problem 71: Result is not expressed in closed-form.

$$\int \frac{\sinh(dx+c)^8}{(a-b\sinh(dx+c)^4)^3} dx$$

Optimal(type 3, 263 leaves, 9 steps):

$$\begin{aligned}
& - \frac{\operatorname{arctanh}\left(\frac{\sqrt{\sqrt{a}-\sqrt{b}} \tanh(dx+c)}{a^{1/4}}\right) (2\sqrt{a}-5\sqrt{b})}{64a^{3/4}b^{3/2}d(\sqrt{a}-\sqrt{b})^{5/2}} + \frac{\operatorname{arctanh}\left(\frac{\sqrt{\sqrt{a}+\sqrt{b}} \tanh(dx+c)}{a^{1/4}}\right) (2\sqrt{a}+5\sqrt{b})}{64a^{3/4}b^{3/2}d(\sqrt{a}+\sqrt{b})^{5/2}} - \frac{(a+5b) \tanh(dx+c)}{32a(a-b)^2bd} \\
& - \frac{\tanh(dx+c)^3}{32a(a-b)bd} + \frac{\tanh(dx+c)^9}{8ad(a-2a\tanh(dx+c)^2+(a-b)\tanh(dx+c)^4)^2} - \frac{\operatorname{sech}(dx+c)^2 \tanh(dx+c)^5}{32abd(a-2a\tanh(dx+c)^2+(a-b)\tanh(dx+c)^4)^2}
\end{aligned}$$

Result(type ?, 2235 leaves): Display of huge result suppressed!

Problem 72: Result is not expressed in closed-form.

$$\int \frac{\operatorname{csch}(dx+c)^2}{(a-b\sinh(dx+c)^4)^3} dx$$

Optimal(type 3, 307 leaves, 8 steps):

$$\begin{aligned}
& - \frac{\operatorname{coth}(dx+c)}{a^3d} - \frac{3 \operatorname{arctanh}\left(\frac{\sqrt{\sqrt{a}-\sqrt{b}} \tanh(dx+c)}{a^{1/4}}\right) \sqrt{b} (20a+15b-34\sqrt{a}\sqrt{b})}{64a^{13/4}d(\sqrt{a}-\sqrt{b})^{5/2}} \\
& + \frac{3 \operatorname{arctanh}\left(\frac{\sqrt{\sqrt{a}+\sqrt{b}} \tanh(dx+c)}{a^{1/4}}\right) \sqrt{b} (20a+15b+34\sqrt{a}\sqrt{b})}{64a^{13/4}d(\sqrt{a}+\sqrt{b})^{5/2}} + \frac{b^2 \tanh(dx+c) (a(a+3b) - (a^2+6ab+b^2) \tanh(dx+c)^2)}{8a^2(a-b)^3d(a-2a\tanh(dx+c)^2+(a-b)\tanh(dx+c)^4)^2} \\
& + \frac{b \tanh(dx+c) \left( \frac{2a^2(9a-17b)}{(a-b)^3} - \frac{(18a^2+15ab-13b^2) \tanh(dx+c)^2}{(a-b)^2} \right)}{32a^3d(a-2a\tanh(dx+c)^2+(a-b)\tanh(dx+c)^4)^2}
\end{aligned}$$

Result(type ?, 2746 leaves): Display of huge result suppressed!

Problem 73: Result is not expressed in closed-form.

$$\int \frac{1}{a + b \sinh(x)^5} dx$$

Optimal (type 3, 280 leaves, 17 steps):

$$\begin{aligned} & - \frac{2 (-1)^{9/10} \operatorname{arctanh} \left( \frac{b^{1/5} - (-1)^{9/10} a^{1/5} \tanh \left( \frac{x}{2} \right)}{\sqrt{-(-1)^{4/5} a^{2/5} - b^{2/5}}} \right)}{5 a^{4/5} \sqrt{-(-1)^{4/5} a^{2/5} - b^{2/5}}} - \frac{2 \operatorname{arctanh} \left( \frac{b^{1/5} - a^{1/5} \tanh \left( \frac{x}{2} \right)}{\sqrt{a^{2/5} + b^{2/5}}} \right)}{5 a^{4/5} \sqrt{a^{2/5} + b^{2/5}}} \\ & + \frac{2 (-1)^{1/5} \operatorname{arctanh} \left( \frac{b^{1/5} + (-1)^{1/5} a^{1/5} \tanh \left( \frac{x}{2} \right)}{\sqrt{(-1)^{2/5} a^{2/5} + b^{2/5}}} \right)}{5 a^{4/5} \sqrt{(-1)^{2/5} a^{2/5} + b^{2/5}}} + \frac{2 (-1)^{9/10} \operatorname{arctanh} \left( \frac{(-1)^{9/10} \left( (-1)^{1/5} b^{1/5} + a^{1/5} \tanh \left( \frac{x}{2} \right) \right)}{\sqrt{-(-1)^{4/5} a^{2/5} + (-1)^{1/5} b^{2/5}}} \right)}{5 a^{4/5} \sqrt{-(-1)^{4/5} a^{2/5} + (-1)^{1/5} b^{2/5}}} \\ & + \frac{2 (-1)^{9/10} \operatorname{arctanh} \left( \frac{(-1)^{3/10} \left( b^{1/5} + (-1)^{3/5} a^{1/5} \tanh \left( \frac{x}{2} \right) \right)}{\sqrt{-(-1)^{4/5} a^{2/5} + (-1)^{3/5} b^{2/5}}} \right)}{5 a^{4/5} \sqrt{-(-1)^{4/5} a^{2/5} + (-1)^{3/5} b^{2/5}}} \end{aligned}$$

Result (type 7, 112 leaves):

$$\left( \sum_{R=\text{RootOf}(a Z^{10} - 5 a Z^8 + 10 a Z^6 - 32 b Z^5 - 10 a Z^4 + 5 a Z^2 - a)} \frac{(-R^8 + 4R^6 - 6R^4 + 4R^2 - 1) \ln \left( \tanh \left( \frac{x}{2} \right) - R \right)}{-R^9 a - 4R^7 a + 6R^5 a - 16R^4 b - 4R^3 a + R a} \right) / 5$$

Problem 75: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(x)}{a + a \sinh(x)^2} dx$$

Optimal (type 3, 18 leaves, 3 steps):

$$\frac{\arctan(\sinh(x))}{2a} + \frac{\operatorname{sech}(x) \tanh(x)}{2a}$$

Result (type 3, 49 leaves):

$$- \frac{\tanh \left( \frac{x}{2} \right)^3}{a \left( \tanh \left( \frac{x}{2} \right)^2 + 1 \right)^2} + \frac{\tanh \left( \frac{x}{2} \right)}{a \left( \tanh \left( \frac{x}{2} \right)^2 + 1 \right)^2} + \frac{\arctan \left( \tanh \left( \frac{x}{2} \right) \right)}{a}$$

Problem 76: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(x)^3}{a + a \sinh(x)^2} dx$$

Optimal (type 3, 29 leaves, 4 steps):

$$\frac{3 \arctan(\sinh(x))}{8a} + \frac{3 \operatorname{sech}(x) \tanh(x)}{8a} + \frac{\operatorname{sech}(x)^3 \tanh(x)}{4a}$$

Result (type 3, 93 leaves):

$$-\frac{5 \tanh\left(\frac{x}{2}\right)^7}{4a \left(\tanh\left(\frac{x}{2}\right)^2 + 1\right)^4} + \frac{3 \tanh\left(\frac{x}{2}\right)^5}{4a \left(\tanh\left(\frac{x}{2}\right)^2 + 1\right)^4} - \frac{3 \tanh\left(\frac{x}{2}\right)^3}{4a \left(\tanh\left(\frac{x}{2}\right)^2 + 1\right)^4} + \frac{5 \tanh\left(\frac{x}{2}\right)}{4a \left(\tanh\left(\frac{x}{2}\right)^2 + 1\right)^4} + \frac{3 \arctan\left(\tanh\left(\frac{x}{2}\right)\right)}{4a}$$

Problem 78: Result more than twice size of optimal antiderivative.

$$\int \operatorname{sech}(dx+c)^3 (a+b \sinh(dx+c)^2) dx$$

Optimal (type 3, 38 leaves, 3 steps):

$$\frac{(a+b) \arctan(\sinh(dx+c))}{2d} + \frac{(a-b) \operatorname{sech}(dx+c) \tanh(dx+c)}{2d}$$

Result (type 3, 81 leaves):

$$\frac{a \operatorname{sech}(dx+c) \tanh(dx+c)}{2d} + \frac{a \arctan(e^{dx+c})}{d} - \frac{b \sinh(dx+c)}{d \cosh(dx+c)^2} + \frac{b \operatorname{sech}(dx+c) \tanh(dx+c)}{2d} + \frac{b \arctan(e^{dx+c})}{d}$$

Problem 80: Result more than twice size of optimal antiderivative.

$$\int \operatorname{sech}(dx+c)^3 (a+b \sinh(dx+c)^2)^2 dx$$

Optimal (type 3, 60 leaves, 5 steps):

$$\frac{(a-b)(a+3b) \arctan(\sinh(dx+c))}{2d} + \frac{b^2 \sinh(dx+c)}{d} + \frac{(a-b)^2 \operatorname{sech}(dx+c) \tanh(dx+c)}{2d}$$

Result (type 3, 168 leaves):

$$\frac{a^2 \operatorname{sech}(dx+c) \tanh(dx+c)}{2d} + \frac{a^2 \arctan(e^{dx+c})}{d} - \frac{2ab \sinh(dx+c)}{d \cosh(dx+c)^2} + \frac{ab \operatorname{sech}(dx+c) \tanh(dx+c)}{d} + \frac{2ab \arctan(e^{dx+c})}{d} + \frac{b^2 \sinh(dx+c)^3}{d \cosh(dx+c)^2} + \frac{3b^2 \sinh(dx+c)}{d \cosh(dx+c)^2} - \frac{3b^2 \operatorname{sech}(dx+c) \tanh(dx+c)}{2d} - \frac{3b^2 \arctan(e^{dx+c})}{d}$$

Problem 81: Result more than twice size of optimal antiderivative.

$$\int \operatorname{sech}(dx+c)^6 (a+b \sinh(dx+c)^2)^2 dx$$

Optimal (type 3, 53 leaves, 3 steps):

$$\frac{a^2 \tanh(dx+c)}{d} - \frac{2a(a-b) \tanh(dx+c)^3}{3d} + \frac{(a-b)^2 \tanh(dx+c)^5}{5d}$$

Result(type 3, 157 leaves):

$$\frac{1}{d} \left( a^2 \left( \frac{8}{15} + \frac{\operatorname{sech}(dx+c)^4}{5} + \frac{4 \operatorname{sech}(dx+c)^2}{15} \right) \tanh(dx+c) + 2ab \left( -\frac{\sinh(dx+c)}{4 \cosh(dx+c)^5} \right. \right. \\ \left. \left. + \frac{\left( \frac{8}{15} + \frac{\operatorname{sech}(dx+c)^4}{5} + \frac{4 \operatorname{sech}(dx+c)^2}{15} \right) \tanh(dx+c)}{4} \right) + b^2 \left( -\frac{\sinh(dx+c)^3}{2 \cosh(dx+c)^5} - \frac{3 \sinh(dx+c)}{8 \cosh(dx+c)^5} \right. \right. \\ \left. \left. + \frac{3 \left( \frac{8}{15} + \frac{\operatorname{sech}(dx+c)^4}{5} + \frac{4 \operatorname{sech}(dx+c)^2}{15} \right) \tanh(dx+c)}{8} \right) \right)$$

Problem 83: Result more than twice size of optimal antiderivative.

$$\int \operatorname{sech}(dx+c)^5 (a+b \sinh(dx+c))^3 dx$$

Optimal(type 3, 97 leaves, 6 steps):

$$\frac{3(a-b)(4b^2+(a+b)^2) \arctan(\sinh(dx+c))}{8d} + \frac{b^3 \sinh(dx+c)}{d} + \frac{3(a-b)^2(a+3b) \operatorname{sech}(dx+c) \tanh(dx+c)}{8d} \\ + \frac{(a-b)^3 \operatorname{sech}(dx+c)^3 \tanh(dx+c)}{4d}$$

Result(type 3, 375 leaves):

$$\frac{a^3 \tanh(dx+c) \operatorname{sech}(dx+c)^3}{4d} + \frac{3a^3 \operatorname{sech}(dx+c) \tanh(dx+c)}{8d} + \frac{3a^3 \arctan(e^{dx+c})}{4d} - \frac{a^2 b \sinh(dx+c)}{d \cosh(dx+c)^4} + \frac{a^2 b \tanh(dx+c) \operatorname{sech}(dx+c)^3}{4d} \\ + \frac{3a^2 b \operatorname{sech}(dx+c) \tanh(dx+c)}{8d} + \frac{3a^2 b \arctan(e^{dx+c})}{4d} - \frac{3b^2 a \sinh(dx+c)^3}{d \cosh(dx+c)^4} - \frac{3b^2 a \sinh(dx+c)}{d \cosh(dx+c)^4} + \frac{3b^2 a \tanh(dx+c) \operatorname{sech}(dx+c)^3}{4d} \\ + \frac{9b^2 a \operatorname{sech}(dx+c) \tanh(dx+c)}{8d} + \frac{9b^2 a \arctan(e^{dx+c})}{4d} + \frac{b^3 \sinh(dx+c)^5}{d \cosh(dx+c)^4} + \frac{5b^3 \sinh(dx+c)^3}{d \cosh(dx+c)^4} + \frac{5b^3 \sinh(dx+c)}{d \cosh(dx+c)^4} \\ - \frac{5b^3 \tanh(dx+c) \operatorname{sech}(dx+c)^3}{4d} - \frac{15b^3 \operatorname{sech}(dx+c) \tanh(dx+c)}{8d} - \frac{15b^3 \arctan(e^{dx+c})}{4d}$$

Problem 84: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(dx+c)^7}{a+b \sinh(dx+c)^2} dx$$

Optimal(type 3, 96 leaves, 4 steps):

$$\frac{(a^2 - 3ab + 3b^2) \sinh(dx + c)}{b^3 d} - \frac{(a - 3b) \sinh(dx + c)^3}{3b^2 d} + \frac{\sinh(dx + c)^5}{5bd} - \frac{(a - b)^3 \arctan\left(\frac{\sinh(dx + c) \sqrt{b}}{\sqrt{a}}\right)}{b^{7/2} d \sqrt{a}}$$

Result (type 3, 1655 leaves):

$$\begin{aligned} & \frac{3a^2 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{db^2 \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} - \frac{3a \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{db \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} - \frac{3a^2 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{db^2 \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} \\ & + \frac{3a \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{db \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} - \frac{4a \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{d \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} \\ & - \frac{4a \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{d \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} - \frac{11}{8db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^2} + \frac{11}{8db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2} \\ & - \frac{1}{2db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^4} - \frac{5}{4db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^3} + \frac{1}{2db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^4} - \frac{5}{4db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^3} \\ & + \frac{a^4 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{db^3 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} + \frac{6a^2 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{db \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} \\ & + \frac{a^4 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{db^3 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} + \frac{6a^2 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{db \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} \\ & + \frac{\arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right) b}{d \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} + \frac{\operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right) b}{d \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} \end{aligned}$$

$$\begin{aligned}
& - \frac{a^3 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{db^3 \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} + \frac{a^3 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{db^3 \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} - \frac{1}{5db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^5} \\
& - \frac{1}{5db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^5} - \frac{3}{db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} - \frac{3}{db \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)} + \frac{3a}{db^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} \\
& + \frac{3a}{db^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)} + \frac{\arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{d\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} - \frac{\operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{d\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} \\
& - \frac{4a^3 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{db^2 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} - \frac{4a^3 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{db^2 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} + \frac{a}{3db^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^3} \\
& + \frac{a}{2db^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)^2} - \frac{a^2}{db^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} + \frac{a}{3db^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^3} - \frac{a}{2db^2 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)^2} \\
& - \frac{a^2}{db^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)}
\end{aligned}$$

Problem 85: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(dx+c)^5}{a+b \sinh(dx+c)^2} dx$$

Optimal(type 3, 124 leaves, 6 steps):

$$\begin{aligned}
& \frac{(3a^2 - 10ab + 15b^2) \arctan(\sinh(dx+c))}{8(a-b)^3 d} - \frac{b^5 / 2 \arctan\left(\frac{\sinh(dx+c) \sqrt{b}}{\sqrt{a}}\right)}{(a-b)^3 d \sqrt{a}} + \frac{(3a-7b) \operatorname{sech}(dx+c) \tanh(dx+c)}{8(a-b)^2 d} \\
& + \frac{\operatorname{sech}(dx+c)^3 \tanh(dx+c)}{4(a-b)d}
\end{aligned}$$

Result(type 3, 1022 leaves):



$$\begin{aligned}
& \frac{b^3 a \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{d(a-b)^3 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} - \frac{b^3 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{d(a-b)^3 \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} \\
& - \frac{b^4 \arctan\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}}\right)}{d(a-b)^3 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} - a + 2b)a}} + \frac{b^3 a \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{d(a-b)^3 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} \\
& + \frac{b^3 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{d(a-b)^3 \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} - \frac{b^4 \operatorname{arctanh}\left(\frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}}\right)}{d(a-b)^3 \sqrt{-(a-b)b} \sqrt{(2\sqrt{-(a-b)b} + a - 2b)a}} \\
& - \frac{5 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^7 a^2}{4d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} + \frac{7 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^7 ab}{2d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} - \frac{9 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^7 b^2}{4d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} \\
& + \frac{3 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^5 a^2}{4d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^5 ab}{2d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^5 b^2}{4d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} \\
& - \frac{3 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 a^2}{4d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 ab}{2d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3 b^2}{4d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} \\
& + \frac{5 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a^2}{4d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} - \frac{7 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) ab}{2d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} + \frac{9 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^2}{4d(a-b)^3 \left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + 1\right)^4} \\
& + \frac{3 \arctan\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right) a^2}{4d(a-b)^3} - \frac{5 \arctan\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right) ab}{2d(a-b)^3} + \frac{15 \arctan\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)\right) b^2}{4d(a-b)^3}
\end{aligned}$$

Problem 86: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(dx+c)^5}{(a+b \sinh(dx+c))^2} dx$$

Optimal(type 3, 92 leaves, 5 steps):

$$\frac{(3a^2 - 2ab - b^2) \arctan\left(\frac{\sinh(dx+c)\sqrt{b}}{\sqrt{a}}\right)}{2a^3/2b^5/2d} + \frac{\sinh(dx+c)}{b^2d} + \frac{(a-b)^2 \sinh(dx+c)}{2ab^2d(a+b\sinh(dx+c)^2)}$$

Result(type 3, 1538 leaves):

$$\begin{aligned} & \frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{db^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)} \\ & + \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{db \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)} \\ & - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) a} \\ & + \frac{a \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{db^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)} \\ & - \frac{2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{db \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)} \\ & + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) a} + \frac{3a^3 \arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{2db^2 \sqrt{-a^2 b(a-b)} \sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}} \\ & - \frac{5a^2 \arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{2db \sqrt{-a^2 b(a-b)} \sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}} + \frac{a \arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{2d \sqrt{-a^2 b(a-b)} \sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}} \end{aligned}$$

$$\begin{aligned}
& + \frac{\arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2b(a-b)}}}\right) b}{2d\sqrt{-a^2b(a-b)}\sqrt{-a^2 + 2ab + 2\sqrt{-a^2b(a-b)}}} - \frac{3a\arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2b(a-b)}}}\right)}{2db^2\sqrt{-a^2 + 2ab + 2\sqrt{-a^2b(a-b)}}} \\
& + \frac{\arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2b(a-b)}}}\right)}{db\sqrt{-a^2 + 2ab + 2\sqrt{-a^2b(a-b)}}} + \frac{\arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2b(a-b)}}}\right)}{2da\sqrt{-a^2 + 2ab + 2\sqrt{-a^2b(a-b)}}} \\
& + \frac{3a^3\operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}}\right)}{2db^2\sqrt{-a^2b(a-b)}\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}} - \frac{5a^2\operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}}\right)}{2db\sqrt{-a^2b(a-b)}\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}} \\
& + \frac{a\operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}}\right)}{2d\sqrt{-a^2b(a-b)}\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}} + \frac{\operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}}\right) b}{2d\sqrt{-a^2b(a-b)}\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}} \\
& + \frac{3a\operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}}\right)}{2db^2\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}} - \frac{\operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}}\right)}{db\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}} - \frac{\operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}}\right)}{2da\sqrt{a^2 - 2ab + 2\sqrt{-a^2b(a-b)}}} \\
& - \frac{1}{db^2\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)} - \frac{1}{db^2\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)}
\end{aligned}$$

Problem 87: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(dx+c)^3}{(a+b\sinh(dx+c))^2} dx$$

Optimal(type 3, 65 leaves, 3 steps):

$$\frac{(a+b)\arctan\left(\frac{\sinh(dx+c)\sqrt{b}}{\sqrt{a}}\right)}{2a^3/2b^3/2d} - \frac{(a-b)\sinh(dx+c)}{2abd(a+b\sinh(dx+c))^2}$$

Result(type 3, 1013 leaves):

$$\begin{aligned}
& \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{db \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)} \\
& - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) a} \\
& - \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{db \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)} \\
& + \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) a} - \frac{a^2 b \operatorname{arctanh}\left(\frac{ab \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(a^2 b - 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}}\right)}{2d\sqrt{-a^2 b^3 (a-b)} \sqrt{(a^2 b - 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}} \\
& - \frac{\operatorname{arctanh}\left(\frac{ab \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(a^2 b - 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}}\right)}{2d\sqrt{(a^2 b - 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}} - \frac{a^2 b \operatorname{arctan}\left(\frac{ab \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(-a^2 b + 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}}\right)}{2d\sqrt{-a^2 b^3 (a-b)} \sqrt{(-a^2 b + 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}} \\
& + \frac{\operatorname{arctan}\left(\frac{ab \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(-a^2 b + 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}}\right)}{2d\sqrt{(-a^2 b + 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}} + \frac{b^3 \operatorname{arctanh}\left(\frac{ab \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(a^2 b - 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}}\right)}{2d\sqrt{-a^2 b^3 (a-b)} \sqrt{(a^2 b - 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}} \\
& - \frac{b \operatorname{arctanh}\left(\frac{ab \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(a^2 b - 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}}\right)}{2da\sqrt{(a^2 b - 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}} + \frac{b^3 \operatorname{arctan}\left(\frac{ab \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(-a^2 b + 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}}\right)}{2d\sqrt{-a^2 b^3 (a-b)} \sqrt{(-a^2 b + 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}} \\
& + \frac{b \operatorname{arctan}\left(\frac{ab \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{\sqrt{(-a^2 b + 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}}\right)}{2da\sqrt{(-a^2 b + 2b^2 a + 2\sqrt{-a^2 b^3 (a-b)}) b}}
\end{aligned}$$

Problem 88: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(dx+c)^2}{(a+b \sinh(dx+c))^2} dx$$

Optimal(type 3, 67 leaves, 3 steps):

$$\frac{\operatorname{arctanh}\left(\frac{\sqrt{a-b} \tanh(dx+c)}{\sqrt{a}}\right)}{2 a^3 / 2 d \sqrt{a-b}} + \frac{\tanh(dx+c)}{2 a d (a - (a-b) \tanh(dx+c)^2)}$$

Result(type 3, 435 leaves):

$$\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) a}$$

$$+ \frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4 b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) a} - \frac{\operatorname{arctan}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{-a^2 + 2 a b + 2 \sqrt{-a^2 b (a-b)}}}\right) b}{2 d \sqrt{-a^2 b (a-b)} \sqrt{-a^2 + 2 a b + 2 \sqrt{-a^2 b (a-b)}}}$$

$$- \frac{\operatorname{arctan}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{-a^2 + 2 a b + 2 \sqrt{-a^2 b (a-b)}}}\right)}{2 d a \sqrt{-a^2 + 2 a b + 2 \sqrt{-a^2 b (a-b)}}} - \frac{\operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a-b)}}}\right) b}{2 d \sqrt{-a^2 b (a-b)} \sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a-b)}}}$$

$$+ \frac{\operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a-b)}}}\right)}{2 d a \sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a-b)}}}$$

Problem 89: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(dx+c)}{(a+b \sinh(dx+c))^2} dx$$

Optimal(type 3, 94 leaves, 5 steps):

$$\frac{\operatorname{arctan}(\sinh(dx+c))}{(a-b)^2 d} - \frac{b \sinh(dx+c)}{2 a (a-b) d (a+b \sinh(dx+c)^2)} - \frac{(3 a-b) \operatorname{arctan}\left(\frac{\sinh(dx+c) \sqrt{b}}{\sqrt{a}}\right) \sqrt{b}}{2 a^3 / 2 (a-b)^2 d}$$

Result(type 3, 1177 leaves):

$$\begin{aligned}
& \frac{b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{d(a-b)^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)} \\
& - \frac{b^2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^3}{d(a-b)^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) a} \\
& - \frac{b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{d(a-b)^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right)} \\
& + \frac{b^2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{d(a-b)^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^4 a - 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a + 4b \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 + a \right) a} \\
& + \frac{3b a^2 \arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{2d(a-b)^2 \sqrt{-a^2 b(a-b)} \sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}} - \frac{2b^2 a \arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{d(a-b)^2 \sqrt{-a^2 b(a-b)} \sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}} \\
& - \frac{3b \arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{2d(a-b)^2 \sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}} + \frac{3b a^2 \operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{2d(a-b)^2 \sqrt{-a^2 b(a-b)} \sqrt{a^2 - 2ab + 2\sqrt{-a^2 b(a-b)}}} \\
& - \frac{2b^2 a \operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{d(a-b)^2 \sqrt{-a^2 b(a-b)} \sqrt{a^2 - 2ab + 2\sqrt{-a^2 b(a-b)}}} + \frac{3b \operatorname{arctanh}\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{2d(a-b)^2 \sqrt{a^2 - 2ab + 2\sqrt{-a^2 b(a-b)}}} \\
& + \frac{b^3 \arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{2d(a-b)^2 \sqrt{-a^2 b(a-b)} \sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}} + \frac{b^2 \arctan\left(\frac{\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}}\right)}{2d(a-b)^2 a \sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}}
\end{aligned}$$

$$+ \frac{b^3 \operatorname{arctanh} \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2 b(a-b)}}} \right)}{2d(a-b)^2 \sqrt{-a^2 b(a-b)} \sqrt{a^2 - 2ab + 2\sqrt{-a^2 b(a-b)}}} - \frac{b^2 \operatorname{arctanh} \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{a^2 - 2ab + 2\sqrt{-a^2 b(a-b)}}} \right)}{2d(a-b)^2 a \sqrt{a^2 - 2ab + 2\sqrt{-a^2 b(a-b)}}} + \frac{2 \operatorname{arctan} \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right) \right)}{d(a-b)^2}$$

Problem 90: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(dx+c)^3}{(a+b \sinh(dx+c))^2} dx$$

Optimal (type 3, 141 leaves, 6 steps):

$$\frac{(a-5b) \operatorname{arctan}(\sinh(dx+c))}{2(a-b)^3 d} + \frac{(5a-b) b^3 /2 \operatorname{arctan} \left( \frac{\sinh(dx+c) \sqrt{b}}{\sqrt{a}} \right)}{2a^3 /2 (a-b)^3 d} + \frac{b(a+b) \sinh(dx+c)}{2a(a-b)^2 d (a+b \sinh(dx+c))^2}$$

$$+ \frac{\operatorname{sech}(dx+c) \tanh(dx+c)}{2(a-b) d (a+b \sinh(dx+c))^2}$$

Result (type 3, 1362 leaves):

$$\frac{b^2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^3}{d(a-b)^3 \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^4 a - 2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 a + 4b \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + a \right)}$$

$$+ \frac{b^3 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^3}{d(a-b)^3 \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^4 a - 2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 a + 4b \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + a \right) a}$$

$$+ \frac{b^2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)}{d(a-b)^3 \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^4 a - 2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 a + 4b \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + a \right)}$$

$$- \frac{b^3 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)}{d(a-b)^3 \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^4 a - 2 \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 a + 4b \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + a \right) a}$$

$$- \frac{5b^2 a^2 \operatorname{arctan} \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}} \right)}{2d(a-b)^3 \sqrt{-a^2 b(a-b)} \sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}} + \frac{3b^3 a \operatorname{arctan} \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}} \right)}{d(a-b)^3 \sqrt{-a^2 b(a-b)} \sqrt{-a^2 + 2ab + 2\sqrt{-a^2 b(a-b)}}}$$

$$\begin{aligned}
& + \frac{5 b^2 \arctan \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{-a^2 + 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \right)}{2 d (a - b)^3 \sqrt{-a^2 + 2 a b + 2 \sqrt{-a^2 b (a - b)}}} - \frac{5 b^2 a^2 \operatorname{arctanh} \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \right)}{2 d (a - b)^3 \sqrt{-a^2 b (a - b)} \sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \\
& + \frac{3 b^3 a \operatorname{arctanh} \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \right)}{d (a - b)^3 \sqrt{-a^2 b (a - b)} \sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a - b)}}} - \frac{5 b^2 \operatorname{arctanh} \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \right)}{2 d (a - b)^3 \sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \\
& - \frac{b^4 \arctan \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{-a^2 + 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \right)}{2 d (a - b)^3 \sqrt{-a^2 b (a - b)} \sqrt{-a^2 + 2 a b + 2 \sqrt{-a^2 b (a - b)}}} - \frac{b^3 \arctan \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{-a^2 + 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \right)}{2 d (a - b)^3 a \sqrt{-a^2 + 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \\
& - \frac{b^4 \operatorname{arctanh} \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \right)}{2 d (a - b)^3 \sqrt{-a^2 b (a - b)} \sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a - b)}}} + \frac{b^3 \operatorname{arctanh} \left( \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) a}{\sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \right)}{2 d (a - b)^3 a \sqrt{a^2 - 2 a b + 2 \sqrt{-a^2 b (a - b)}}} \\
& - \frac{a \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^3}{d (a - b)^3 \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + 1 \right)^2} + \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^3 b}{d (a - b)^3 \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + 1 \right)^2} + \frac{a \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)}{d (a - b)^3 \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + 1 \right)^2} \\
& - \frac{\tanh \left( \frac{dx}{2} + \frac{c}{2} \right) b}{d (a - b)^3 \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right)^2 + 1 \right)^2} + \frac{\arctan \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right) \right) a}{d (a - b)^3} - \frac{5 \arctan \left( \tanh \left( \frac{dx}{2} + \frac{c}{2} \right) \right) b}{d (a - b)^3}
\end{aligned}$$

Problem 91: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(dx + c)^6}{(a + b \sinh(dx + c))^3} dx$$

Optimal (type 3, 146 leaves, 6 steps):

$$\frac{x}{b^3} - \frac{(8 a^2 + 4 a b + 3 b^2) \operatorname{arctanh} \left( \frac{\sqrt{a - b} \tanh(dx + c)}{\sqrt{a}} \right) \sqrt{a - b}}{8 a^5 / 2 b^3 d} - \frac{(a - b) \tanh(dx + c)}{4 a b d (a - (a - b) \tanh(dx + c))^2} - \frac{(a - b) (4 a + 3 b) \tanh(dx + c)}{8 a^2 b^2 d (a - (a - b) \tanh(dx + c))^2}$$



Result(type ?, 2365 leaves): Display of huge result suppressed!

Problem 92: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(dx+c)^2}{(a+b\sinh(dx+c)^2)^3} dx$$

Optimal(type 3, 129 leaves, 4 steps):

$$\frac{(4a-3b) \operatorname{arctanh}\left(\frac{\sqrt{a-b} \tanh(dx+c)}{\sqrt{a}}\right)}{8a^{5/2}(a-b)^{3/2}d} - \frac{b \tanh(dx+c)}{4a(a-b)d(a-(a-b)\tanh(dx+c)^2)^2} + \frac{(4a-3b) \tanh(dx+c)}{8a^2(a-b)d(a-(a-b)\tanh(dx+c)^2)}$$

Result(type ?, 2650 leaves): Display of huge result suppressed!

Problem 93: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(dx+c)}{(a+b\sinh(dx+c)^2)^3} dx$$

Optimal(type 3, 145 leaves, 6 steps):

$$\frac{\operatorname{arctan}(\sinh(dx+c))}{(a-b)^3 d} - \frac{b \sinh(dx+c)}{4a(a-b)d(a+b\sinh(dx+c)^2)^2} - \frac{(7a-3b)b \sinh(dx+c)}{8a^2(a-b)^2 d(a+b\sinh(dx+c)^2)}$$
$$- \frac{(15a^2-10ab+3b^2) \operatorname{arctan}\left(\frac{\sinh(dx+c)\sqrt{b}}{\sqrt{a}}\right) \sqrt{b}}{8a^{5/2}(a-b)^3 d}$$

Result(type ?, 2395 leaves): Display of huge result suppressed!

Problem 94: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(dx+c)^3}{(a+b\sinh(dx+c)^2)^3} dx$$

Optimal(type 3, 199 leaves, 7 steps):

$$\frac{(a-7b) \operatorname{arctan}(\sinh(dx+c))}{2(a-b)^4 d} + \frac{b^{3/2}(35a^2-14ab+3b^2) \operatorname{arctan}\left(\frac{\sinh(dx+c)\sqrt{b}}{\sqrt{a}}\right)}{8a^{5/2}(a-b)^4 d} + \frac{b(2a+b) \sinh(dx+c)}{4a(a-b)^2 d(a+b\sinh(dx+c)^2)^2}$$
$$+ \frac{(-b+4a)b(a+3b) \sinh(dx+c)}{8a^2(a-b)^3 d(a+b\sinh(dx+c)^2)} + \frac{\operatorname{sech}(dx+c) \tanh(dx+c)}{2(a-b)d(a+b\sinh(dx+c)^2)^2}$$

Result(type ?, 2584 leaves): Display of huge result suppressed!

Problem 95: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{sech}(dx+c)^4}{(a+b\sinh(dx+c)^2)^3} dx$$

Optimal(type 3, 187 leaves, 6 steps):

$$\frac{b^2 (48 a^2 - 16 a b + 3 b^2) \operatorname{arctanh}\left(\frac{\sqrt{a-b} \tanh(dx+c)}{\sqrt{a}}\right)}{8 a^5 \sqrt{2} (a-b)^9 \sqrt{2} d} + \frac{(a-4 b) \tanh(dx+c)}{(a-b)^4 d} - \frac{\tanh(dx+c)^3}{3 (a-b)^3 d} + \frac{b^4 \tanh(dx+c)}{4 a (a-b)^4 d (a-(a-b) \tanh(dx+c)^2)^2}$$

$$- \frac{(16 a-3 b) b^3 \tanh(dx+c)}{8 a^2 (a-b)^4 d (a-(a-b) \tanh(dx+c)^2)}$$

Result(type ?, 2123 leaves): Display of huge result suppressed!

Problem 96: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(x)^2}{1 - \sinh(x)^2} dx$$

Optimal(type 3, 15 leaves, 4 steps):

$$-x + \operatorname{arctanh}(\sqrt{2} \tanh(x)) \sqrt{2}$$

Result(type 3, 53 leaves):

$$\ln\left(\tanh\left(\frac{x}{2}\right) - 1\right) + \sqrt{2} \operatorname{arctanh}\left(\frac{\left(2 \tanh\left(\frac{x}{2}\right) + 2\right) \sqrt{2}}{4}\right) - \ln\left(\tanh\left(\frac{x}{2}\right) + 1\right) + \sqrt{2} \operatorname{arctanh}\left(\frac{\left(2 \tanh\left(\frac{x}{2}\right) - 2\right) \sqrt{2}}{4}\right)$$

Problem 97: Unable to integrate problem.

$$\int \operatorname{sech}(fx+e) \sqrt{a+b \sinh(fx+e)^2} dx$$

Optimal(type 3, 73 leaves, 6 steps):

$$\frac{\operatorname{arctan}\left(\frac{\sinh(fx+e) \sqrt{a-b}}{\sqrt{a+b \sinh(fx+e)^2}}\right) \sqrt{a-b}}{f} + \frac{\operatorname{arctanh}\left(\frac{\sinh(fx+e) \sqrt{b}}{\sqrt{a+b \sinh(fx+e)^2}}\right) \sqrt{b}}{f}$$

Result(type 9, 50 leaves):

$$\frac{\operatorname{int/undef0}\left(-\frac{-b \sinh(fx+e)^2 - a}{\cosh(fx+e)^2 \sqrt{a+b \sinh(fx+e)^2}}, \sinh(fx+e)\right)}{f}$$

Problem 99: Unable to integrate problem.

$$\int \operatorname{sech}(fx+e) (a+b \sinh(fx+e)^2)^{3/2} dx$$

Optimal(type 3, 107 leaves, 7 steps):

$$\frac{(a-b)^3/2 \arctan\left(\frac{\sinh(fx+e)\sqrt{a-b}}{\sqrt{a+b\sinh(fx+e)^2}}\right)}{f} + \frac{(3a-2b) \operatorname{arctanh}\left(\frac{\sinh(fx+e)\sqrt{b}}{\sqrt{a+b\sinh(fx+e)^2}}\right)\sqrt{b}}{2f} + \frac{b\sinh(fx+e)\sqrt{a+b\sinh(fx+e)^2}}{2f}$$

Result(type 9, 62 leaves):

$$\frac{\operatorname{int/indef0}\left(\frac{b^2 \sinh(fx+e)^4 + 2ab\sinh(fx+e)^2 + a^2}{\cosh(fx+e)^2 \sqrt{a+b\sinh(fx+e)^2}}, \sinh(fx+e)\right)}{f}$$

Problem 101: Unable to integrate problem.

$$\int \frac{\operatorname{sech}(fx+e)}{\sqrt{a+b\sinh(fx+e)^2}} dx$$

Optimal(type 3, 40 leaves, 3 steps):

$$\frac{\arctan\left(\frac{\sinh(fx+e)\sqrt{a-b}}{\sqrt{a+b\sinh(fx+e)^2}}\right)}{f\sqrt{a-b}}$$

Result(type 9, 34 leaves):

$$\frac{\operatorname{int/indef0}\left(\frac{1}{\cosh(fx+e)^2 \sqrt{a+b\sinh(fx+e)^2}}, \sinh(fx+e)\right)}{f}$$

Problem 103: Unable to integrate problem.

$$\int \frac{\cosh(fx+e)^3}{(a+b\sinh(fx+e)^2)^{3/2}} dx$$

Optimal(type 3, 69 leaves, 4 steps):

$$\frac{\operatorname{arctanh}\left(\frac{\sinh(fx+e)\sqrt{b}}{\sqrt{a+b\sinh(fx+e)^2}}\right)}{b^3/2f} - \frac{(a-b)\sinh(fx+e)}{abf\sqrt{a+b\sinh(fx+e)^2}}$$

Result(type 9, 34 leaves):

$$\frac{\operatorname{int/indef0}\left(\frac{\cosh(fx+e)^2}{(a+b\sinh(fx+e)^2)^{3/2}}, \sinh(fx+e)\right)}{f}$$

Problem 107: Unable to integrate problem.

$$\int \frac{\cosh(fx + e)^3}{(a + b \sinh(fx + e)^2)^{5/2}} dx$$

Optimal(type 3, 65 leaves, 3 steps):

$$\frac{\cosh(fx + e)^2 \sinh(fx + e)}{3 a f (a + b \sinh(fx + e)^2)^{3/2}} + \frac{2 \sinh(fx + e)}{3 a^2 f \sqrt{a + b \sinh(fx + e)^2}}$$

Result(type 9, 64 leaves):

$$\frac{\operatorname{int/indef0}\left(\frac{\cosh(fx + e)^2}{(b^2 \sinh(fx + e)^4 + 2 a b \sinh(fx + e)^2 + a^2) \sqrt{a + b \sinh(fx + e)^2}}, \sinh(fx + e)\right)}{f}$$

Problem 108: Unable to integrate problem.

$$\int \cosh(fx + e) (a + b \sinh(fx + e)^2)^p dx$$

Optimal(type 5, 65 leaves, 3 steps):

$$\frac{\operatorname{hypergeom}\left(\left[\frac{1}{2}, -p\right], \left[\frac{3}{2}\right], -\frac{b \sinh(fx + e)^2}{a}\right) \sinh(fx + e) (a + b \sinh(fx + e)^2)^p}{f \left(1 + \frac{b \sinh(fx + e)^2}{a}\right)^p}$$

Result(type 8, 23 leaves):

$$\int \cosh(fx + e) (a + b \sinh(fx + e)^2)^p dx$$

Problem 109: Unable to integrate problem.

$$\int \cosh(fx + e)^2 (a + b \sinh(fx + e)^2)^p dx$$

Optimal(type 6, 84 leaves, 3 steps):

$$\frac{\operatorname{AppellF1}\left(\frac{1}{2}, -\frac{1}{2}, -p, \frac{3}{2}, -\sinh(fx + e)^2, -\frac{b \sinh(fx + e)^2}{a}\right) (a + b \sinh(fx + e)^2)^p \sqrt{\cosh(fx + e)^2} \tanh(fx + e)}{f \left(1 + \frac{b \sinh(fx + e)^2}{a}\right)^p}$$

Result(type 8, 25 leaves):

$$\int \cosh(fx + e)^2 (a + b \sinh(fx + e)^2)^p dx$$

Problem 110: Unable to integrate problem.

$$\int \frac{\cosh(dx+c)^5}{(a+b\sqrt{\sinh(dx+c)})^2} dx$$

Optimal (type 3, 248 leaves, 4 steps):

$$\begin{aligned} & \frac{2(a^4+b^4)(9a^4+b^4)\ln(a+b\sqrt{\sinh(dx+c)})}{b^{10}d} + \frac{a^2(7a^4+6b^4)\sinh(dx+c)}{b^8d} - \frac{4a(3a^4+2b^4)\sinh(dx+c)^3/2}{3b^7d} + \frac{(5a^4+2b^4)\sinh(dx+c)^2}{2b^6d} \\ & - \frac{8a^3\sinh(dx+c)^5/2}{5b^5d} + \frac{a^2\sinh(dx+c)^3}{b^4d} - \frac{4a\sinh(dx+c)^7/2}{7b^3d} + \frac{\sinh(dx+c)^4}{4b^2d} - \frac{16a^3(a^4+b^4)\sqrt{\sinh(dx+c)}}{b^9d} \\ & + \frac{2a(a^4+b^4)^2}{b^{10}d(a+b\sqrt{\sinh(dx+c)})} \end{aligned}$$

Result (type 9, 954 leaves):

$$\begin{aligned} & - \frac{8 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a^4}{db^4 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a^2 + 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^2 - a^2 \right)} - \frac{4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) a^8}{db^8 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a^2 + 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^2 - a^2 \right)} \\ & + \frac{9 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a^2 + 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^2 - a^2\right) a^8}{db^{10}} + \frac{10 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a^2 + 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^2 - a^2\right) a^4}{db^6} \\ & - \frac{7a^6}{db^8 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1 \right)} - \frac{5a^4}{2db^6 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1 \right)} - \frac{6a^2}{db^4 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1 \right)} - \frac{a^2}{db^4 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1 \right)^3} \\ & + \frac{5a^4}{2db^6 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1 \right)^2} + \frac{3a^2}{2db^4 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1 \right)^2} - \frac{9 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right) a^8}{db^{10}} - \frac{10 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right) a^4}{db^6} \\ & - \frac{7a^6}{db^8 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1 \right)} + \frac{5a^4}{2db^6 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1 \right)} - \frac{6a^2}{db^4 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1 \right)} - \frac{a^2}{db^4 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1 \right)^3} \\ & + \frac{5a^4}{2db^6 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1 \right)^2} - \frac{3a^2}{2db^4 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1 \right)^2} - \frac{9 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right) a^8}{db^{10}} - \frac{10 \ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right) a^4}{db^6} \\ & + \frac{\text{int/indef0}\left(-\frac{2 \cosh(dx+c)^4 a b \sqrt{\sinh(dx+c)}}{b^4 \sinh(dx+c)^2 - 2 a^2 b^2 \sinh(dx+c) + a^4}, \sinh(dx+c)\right)}{d} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1\right)}{db^2} - \frac{\ln\left(\tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1\right)}{db^2} \end{aligned}$$

$$\begin{aligned}
& - \frac{4 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)}{d \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a^2 + 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^2 - a^2 \right)} + \frac{9}{8 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1 \right)^2} + \frac{1}{4 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1 \right)^4} \\
& + \frac{1}{2 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1 \right)^3} + \frac{9}{8 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1 \right)^2} + \frac{\ln\left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right)^2 a^2 + 2 \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) b^2 - a^2 \right)}{d b^2} \\
& + \frac{1}{4 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1 \right)^4} - \frac{1}{2 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1 \right)^3} + \frac{7}{8 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) - 1 \right)} - \frac{7}{8 d b^2 \left( \tanh\left(\frac{dx}{2} + \frac{c}{2}\right) + 1 \right)}
\end{aligned}$$

Problem 111: Result more than twice size of optimal antiderivative.

$$\int \frac{\cosh(dx+c)}{\left(a+b\sqrt{\sinh(dx+c)}\right)^2} dx$$

Optimal (type 3, 45 leaves, 4 steps):

$$\frac{2 \ln\left(a+b\sqrt{\sinh(dx+c)}\right)}{b^2 d} + \frac{2 a}{b^2 d \left(a+b\sqrt{\sinh(dx+c)}\right)}$$

Result (type 3, 143 leaves):

$$\begin{aligned}
& - \frac{2 a^2}{d \left(\sinh(dx+c) b^2 - a^2\right) b^2} + \frac{\ln\left(\sinh(dx+c) b^2 - a^2\right)}{d b^2} + \frac{a}{b^2 d \left(a+b\sqrt{\sinh(dx+c)}\right)} + \frac{\ln\left(a+b\sqrt{\sinh(dx+c)}\right)}{b^2 d} + \frac{a}{d b^2 \left(b\sqrt{\sinh(dx+c)} - a\right)} \\
& - \frac{\ln\left(b\sqrt{\sinh(dx+c)} - a\right)}{d b^2}
\end{aligned}$$

Problem 112: Unable to integrate problem.

$$\int \frac{\cosh(dx+c)^5}{\left(a+b\sinh(dx+c)^n\right)^2} dx$$

Optimal (type 5, 132 leaves, 6 steps):

$$\begin{aligned}
& \frac{\text{hypergeom}\left(\left[2, \frac{1}{n}\right], \left[1 + \frac{1}{n}\right], -\frac{b \sinh(dx+c)^n}{a}\right) \sinh(dx+c)}{a^2 d} + \frac{2 \text{hypergeom}\left(\left[2, \frac{3}{n}\right], \left[\frac{3+n}{n}\right], -\frac{b \sinh(dx+c)^n}{a}\right) \sinh(dx+c)^3}{3 a^2 d} \\
& + \frac{\text{hypergeom}\left(\left[2, \frac{5}{n}\right], \left[\frac{5+n}{n}\right], -\frac{b \sinh(dx+c)^n}{a}\right) \sinh(dx+c)^5}{5 a^2 d}
\end{aligned}$$

Result (type 8, 723 leaves):

$$\begin{aligned}
& \left( (e^{dx+c})^8 + 4(e^{dx+c})^6 + 6(e^{dx+c})^4 + 4(e^{dx+c})^2 + 1 \right) (e^{dx+c} - 1) (1 + e^{dx+c}) \Big/ \left( 32(e^{dx+c})^5 n a d \left( a \right. \right. \\
& + b \\
& \left. \left. e \left( -\ln(2) - \ln(e^{dx+c}) + \ln(e^{dx+c} - 1) + \ln(1 + e^{dx+c}) \right) \right. \right. \\
& \left. \left. - \frac{1 \pi \operatorname{csgn}(1(e^{dx+c} - 1)(1 + e^{dx+c})) (-\operatorname{csgn}(1(e^{dx+c} - 1)(1 + e^{dx+c})) + \operatorname{csgn}(1(e^{dx+c} - 1))) (-\operatorname{csgn}(1(e^{dx+c} - 1)(1 + e^{dx+c})) + \operatorname{csgn}(1(1 + e^{dx+c})))}{2} \right. \right. \\
& \left. \left. - \frac{1 \pi \operatorname{csgn}\left(\frac{1(e^{dx+c} - 1)(1 + e^{dx+c})}{e^{dx+c}}\right) \left( -\operatorname{csgn}\left(\frac{1(e^{dx+c} - 1)(1 + e^{dx+c})}{e^{dx+c}}\right) + \operatorname{csgn}\left(\frac{1}{e^{dx+c}}\right) \right) \left( -\operatorname{csgn}\left(\frac{1(e^{dx+c} - 1)(1 + e^{dx+c})}{e^{dx+c}}\right) + \operatorname{csgn}(1(e^{dx+c} - 1)(1 + e^{dx+c})) \right) \right)}{2} \right) \Bigg) \\
& + \int \left( n(e^{dx+c})^{10} - 5(e^{dx+c})^{10} + 5n(e^{dx+c})^8 - 9(e^{dx+c})^8 + 10n(e^{dx+c})^6 - 2(e^{dx+c})^6 + 10n(e^{dx+c})^4 - 2(e^{dx+c})^4 + 5n(e^{dx+c})^2 \right. \\
& \left. - 9(e^{dx+c})^2 + n - 5 \right) \Big/ \left( 32(e^{dx+c})^5 n a \left( a \right. \right. \\
& + b \\
& \left. \left. e \left( -\ln(2) - \ln(e^{dx+c}) + \ln(e^{dx+c} - 1) + \ln(1 + e^{dx+c}) \right) \right. \right. \\
& \left. \left. - \frac{1 \pi \operatorname{csgn}(1(e^{dx+c} - 1)(1 + e^{dx+c})) (-\operatorname{csgn}(1(e^{dx+c} - 1)(1 + e^{dx+c})) + \operatorname{csgn}(1(e^{dx+c} - 1))) (-\operatorname{csgn}(1(e^{dx+c} - 1)(1 + e^{dx+c})) + \operatorname{csgn}(1(1 + e^{dx+c})))}{2} \right. \right. \\
& \left. \left. - \frac{1 \pi \operatorname{csgn}\left(\frac{1(e^{dx+c} - 1)(1 + e^{dx+c})}{e^{dx+c}}\right) \left( -\operatorname{csgn}\left(\frac{1(e^{dx+c} - 1)(1 + e^{dx+c})}{e^{dx+c}}\right) + \operatorname{csgn}\left(\frac{1}{e^{dx+c}}\right) \right) \left( -\operatorname{csgn}\left(\frac{1(e^{dx+c} - 1)(1 + e^{dx+c})}{e^{dx+c}}\right) + \operatorname{csgn}(1(e^{dx+c} - 1)(1 + e^{dx+c})) \right) \right)}{2} \right) \Bigg) dx
\end{aligned}$$

Problem 113: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{coth}(x)}{1 - \sinh(x)^2} dx$$

Optimal(type 3, 15 leaves, 4 steps):

$$\ln(\sinh(x)) - \frac{\ln(1 - \sinh(x)^2)}{2}$$

Result(type 3, 40 leaves):

$$\ln\left(\tanh\left(\frac{x}{2}\right)\right) - \frac{\ln\left(\tanh\left(\frac{x}{2}\right)^2 + 2 \tanh\left(\frac{x}{2}\right) - 1\right)}{2} - \frac{\ln\left(\tanh\left(\frac{x}{2}\right)^2 - 2 \tanh\left(\frac{x}{2}\right) - 1\right)}{2}$$

Problem 114: Unable to integrate problem.

$$\int \coth(fx + e)^3 \sqrt{a + a \sinh(fx + e)^2} \, dx$$

Optimal(type 3, 71 leaves, 7 steps):

$$-\frac{(a \cosh(fx + e)^2)^{3/2} \operatorname{csch}(fx + e)^2}{2af} - \frac{3 \operatorname{arctanh}\left(\frac{\sqrt{a \cosh(fx + e)^2}}{\sqrt{a}}\right) \sqrt{a}}{2f} + \frac{3 \sqrt{a \cosh(fx + e)^2}}{2f}$$

Result(type 9, 53 leaves):

$$\frac{\operatorname{int/indef0}\left(\frac{a \cosh(fx + e)^4}{\sinh(fx + e) (\cosh(fx + e)^2 - 1) \sqrt{a \cosh(fx + e)^2}}, \sinh(fx + e)\right)}{f}$$

Problem 118: Unable to integrate problem.

$$\int \frac{\tanh(fx + e)^5}{\sqrt{a + a \sinh(fx + e)^2}} \, dx$$

Optimal(type 3, 56 leaves, 5 steps):

$$-\frac{a^2}{5f(a \cosh(fx + e)^2)^{5/2}} + \frac{2a}{3f(a \cosh(fx + e)^2)^{3/2}} - \frac{1}{f\sqrt{a \cosh(fx + e)^2}}$$

Result(type 9, 40 leaves):

$$\frac{\operatorname{int/indef0}\left(\frac{\sinh(fx + e)^5}{\cosh(fx + e)^6 \sqrt{a \cosh(fx + e)^2}}, \sinh(fx + e)\right)}{f}$$

Problem 121: Unable to integrate problem.

$$\int \frac{\tanh(fx + e)^5}{(a + a \sinh(fx + e)^2)^{3/2}} \, dx$$



Optimal(type 3, 56 leaves, 5 steps):

$$-\frac{a^2}{7f(a \cosh(fx + e))^2}^{7/2} + \frac{2a}{5f(a \cosh(fx + e))^2}^{5/2} - \frac{1}{3f(a \cosh(fx + e))^2}^{3/2}$$

Result(type 9, 43 leaves):

$$\frac{\text{int/indef0}\left(\frac{\sinh(fx + e)^5}{\cosh(fx + e)^8 a \sqrt{a \cosh(fx + e)^2}}, \sinh(fx + e)\right)}{f}$$

Problem 124: Unable to integrate problem.

$$\int \coth(fx + e) \sqrt{a + b \sinh(fx + e)^2} dx$$

Optimal(type 3, 46 leaves, 4 steps):

$$-\frac{\text{arctanh}\left(\frac{\sqrt{a + b \sinh(fx + e)^2}}{\sqrt{a}}\right) \sqrt{a}}{f} + \frac{\sqrt{a + b \sinh(fx + e)^2}}{f}$$

Result(type 9, 45 leaves):

$$\frac{\text{int/indef0}\left(\frac{b \sinh(fx + e) + \frac{a}{\sinh(fx + e)}}{\sqrt{a + b \sinh(fx + e)^2}}, \sinh(fx + e)\right)}{f}$$

Problem 125: Unable to integrate problem.

$$\int \coth(fx + e)^5 \sqrt{a + b \sinh(fx + e)^2} dx$$

Optimal(type 3, 147 leaves, 6 steps):

$$\begin{aligned} & -\frac{(8a^2 + 8ab - b^2) \text{arctanh}\left(\frac{\sqrt{a + b \sinh(fx + e)^2}}{\sqrt{a}}\right)}{8a^3/2f} - \frac{(8a - b) \text{csch}(fx + e)^2 (a + b \sinh(fx + e)^2)^3/2}{8a^2f} - \frac{\text{csch}(fx + e)^4 (a + b \sinh(fx + e)^2)^3/2}{4af} \\ & + \frac{(8a^2 + 8ab - b^2) \sqrt{a + b \sinh(fx + e)^2}}{8a^2f} \end{aligned}$$

Result(type 9, 79 leaves):

$$\frac{\text{int/indef0}\left(\frac{\cosh(fx + e)^4 (a - b + b \cosh(fx + e)^2)}{\sinh(fx + e) (1 + \cosh(fx + e)^4 - 2 \cosh(fx + e)^2) \sqrt{a + b \sinh(fx + e)^2}}, \sinh(fx + e)\right)}{f}$$

Problem 128: Unable to integrate problem.

$$\int (a + b \sinh(fx + e))^3 / 2 \tanh(fx + e)^5 dx$$

Optimal(type 3, 208 leaves, 7 steps):

$$\frac{(8a^2 - 40ab + 35b^2)(a + b \sinh(fx + e))^3 / 2}{24(a - b)^2 f} + \frac{(8a - 9b) \operatorname{sech}(fx + e)^2 (a + b \sinh(fx + e))^5 / 2}{8(a - b)^2 f} - \frac{\operatorname{sech}(fx + e)^4 (a + b \sinh(fx + e))^5 / 2}{4(a - b)f}$$

$$- \frac{(8a^2 - 40ab + 35b^2) \operatorname{arctanh}\left(\frac{\sqrt{a + b \sinh(fx + e)^2}}{\sqrt{a - b}}\right)}{8f\sqrt{a - b}} + \frac{(8a^2 - 40ab + 35b^2) \sqrt{a + b \sinh(fx + e)^2}}{8(a - b)f}$$

Result(type 9, 70 leaves):

$$\frac{\operatorname{int/indef0}\left(\frac{\sinh(fx + e)^5 (b^2 \sinh(fx + e)^4 + 2ab \sinh(fx + e)^2 + a^2)}{\cosh(fx + e)^6 \sqrt{a + b \sinh(fx + e)^2}}, \sinh(fx + e)\right)}{f}$$

Problem 129: Unable to integrate problem.

$$\int \coth(fx + e) (a + b \sinh(fx + e))^3 / 2 dx$$

Optimal(type 3, 66 leaves, 5 steps):

$$- \frac{a^3 / 2 \operatorname{arctanh}\left(\frac{\sqrt{a + b \sinh(fx + e)^2}}{\sqrt{a}}\right)}{f} + \frac{(a + b \sinh(fx + e))^3 / 2}{3f} + \frac{a \sqrt{a + b \sinh(fx + e)^2}}{f}$$

Result(type 9, 61 leaves):

$$\frac{\operatorname{int/indef0}\left(\frac{b^2 \sinh(fx + e)^3 + 2ab \sinh(fx + e) + \frac{a^2}{\sinh(fx + e)}}{\sqrt{a + b \sinh(fx + e)^2}}, \sinh(fx + e)\right)}{f}$$

Problem 130: Unable to integrate problem.

$$\int \coth(fx + e)^3 (a + b \sinh(fx + e))^3 / 2 dx$$

Optimal(type 3, 120 leaves, 6 steps):

$$\frac{(2a + 3b)(a + b \sinh(fx + e))^3 / 2}{6af} - \frac{\operatorname{csch}(fx + e)^2 (a + b \sinh(fx + e))^5 / 2}{2af} - \frac{(2a + 3b) \operatorname{arctanh}\left(\frac{\sqrt{a + b \sinh(fx + e)^2}}{\sqrt{a}}\right) \sqrt{a}}{2f}$$

$$+ \frac{(2a + 3b) \sqrt{a + b \sinh(fx + e)^2}}{2f}$$

Result(type 9, 83 leaves):

$$\frac{\text{int/indef0} \left( \frac{b^2 \sinh(fx + e)^3 + (2ab + b^2) \sinh(fx + e) + \frac{a^2 + 2ab}{\sinh(fx + e)} + \frac{a^2}{\sinh(fx + e)^3}, \sinh(fx + e) \right)}{f}$$

Problem 133: Unable to integrate problem.

$$\int \frac{\coth(fx + e)^5}{\sqrt{a + b \sinh(fx + e)^2}} dx$$

Optimal(type 3, 110 leaves, 5 steps):

$$- \frac{(8a^2 - 8ab + 3b^2) \operatorname{arctanh} \left( \frac{\sqrt{a + b \sinh(fx + e)^2}}{\sqrt{a}} \right)}{8a^5 / 2f} - \frac{(8a - 3b) \operatorname{csch}(fx + e)^2 \sqrt{a + b \sinh(fx + e)^2}}{8a^2 f} - \frac{\operatorname{csch}(fx + e)^4 \sqrt{a + b \sinh(fx + e)^2}}{4af}$$

Result(type 9, 53 leaves):

$$\frac{\text{int/indef0} \left( \frac{\frac{1}{\sinh(fx + e)} + \frac{2}{\sinh(fx + e)^3} + \frac{1}{\sinh(fx + e)^5}}{\sqrt{a + b \sinh(fx + e)^2}}, \sinh(fx + e) \right)}{f}$$

Problem 134: Unable to integrate problem.

$$\int \frac{\tanh(fx + e)^3}{(a + b \sinh(fx + e)^2)^{3/2}} dx$$

Optimal(type 3, 106 leaves, 5 steps):

$$- \frac{(2a + b) \operatorname{arctanh} \left( \frac{\sqrt{a + b \sinh(fx + e)^2}}{\sqrt{a - b}} \right)}{2(a - b)^5 / 2f} + \frac{2a + b}{2(a - b)^2 f \sqrt{a + b \sinh(fx + e)^2}} + \frac{\operatorname{sech}(fx + e)^2}{2(a - b) f \sqrt{a + b \sinh(fx + e)^2}}$$

Result(type 9, 102 leaves):

$$\frac{\text{int/indef0} \left( - \frac{\sinh(fx + e)^3 \sqrt{a + b \sinh(fx + e)^2} \cosh(fx + e)^2}{-b^2 \cosh(fx + e)^{10} + (-2ab + 2b^2) \cosh(fx + e)^8 + (-a^2 + 2ab - b^2) \cosh(fx + e)^6}, \sinh(fx + e) \right)}{f}$$

Problem 135: Unable to integrate problem.

$$\int \frac{\coth(fx + e)}{(a + b \sinh(fx + e)^2)^{3/2}} dx$$

Optimal(type 3, 49 leaves, 4 steps):

$$-\frac{\operatorname{arctanh}\left(\frac{\sqrt{a + b \sinh(fx + e)^2}}{\sqrt{a}}\right)}{a^{3/2}f} + \frac{1}{af\sqrt{a + b \sinh(fx + e)^2}}$$

Result(type 9, 34 leaves):

$$\frac{\operatorname{int/indef0}\left(\frac{1}{\sinh(fx + e) (a + b \sinh(fx + e)^2)^{3/2}}, \sinh(fx + e)\right)}{f}$$

Problem 136: Unable to integrate problem.

$$\int \frac{\coth(fx + e)^3}{(a + b \sinh(fx + e)^2)^{3/2}} dx$$

Optimal(type 3, 94 leaves, 5 steps):

$$-\frac{(2a - 3b) \operatorname{arctanh}\left(\frac{\sqrt{a + b \sinh(fx + e)^2}}{\sqrt{a}}\right)}{2a^5/2f} + \frac{2a - 3b}{2a^2f\sqrt{a + b \sinh(fx + e)^2}} - \frac{\operatorname{csch}(fx + e)^2}{2af\sqrt{a + b \sinh(fx + e)^2}}$$

Result(type 9, 42 leaves):

$$\frac{\operatorname{int/indef0}\left(\frac{\cosh(fx + e)^2}{\sinh(fx + e)^3 (a + b \sinh(fx + e)^2)^{3/2}}, \sinh(fx + e)\right)}{f}$$

Problem 137: Unable to integrate problem.

$$\int \frac{\coth(fx + e)^3}{(a + b \sinh(fx + e)^2)^{5/2}} dx$$

Optimal(type 3, 123 leaves, 6 steps):

$$-\frac{(2a - 5b) \operatorname{arctanh}\left(\frac{\sqrt{a + b \sinh(fx + e)^2}}{\sqrt{a}}\right)}{2a^7/2f} + \frac{2a - 5b}{6a^2f(a + b \sinh(fx + e)^2)^{3/2}} - \frac{\operatorname{csch}(fx + e)^2}{2af(a + b \sinh(fx + e)^2)^{3/2}} + \frac{2a - 5b}{2a^3f\sqrt{a + b \sinh(fx + e)^2}}$$

Result(type 9, 72 leaves):

$$\frac{\text{int/indef0}\left(\frac{\cosh(fx + e)^2}{(b^2 \sinh(fx + e)^4 + 2ab \sinh(fx + e)^2 + a^2) \sinh(fx + e)^3 \sqrt{a + b \sinh(fx + e)^2}}, \sinh(fx + e)\right)}{f}$$

Problem 139: Unable to integrate problem.

$$\int \coth(dx + c)^3 (a + b \sinh(dx + c)^2)^p dx$$

Optimal(type 5, 92 leaves, 3 steps):

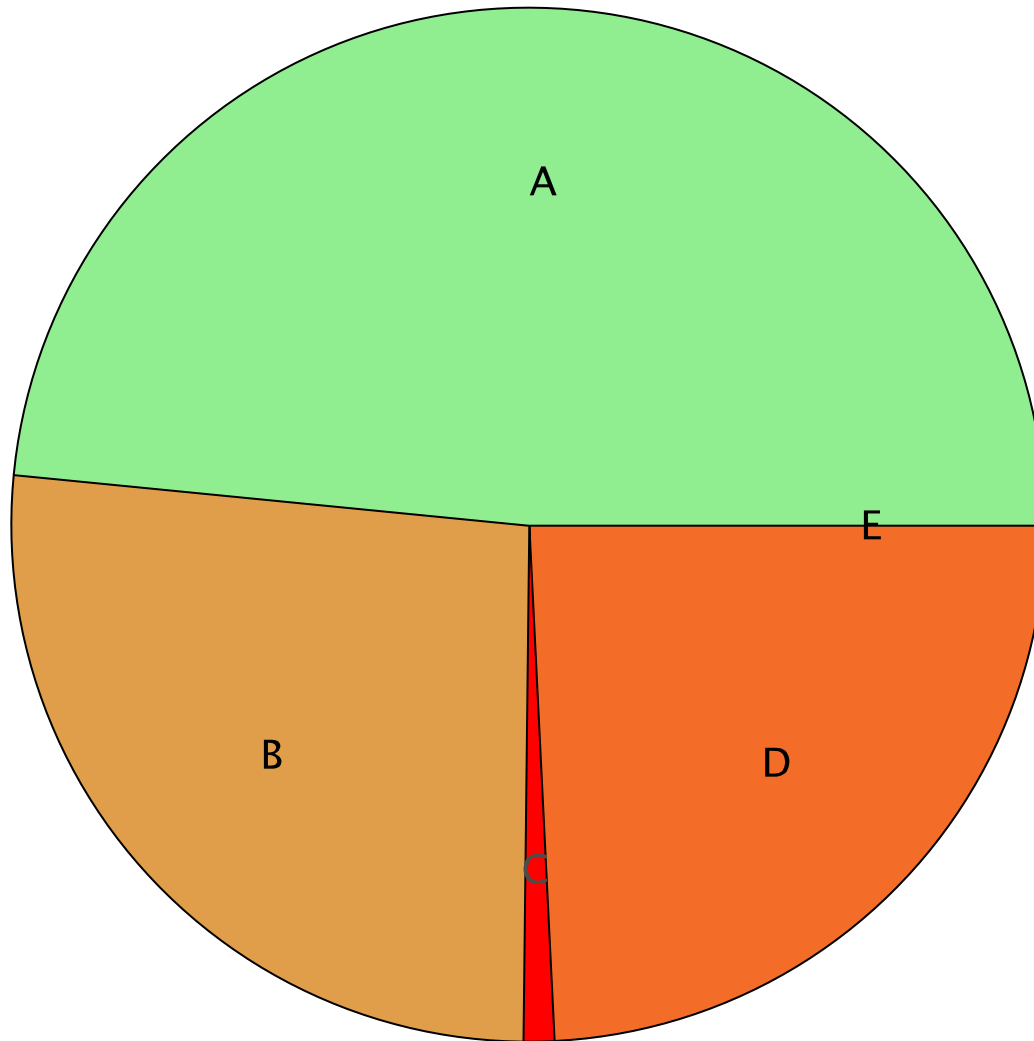
$$-\frac{\operatorname{csch}(dx + c)^2 (a + b \sinh(dx + c)^2)^{1+p}}{2ad} - \frac{(pb + a) \operatorname{hypergeom}\left([1, 1 + p], [2 + p], 1 + \frac{b \sinh(dx + c)^2}{a}\right) (a + b \sinh(dx + c)^2)^{1+p}}{2a^2 d (1 + p)}$$

Result(type 8, 25 leaves):

$$\int \coth(dx + c)^3 (a + b \sinh(dx + c)^2)^p dx$$

Summary of Integration Test Results

417 integration problems



A - 202 optimal antiderivatives  
B - 110 more than twice size of optimal antiderivatives  
C - 4 unnecessarily complex antiderivatives  
D - 101 unable to integrate problems  
E - 0 integration timeouts